

# HARRY GWALA DISTRICT

# **FET MATHEMATICS**

# GRADE 10 LOCKDOWN HOLIDAY LEARNER REVISION BOOKLET AUGUST 2020

Compiled by Harry Gwala FET Mathematics Advisors
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#### INTRODUCTION

An unprecedented Pandemic of COVID19 has hit South Africa and the World. This has put the lives of learners and teachers at risk and has negatively affected the education system. In KZN Grade 10 learners were taught the First Term Content and will only return to school on the 24 August 2020

In an effort to assist teachers and learners to use this time away from school effectively, Harry Gwala FET Mathematics Advisors have decided to compile a booklet to enable learners to revise the important content that was already taught in Term 1 namely: **Algebra Equations & Inequalities; Euclidean Geometry and Trigonometry**. This booklet includes these sections and contains work to be done daily by learners for 3 weeks from the 3<sup>rd</sup> August to 21<sup>st</sup> August and utilizes the DBE Final Examination Papers for the past four years. In an effort to let learners work independently the answers (not solutions) are provided at the back. These answers are just a guideline and it is envisioned that learners will complete daily tasks where they will provide the complete solutions to educators. Their efforts must be submitted to educators via social media where a control could will be kept. In the event where learners cannot submit work daily then they should present hard copies of all work to the educator on returning to school on the 24<sup>th</sup> August.

It is hoped that this booklet will allow teachers and learners to work in an effective and systematic way during the extended break so that when they return to school they will be ready to proceed with the remainder of the year's work.

In conclusion we would like to extend an earnest plea to all teachers and learners to abide by guidelines set by the NCCC and WHO to stay safe and prevent the spread of COVID19. We pray for your health and safety and look forward to continuing to assist you when you return in the new term. God Bless.

Kind Regards,

*Mr. M. Govender, Mr. S. Ngubo & Mr. N. Gopichund* (Harry Gwala FET Mathematics Advisors)

# WEEK 1 (3<sup>rd</sup> – 7<sup>th</sup> AUGUST 2020)

#### ALGEBRA, EQUATIONS AND INEQUALITIES

# MONDAY 3rd AUGUST

**DBE 2016** 

#### QUESTION 1

1.1 Factorise the following expressions fully:

1.1.1 
$$x^2 - x$$
 (1)

$$1.1.2 3x^2 + 3px - 2mx - 2mp (3)$$

1.1.3 
$$2p^2 - 2p - 12$$
 (3)

1.2 Simplify the following:

1.2.1 
$$\frac{2^{a+1} - 2^{a-1}}{2^a} \tag{3}$$

1.2.2 
$$\frac{x^2 - x + 1}{x^3 + 1} \div \frac{2x}{2x + 2} \tag{4}$$
 [14]

#### **QUESTION 2**

2.1 Solve for x:

$$2.1.1 x(x-1) = 20 (4)$$

$$2.1.2 \qquad \frac{3x-2}{2} = x+1 \tag{3}$$

2.2 Given:  $-4 \le -\frac{1}{2}m < 5$  where  $m \in \mathbb{R}$ 

2.2.1 Solve for 
$$m$$
. (3)

2.2.2 Write the answer to QUESTION 2.2.1 in interval notation. (1)

2.3 Given:  $4x^2 - y^2 = 171$  and 2x - y = 9

2.3.1 Calculate the value of 
$$2x + y$$
. (2)

2.3.2 Solve simultaneously for 
$$x$$
 and  $y$ . (3) [16]

# TUESDAY 4TH AUGUST

**DBE 2017** 

#### QUESTION 1

1.1 Given:  $q = \sqrt{b^2 - 4ac}$ 

1.1.1 Determine the value of 
$$q$$
 if  $a = 2$ ,  $b = -1$  and  $c = -4$ .  
Leave your answer in simplest surd form. (2)

1.1.2 State whether 
$$q$$
 is rational or irrational. (1)

1.1.3 Between which TWO consecutive integers does 
$$q$$
 lie? (1)

1.2 Factorise the following expressions fully:

1.2.1 
$$t^2(r-s)-r+s$$
 (3)

1.2.2 
$$\frac{x^3 + 1}{x^2 - x + 1}$$
 (2)

1.3 Simplify the following completely:

1.3.1 
$$(2y+3)(7y^2-6y-8)$$
 (2)

1.3.2 
$$\frac{3}{x^2 - 9} + \frac{2}{(x - 3)^2}$$
 (3)

1.3.3 
$$\frac{3^t - 3^{t-2}}{2 \cdot 3^t - 3^t} \tag{3}$$

#### **QUESTION 2**

2.1 Given: 4-2x < 16 where  $x \in R$ 

2.1.2 Hence, represent your answer to QUESTION 2.1.1 on a number line. (1)

2.2 Solve simultaneously for x and y:

$$-2x - y = 10$$
 and  $3x - 4y = -4$  (4)

2.3 Solve for x:

$$2.3.1 \qquad \frac{x(x-5)}{6} - 1 = 0 \tag{3}$$

$$2.3.2 c = \sqrt{a+2x} (2)$$

2.4 Tabelo is currently four times as old as his daughter, Linda. Six years from now, Tabelo will be three times as old as Linda.

# WEDNESDAY 5TH AUGUST

**DBE 2018** 

#### **QUESTION 1**

1.1 Factorise the following expressions fully:

1.1.1 
$$4x - x^3$$
 (2)

$$1.1.2 x^2 + 15x - 54 (2)$$

1.1.3 
$$y - xy + x - 1$$
 (3)

1.2 Simplify the following expressions fully:

1.2.1 
$$(x+2)(x^2-x+3)$$
 (2)

$$1.2.2 \qquad \frac{5}{x+3} - \frac{3}{2-x} \tag{3}$$

1.2.3 
$$\frac{25^{-x}.15^{x+1}}{3^x.5^{-x}} \tag{3}$$

1.3 Determine the value of 
$$(3p+q)^2$$
 if  $9p^2+q^2=12$  and  $pq=-3$ . (3)

#### **QUESTION 2**

2.1 Solve for x:

$$2.1.1 px + qx = a (2)$$

$$2.1.2 2x^2 - 5x + 2 = 0 (3)$$

$$2.1.3 \qquad \left(\frac{1}{2}\right)^{3x+1} = 32 \tag{3}$$

2.2 Given:  $-11 \le 3m - 8 < 4$ 

2.2.1 Solve for 
$$m$$
. (2)

2.2.2 Hence, write down the number of integers that satisfy the inequality. (1)

2.3 Solve simultaneously for x and y if:

$$5x + 4y = 21$$
 and  $2x = 3 - y$  (4)

[15]

# THURSDAY 6TH AUGUST

**DBE 2019** 

#### **QUESTION 1**

1.1 Factorise the following expressions fully:

1.1.1 
$$3y^2 + y$$
 (1)

$$1.1.2 x^2 - 10x - 24 (2)$$

1.1.3 
$$9x^2 - y^2 + 10y - 25$$
 (3)

1.2 Simplify the following expressions fully:

1.2.1 
$$\left(4 + \frac{1}{x}\right)\left(2 - \frac{3}{x}\right)$$
 (2)

1.2.2 
$$\frac{5x-5}{5x}$$
 (2)

1.2.3 
$$\frac{3^{x+1}+3^x}{27.3^{-1+x}}$$
 (3)

#### **QUESTION 2**

2.1 Solve for x:

$$2.1.1 2x^2 - 10x = 0 (2)$$

$$2.1.2 px - kx = k - p (3)$$

$$2.1.3 2^{\frac{x}{3}} = \frac{1}{128} (3)$$

2.2 Given:  $\frac{x+5}{2} > -2$ 

2.2.1 Solve for 
$$x$$
. (2)

2.2.2 If  $x \in R$ , represent the solution to QUESTION 2.2.1 on a number line. (1)

2.3 Solve simultaneously for x and y if:

$$x(x-3) + y(3-x) = 0 (4)$$

2.4 During a fundraising event, only R10, R20 and R50 notes were collected. In the final count, there were twice as many R20 notes as there were R50 notes, and 15 more R10 notes than R50 notes.

If R10 150 was collected in total, determine the number of R10, R20 and R50 notes that were collected.

(4) [19]

# FRIDAY 7TH AUGUST – REVISION & CONSOLIDATION OF WEEK'S WORK

# WEEK 2 $(10^{th} - 14^{th} \text{ AUGUST } 2020)$

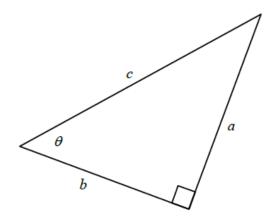
#### **TRIGONOMETRY**

# MONDAY 10<sup>TH</sup> AUGUST

**DBE 2016** 

#### **QUESTION 4**

4.1 A right-angled triangle has sides a, b and c and the angle  $\theta$ , as shown below.



4.1.1 Write the following in terms of a, b and c:

(a) 
$$\cos \theta$$
 (1)

(b) 
$$tan \theta$$
 (1)

(c) 
$$\sin(90^{\circ} - \theta)$$
 (2)

4.1.2 If it is given that a = 5 and  $\theta = 50^{\circ}$ , calculate the numerical value of b. (2)

4.2 Given that  $\hat{A} = 38.2^{\circ}$  and  $\hat{B} = 146.4^{\circ}$ .

Calculate the value of 2cosecA + cos3B. (3)

4.3 Simplify fully, WITHOUT the use of a calculator:

$$\frac{\sin 45^{\circ}.\tan^2 60^{\circ}}{\cos 45^{\circ}} \tag{4}$$

4.4 Given that  $5\cos \beta - 3 = 0$  and  $0^{\circ} < \beta < 90^{\circ}$ .

If 
$$\alpha + \beta = 90^{\circ}$$
 and  $0^{\circ} < \alpha < 90^{\circ}$ , calculate the value of cot  $\alpha$ . (4) [17]

# TUESDAY 11<sup>TH</sup> AUGUST

**DBE 2017** 

#### **QUESTION 4**

- 4.1 Given  $4 \cot \theta + 3 = 0$  and  $0^{\circ} < \theta < 180^{\circ}$ .
  - 4.1.1 Use a sketch to determine the value of the following. DO NOT use a calculator.

(a) 
$$\cos \theta$$
 (4)

(b) 
$$\frac{3\sin\theta\sec\theta}{\tan\theta}$$
 (4)

- 4.1.2 Hence, show that  $\sin^2 \theta 1 = -\cos^2 \theta$ . (3)
- 4.2 Simplify the following expression WITHOUT using a calculator:

$$\cos 30^{\circ} \tan 60^{\circ} + \csc^2 45^{\circ} \sin^2 60^{\circ}$$
 (3)

4.3 Solve for  $\theta$  correct to TWO decimal places, if

$$\frac{4}{3}\sin\theta = \cos 37^{\circ} \text{ and } 0^{\circ} \le \theta \le 90^{\circ}.$$
(2)

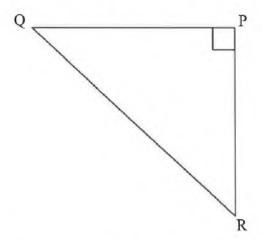
[16]

# WEDNESDAY 12TH AUGUST

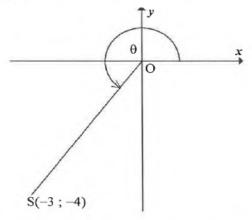
#### **DBE 2018**

## QUESTION 3

3.1 In the diagram below,  $\triangle QPR$  is a right-angled triangle with  $Q\hat{P}R = 90^{\circ}$ .



- 3.1.1 Use the sketch to determine the ratio of  $tan(90^{\circ} R)$ . (1)
- 3.1.2 Write down the trigonometric ratio that is equal to  $\frac{QR}{QP}$ . (1)
- 3.2 S(-3; -4) is a point on the Cartesian plane such that OS makes an angle of  $\theta$  with the positive x-axis.



Calculate the following WITHOUT using a calculator:

3.2.2 The value of 
$$\sec \theta + \sin^2 \theta$$
 (3)

3.3 Determine the value of the following WITHOUT using a calculator:

$$\frac{\cos 45^{\circ}}{\sin 90^{\circ}. \tan 60^{\circ}}$$
 (4)

# THURSDAY 13<sup>TH</sup> AUGUST

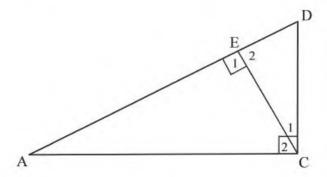
#### **DBE 2019**

#### **QUESTION 3**

3.1 If 
$$x = 37^{\circ}$$
 and  $y = 44^{\circ}$ , calculate the value of  $\sin^2 x + 2\cos y$ . (1)

3.2 WITHOUT using a calculator, determine the value of 
$$\frac{\sin 30^{\circ}.\cot 45^{\circ}}{\cos 30^{\circ}.\tan 60^{\circ}}$$
 (3)

3.3 In the diagram below, ΔACD is right-angled at C. E lies on AD such that CE is perpendicular to AD.



3.3.1 Write down the ratio for 
$$\cos D$$
 in  $\triangle ACD$ . (1)

3.3.2 Write down the ratio for 
$$\cos D$$
 in  $\Delta CED$ . (1)

3.3.3 If 
$$AD = 13$$
 units and  $DC = 5$  units, calculate the length of ED. (2)

3.4 Given that  $\cos \theta = \frac{5}{13}$  and  $\sin \theta < 0$ .

With the aid of a diagram and WITHOUT using a calculator, determine the value of:

3.4.1 
$$\sin \theta$$
 (3)

3.4.2 
$$\sec \theta + \tan^2 \theta + 1$$
 (4)

# FRIDAY 14<sup>TH</sup> AUGUST – REVISION & CONSOLIDATION OF WEEK'S WORK

# WEEK 3 $(17^{TH} - 21^{ST} \text{ AUGUST 2020})$

#### **EUCLIDEAN GEOMETRY**

## MONDAY 17<sup>TH</sup> AUGUST

**DBE 2016** 

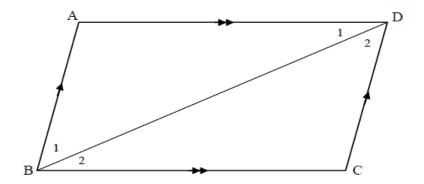
Give reasons for your statements in QUESTIONS 8 and 9.

#### **QUESTION 8**

8.1 Complete the following statement:

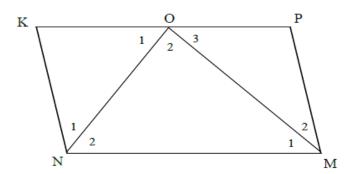
If the opposite angles of a quadrilateral are equal, then the quadrilateral ... (1)

8.2 Use the sketch below to prove that the opposite sides of a parallelogram are equal.



(6)

8.3 In the sketch below, KPMN is a parallelogram. ON bisects KNM and OM bisects NMP.



8.3.1 Show that  $NOM = 90^{\circ}$ . (3)

8.3.2 Prove that O is the midpoint of KP. (6)

[16]

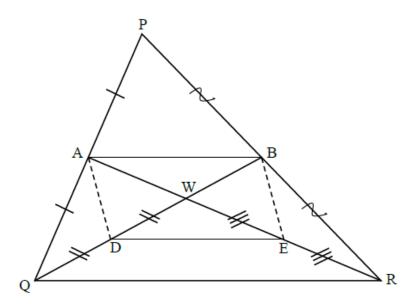
#### **QUESTION 9**

9.1 Complete the following statement:

The line through the midpoint of two sides in a triangle is parallel to and ... the third side.

(1)

9.2 In ΔPQR, A and B are the midpoints of sides PQ and PR respectively. AR and BQ intersect at W. D and E are points on WQ and WR respectively such that WD = DQ and WE = ER.



Prove that ADEB is a parallelogram.

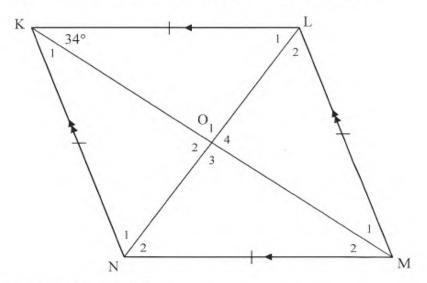
(5)

[6]

# TUESDAY 18<sup>TH</sup> AUGUST

#### DBE 2017 QUESTION 8

8.1 KLMN is a rhombus with diagonals intersecting at O.  $L\hat{K}M = 34^{\circ}$ .



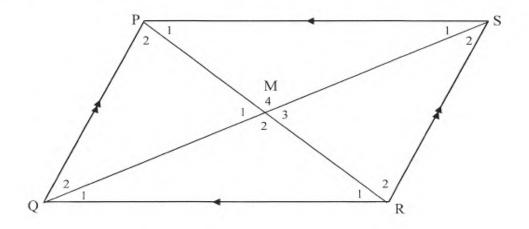
8.1.1 Write down the size of  $\hat{O}_1$ . (1)

8.1.2 Calculate the size of  $\hat{L}_1$ . (2)

8.1.3 Calculate the size of KNM. (2)

8.2 Given parallelogram PQRS with diagonals PR and QS intersecting at M.

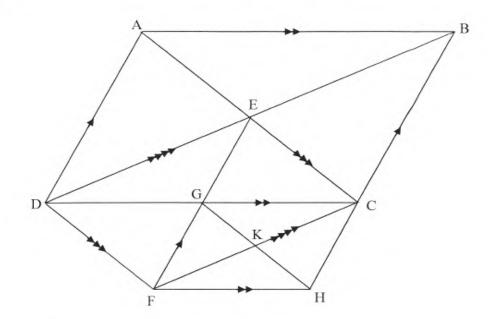
8.2 Given parallelogram PQRS with diagonals PR and QS intersecting at M.



Prove that the diagonals bisect each other.

(4)

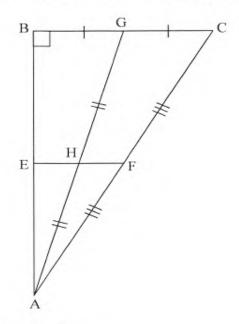
8.3 In the diagram, ABCD is a parallelogram with diagonals intersecting at E. The diagonals of parallelogram DECF intersect at G. The diagonals of parallelogram FGCH intersect at K.



Prove that 
$$DB = 4KC$$
. (4) [13]

#### **QUESTION 9**

 $\Delta ABC$  is right-angled at B. F and G are the midpoints of AC and BC respectively. H is the midpoint of AG. E lies on AB such that FHE is a straight line.



9.1 Prove that E is the midpoint of AB.

- (3)
- 9.2 If EH = 3,5 cm and the area of  $\triangle AEH = 9,5 \text{cm}^2$ , calculate the length of AB.
- (3)

Hence, calculate the area of ΔABC.

(3)

# WEDNESDAY 19<sup>TH</sup> AUGUST

#### **DBE 2018**

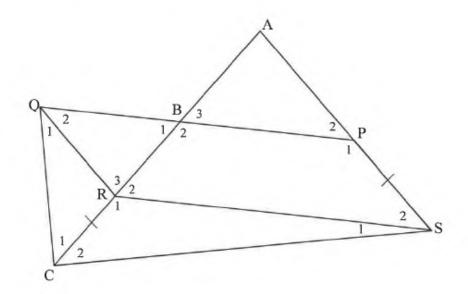
#### **QUESTION 7**

7.1 Complete the statement so that it is TRUE:

> The line drawn from the midpoint of the one side of a triangle, parallel to the second side, ...

(1)

7.2 ACS is a triangle. P is a point on AS and R is a point on AC such that PSRQ is a parallelogram. PQ intersects AC at B such that B is the midpoint of AR. QC is joined. Also, CR = PS,  $\hat{C}_1 = 50^{\circ}$  and BP = 60 mm.



7.2.1 Calculate the size of A. (5)

7.2.2 Determine the length of QP. (3)

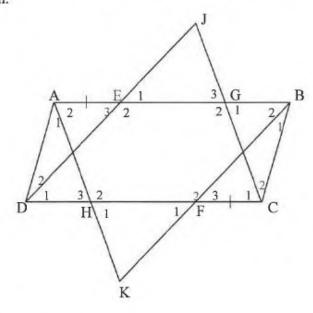
[9]

# Downloaded from Stanmorephysics.com

#### HARRY GWALA DISTRICT QUESTION 8

#### **FET MATHEMATICS**

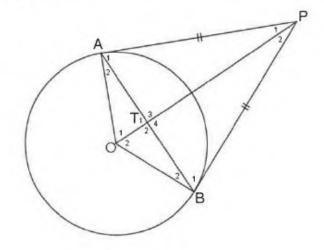
8.1 ABCD is a parallelogram. E and F are points on AB and DC respectively such that AE = CF. DE is produced to J and CJ is drawn. BF is produced to K and AK is drawn.



Prove that:

8.1.2 
$$\hat{E}_1 = \hat{F}_1$$
 (4)

8.2 In the diagram below O is the centre of the circle. A and B lie on the circumference of the circle. AP = BP.



Prove that:

$$8.2.1 \qquad AT = BT \tag{5}$$

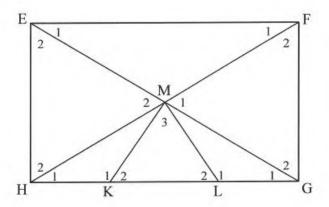
8.2.2 
$$O\hat{T}A = 90^{\circ}$$
 (1) [15]

# THURSDAY 20<sup>TH</sup> AUGUST

**DBE 2019** 

#### **QUESTION 7**

7.1 In the diagram, EFGH is a rectangle having diagonals intersecting at M.  $\hat{M}_2 = 60^\circ$  and  $\hat{L}_2 = 40^\circ$ .

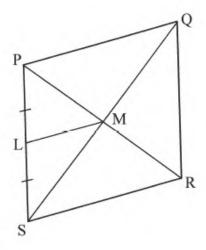


Calculate the size of:

7.1.1 
$$\hat{F}_{1}$$
 (2)

$$7.1.2$$
 G $\hat{M}$ L (3)

7.2 PQRS is a rhombus with diagonals PR and SQ intersecting at M. The perimeter of the rhombus is 12 cm. L is the midpoint of PS.



Calculate the length of LM.

(4)

[9]

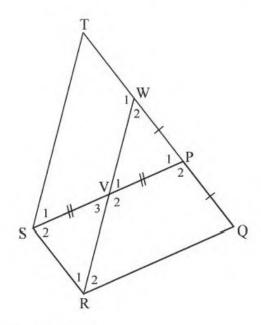
(1)

## **QUESTION 8**

8.1 Complete the statement so that it is TRUE:

The diagonals of a parallelogram ... each other.

8.2 In the diagram below, P is the midpoint of side WQ of ΔWQR. V is on WR such that VP||RQ. PV is produced by its own length to S. PW is produced to T and ST drawn.



- 8.2.1 Give a reason why WV = VR. (1)
- 8.2.2 Prove that:

(a) 
$$\Delta VWP \equiv \Delta VRS$$
 (3)

- (b) SWPR is a parallelogram (2)
- (c) PQRS is a parallelogram (3)
- 8.2.3 If it is further given that RSTW is a parallelogram, show that TQ = 3SR. (2) [12]

# FRIDAY 21ST AUGUST – REVISION & CONSOLIDATION OF WEEK'S WORK

# ANSWERS TO QUESTIONS

## WEEK 1

MATHEMATICS PAPER 1 (DBE NATIONAL PAPER (2016)	
Algebra,	Equations and Inequalities
1.1.1	x(x-1)
1.1.2	(3x-2m)(x+p)
1.1.3	2(p-3)(p+2)
1.2.1	$x = \frac{3}{2}$
1.2.2	$\frac{1}{x}$
2.1.1	x = 5  or  x = -4
2.1.2	x = 4
2.2.1	$-10 < m \le 8$
2.2.2	(-10; 8]
2.3.1	2x + y = 19
2.3.2	x = 7  and  y = 5

MAT	HEMATICS PAPER 1 (DBE NATIONAL PAPER (2017)
	ra, Equations and Inequalities
1.1.1	$q = \sqrt{33}$
1.1.2	Irrational
1.1.3	5 and 6
1.2.1	(r-s)(t+1)(t-1)
1.2.2	(x+1)
1.3.1	$14y^3 + 9y^2 - 34y - 24$
1.3.2	$\frac{5x-3}{(x-3)^2(x-3)}$
	$(x-3)^2(x+3)$
2.1.1	<u>8</u>
2.1.2	·
	<b>→</b>
	-6 0
2.1.3	x > -6
2.2	x = -4 $y = -2$
2.3.1	x = 6 or $x = -1$
2.3.2	$x = \frac{c^2 - a}{a}$
	2
2.4	x = 12

MAT	HEMATICS PAPER 1 (DBE NATIONAL PAPER (2018)
Algeb	ra, Equations and Inequalities
1.1.1	x(2-x)(2+x)
1.1.2	(x+18)(x-3)
1.1.3	(y-1)(1-x)
1.2.1	$x^3 + x^2 + x + 6$
1.2.2	8x-1
	(x+3)(x-2)
1.2.3	15
1.3	-6
2.1.1	$x = \frac{a}{p+q} \; ; \; p \neq -q$
2.1.2	$x = \frac{1}{2}  \text{or}  x = 2$
2.1.3	x = -2
2.2.1	$-1 \le m < 4$
2.2.2	5

MAT	HEMATICS PAPER 1 (DBE NATIONAL PAPER (2019)
	ra, Equations and Inequalities
1.1.1	y(3y+1)
1.1.2	(x-12)(x+2)
1.1.3	(3x+y-5)(3x-y+5)
1.2.1	$8 - \frac{10}{x} - \frac{3}{x^2}$ $\frac{x-1}{x}$
1.2.2	$\frac{x-1}{x}$
1.2.3	4 9
2.1.1	x = 0  or  x = 5
2.1.2	x = -1
2.1.3	x = -21
2.2.1	x > -9
2.2.2	-9 x
2.3	x = 3  or  y = x = 3
2.4	x = 100

# WEEK 2

MATHEMATICS PAPER 2 (DBE NATIONAL PAPER (2016)	
Trigonometr	<i>y</i>
4.1.1(a)	$\frac{b}{c}$
4.1.1 (b)	$\frac{a}{b}$
4.1.3(c)	$\frac{b}{c}$
4.1.2	b= 4.20
4.2	3.42
4.3	3
4.4	$\cot \alpha = \frac{4}{3}$

MATHE	MATHEMATICS PAPER 2 (DBE NATIONAL PAPER (2017)	
4.1.1(a)	$\cos\theta = -\frac{3}{5}$	
4.1.2(b)	$\sin^2\theta - 1 = -\cos^2\theta.$	
4.2	3	
4.3	$\theta = 36.8^{\circ}$	

MATH	MATHEMATICS PAPER 2 (DBE NATIONAL PAPER (2018)	
3.1.1	$\underline{q}$	
	r	
3.1.2	sec Q	
3.2.1	5	
3.2.2	<u>-77</u> 75	
3.3	$\frac{2}{\sqrt{6}}$	

MATH	MATHEMATICS PAPER 2 (DBE NATIONAL PAPER (2019)	
3.1	1,80	
3.2	$\frac{1}{3}$	
3.3.1	$\cos D = \frac{cD}{AD}$	
3.3.2	$\cos D = \frac{DE}{CD}$	
3.3.3	ED=1,92	

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HARRY GWALA DISTRICT		GWALA DISTRICT	FET MATHEMATICS
	3.4.1	-12	
		$\sin \theta = \frac{13}{13}$	
	3.4.2	234	

# WEEK 3 MATHEMATICS PAPER 2 (DBE NATIONAL PAPER (2016)

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8.1	Is parallel
8.2	Proof
8.3.1	Proof
8.3.2	Proof
9.1	Half the length
9.2	Proof

## MATHEMATICS PAPER 2 (DBE NATIONAL PAPER (2017)

8.1.1	$\hat{0}_1 = 90^{\circ}$
8.1.2	$\hat{L}_1 = 56^{\circ}$
8.1.3	$K\widehat{M}N = 112^{\circ}$
8.2	Proof
8.3	Proof
9.1	Proof
9.2	10,86cm
9.3	76cm <sup>2</sup>

# MATHEMATICS PAPER 2 (DBE NATIONAL PAPER (2018)

7.1	Bisects the third side
7.2.1	$\widehat{A} = 100^{\circ}$
7.2.2	QP = 120
8.1.1	Proof
8.1.2	Proof
8.2.1	Proof
8.2.2	$0\widehat{T}A = 90^{\circ}$

## MATHEMATICS PAPER 2 (DBE NATIONAL PAPER (2019)

7.1.1	$\hat{F}_1 = 30^{\circ}$
7.1.2	$\widehat{GML} = 10^{\circ}$
7.2	LM=1,5cm
8.1	Bisect each other
8.2.1	The line drawn from the midpoint of one side of a triangle parallel to the other side
	bisects the third side.
8.2.2a	Proof
8.2.2b	Proof
8.2.2c	Proof
8.3	Proof

ALL DBE November National Papers from 2016-2019 were utilized when compiling this document.