

SENIOR PHASE

GRADE 9

NOVEMBER 2016

MATHEMATICS

MARKS: 100

TIME: 2 hours





This question paper consists of 13 pages including an information sheet.

INSTRUCTIONS AND INFORMATION

- 1. Read the following instructions carefully.
- 2. Answer ALL the questions.
- 3. Write neatly and legibly.
- 4. Number your answers exactly as questions are numbered.
- 5. Give reasons for each statement in QUESTION 5 and QUESTION 6.
- 6. Show ALL working.
- 7. You may use an approved scientific calculator (non-programmable and non-graphical).
- 8. Diagrams are NOT necessarily drawn to scale.
- 9. Use attached ANNEXTURE A to answer QUESTION 3.3.



In this question, write only the correct letter next to the corresponding number, e.g. If the correct answer for question 1.1 is D, write **1.1 D** only.

1.1	What	is the correct pair of values of x in $(x - 3)(x + 2) = 0$?	
ĥ	A	x = -3 and $x = -2$	
f	в	x = 3 and x = -2	
	С	x = -3 and $x = 2$	(1)
	D	x = 3 and x = 2	(1)
1.2	What	is the HCF of 210 and 350?	
	А	$2 \times 5 \times 5 \times 7$	
	В	$2 \times 3 \times 5 \times 7$	
	С	$2 \times 5 \times 7$	
	D	5 × 7	(1)
1.3	Calcu	late: $6 + 6 \div 2 - 6 \times (-2)$	
	А	21	
	В	18	
	С	12	
	D	0	(1)
1.4	Deter	mine the next term in the pattern 2; 5; 9; 14;?	
	А	21	
	В	20	
	С	19	
	D	18	(1)
1.5	Whicl	n of the following statements is true about a kite?	
	А	The longer diagonal bisects the shorter diagonal at 90°.	
	В	The shorter diagonal bisects the longer diagonal at 90°.	
	С	Diagonals bisect each other.	

D Diagonals are equal.

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- 1.8 What will be the total surface area of a cube with a volume of 64 cm³?
 - A 96 cm²
 - B 64cm²
 - C 16 cm²
 - D 4 cm²

(1)



1.9 What is the length of AD in the figure below?



(1)

1.10 What is the mode of the scores presented in the frequency distribution table below?

Score	Frequency
111	2
112,1	7
114,3	6
115	2
211	1

A 118,5

B 113,6

C 112,1

D 100



(1) **[10]**

5

- 2.1 Write 0,000 000 674 in scientific notation. (1)
- 2.2 Simplify:

IU

2.1.1
$$\sqrt[3]{x^3} + x^0$$
 (2)

2.1.2
$$\sqrt{0.03 x^8 + 0.01 x^8}$$
 (2)

2.2.2
$$\frac{(2d^2e)^2}{(4d^{-3}e^{-2})^{-1}}$$
(3)

2.2.4
$$2(x+2)^2 - 2(x+1)(x+2)$$
 (4)

2.3 Factorise completely:

2.3.1 $x^2 + 5x - 24$ (2)

2.3.2
$$2(a-b) - b + a$$
 (3)

2.4 Solve for *x*:

2.4.1 4x - 10 = 6(2)

$$\frac{2.4.2}{2} = \frac{3x - 10}{2} = \frac{2x - 5}{3}$$
(3)

2.4.3
$$x^2 = 4$$
 (2)

2.4.4
$$3x^5 = 96$$
 (2)

[26]



3.1 Study the geometric pattern below and answer the questions that follow.

FIGURE 1	FIGURE 2		FIGURE 3
Figure	1	2	3

3.1.1 Complete the table.

6

Number of lines

- (1)
- 3.1.2 Write down the general rule for the pattern in the form $T_n =$. (2)

11

3.2 Study the straight line graphs below and answer the questions that follow.



3.2.1 Write down the equation of AB. (1	(1)
---	-----

- 3.2.2 Write down the equation of AD. (1)
- 3.3 On the attached grid, draw a graph defined by y = -2x + 1. Remove the ANNEXURE and attach it in your ANSWER BOOK.

(3) [**8**]

4.1 How long will it take an investment of R5 000 at 12% per annum simple interest to earn R1 800 interest? (3)
4.2 The sum of two numbers is 143 and their difference is 7, what are the numbers? (3)
4.3 There are 10 boxes, five contain pencils, four contain pens and two contain pens and pencils. How many boxes contain no pens and pencils? (2)
4.4 A car travelling at an average speed of 100 km/h covers a certain distance in 3 hours. At what average speed must the car travel to cover the same distance in 2 hours? (4)

QUESTION 5

5.1 In the diagram below $A\hat{B}E = 65^{\circ}$ and $D\hat{C}F = 32^{\circ}$.



- 5.1.1 Calculate the size of $E\hat{B}C$. Give reasons for your answer. (2)
- 5.1.2 Calculate the size of \widehat{AB} . Give reasons for your answer. (3)



5.2 In the diagram below, $\widehat{CAB} = 2x - 48^\circ$, $\widehat{ABC} = x + 14^\circ$ and $\widehat{BCE} = 116^\circ$.



5.2.1	Calculate the value of x . Give reasons for your answer.	(3)
5.2.2	Calculate the actual size of \widehat{CAB} .	(2)
5.2.3	What type of Δ is ΔABC ? Give reasons for your answer.	(2)

5.3 In the figure below, O is the centre of the circle.



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QUESTION 6

6.1 In the diagram below, prove that $\Delta KLM \equiv \Delta KNM$. (4)



6.2 In the diagram below, AB || PQ.



- 6.2.1 Prove that $\triangle ABO \parallel \mid \triangle PQO$.
- 6.2.2 Calculate the value of *x*.

(4)

(3) **[11]**



7.1 In the figure below ABCD is a square and AOD is the diameter of the circle. Calculate the area of the shaded part if r = 7 cm. N.B $\pi = \frac{22}{7}$



7.2 A rectangular carpet has a perimeter of 16 m and an area of 15 m^2 . What are the dimensions of the sides of the carpet?

(4) **[8]**



(4)

8.1 A spinner with 5 colours, red, yellow, green, black and white is spun and a coin is tossed, at the same time.



Draw a tree diagram to illustrate the number of possible outcomes for the experiment.

(2)

(1)

- 2 What is the probability of spinning any colour and tossing a head? (1)
- 1.3 What is the probability of spinning a red colour?
- 8.2 The pie chart below shows different modes of transport used by learners of Boiteko Junior Secondary School when travelling to school. The total number of learners in the school is 600. Study the graph and answer the questions that follow.







Although great care is taken with the setting and quality assurance of question paper, unfortunately due to various factors, errors due creep in. In order to ensure that learners are not disadvantaged in any way, it is requested that the following must be brought to the attention of learners before they start to write.

ERRATA FOR GRADE 9 MATHS PAPER BEFORE WRITING COMMENCES

QUESTION PAPER

ITEM NO.	INCORRECT STATEMENT	CORRECT STATEMENT/ SUGGESTIONS
1.7	Which of the following statements has the same effect as rotating an object about the line $y = x$?	Which of the following statements has the same effect as rotating an object 270° clockwise about the origin?
2.2	Numbering is incorrect.	The correct numbering is:
	2.1.1	<mark>2.2.1</mark>
	<mark>2.1.2</mark>	2.2.2
	2.2.2	2.2.3

3.2	The points on the graph have shifted.	The correct graph with correct points is drawn
		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
4.3	There are 10 boxes, five contain pencils, four contain pens and two contain pens and pencils. How many boxes contain no pens and pencils?	There are 10 boxes, five contain pencils, four contain pens and two contain pens and pencils. How many boxes contain neither pens nor pencils (i.e. no pens and no pencils)?
6.2	In the diagram below, AB PQ.	In the diagram below, AB \parallel PQ , OB= 5 cm and QO = x.
8.2	The sectors are all labelled as CATEGORY	Sectors are labelled differently as Own transport , Bus and Walk



We want to apologise for any inconvenience caused and please note that the errata was issued to ensure that learners are assessed in the most accurate and fair manner.

Yours in education.

MS N. MBELEKI CES: INSTRUMENT DEVELOPMENT SECTION



THIS MUST BE <u>ISSUED ONLY</u> TO MARKERS OF THE PAPER AFTER THE PAPER HAS BEEN WRITTEN.

MEMORANDUM

ITEM NO.	INCORRECT ANSWER	CORRECT ANSWER
1.7		B
	4	
2.3.2	2(a-b)-b+a	2(a-b)-b+a
	$\frac{2(a-b)-1(b-a)}{\checkmark} \checkmark M$	$2(a-b)+1(a-b) \checkmark M$
	$2(a-b)+1(a-b) \checkmark M$	$(2+1)(a-b) \checkmark \mathbf{M}$
	$3(a-b) \checkmark \mathbf{A}$	$3(a-b) \checkmark \mathbf{A}$
2.4.3		Alternative response
		$x^2 = (\pm 2)^2 \checkmark \mathbf{M}$
		$x = -2 \text{ or } x = 2 \checkmark \mathbf{A}$

We want to apologise for any inconvenience caused and please note that the errata was issued to ensure that learners are assessed in the most accurate and fair manner.

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MS N. MBELEKI CES: INSTRUMENT DEVELOPMENT SECTION







SENIOR PHASE

GRADE 9

NOVEMBER 2016

MATHEMATICS MEMORANDUM

MARKS: 100



This memorandum consists of 9 pages.

NOTE:

- This is marking guideline. In instances where learners have used different mathematically sound strategies to solve the problems, they should be credited.
- Underline errors committed by learners and apply Consistent Accuracy (CA) marking.

	KEY
M	Method mark
CA	Consistent Accuracy mark
А	Accuracy mark
S	Statement
R	Reason
S/R	Statement and Reason

QUES	FION 1	[10 marks]		
Ques.			Mark Allocation	Total
1.1	В	✓	1 mark for each correct answer	(1)
1.2	С	✓		(1)
4.0				(4)
1.3	A	•		(1)
1.4	В	✓		(1)
1.5	Δ			(1)
1.5	<u> </u>			(1)
1.6	D	✓		(1)
1.7	С	✓		(1)
1.8	Λ			(1)
1.0				
1.9	С	✓		(1)
1.10	С	✓		(1)
				[10]

QUESTION 2 [26 marks]				
Ques.	Solution	Mark Allocation	Total	
2.1	$6,74 \times 10^{-7} \checkmark A$	Answer: 1 mark	(1)	
2.2.1	$\sqrt[3]{x^3} + x^0$	<i>x</i> : 1 mark		
Ш		+1: 1 mark		
	x + 1		(2)	
2.2.2	$\sqrt{0.03 x^8 + 0.01 x^8}$	$\sqrt{0.04 x^8}$: 1 mark		
	$\sqrt{0.04 x^8}$ \checkmark A	Answer: 1 mark		
	$0,2 x^4 \checkmark A$		(2)	
2.2.3	$(2d^2e)^2$	$2^2 d^4 e^2$: 1 mark		
	$\overline{(4d^{-3}e^{-2})^{-1}}$	$2^2 d^{-3} e^{-2}$: 1 mark		
	✓ M ✓ M	Answer: 1 mark		
	$2^2 d^4 e^2 \times 2^2 d^{-3} e^{-2}$			
0.0.4	$16d \checkmark A$	2	(3)	
2.2.4	$2(x+2)^{2} - 2(x+1)(x+2)$	$x^2 + 4x + 4$: 1 mark		
	$\bigvee M \qquad \checkmark M$ 2(x ² + 4x + 4) - 2(x ² + 3x + 2)	$x^2 + 3x + 2:1$ mark		
	$2x^2 + 8x + 8 - 2x^2 - 6x - 4$	$2x^2 + 8x + 8 - 2x^2 - 6x - 4$		
	$2x + 4 \checkmark CA$: 1 mark		
2.2.4		Answer: 1 mark	(4)	
2.3.1	$x^{-} + 5x - 24$	x + 8: 1 mark		
	$\bigvee \mathbf{A} \checkmark \mathbf{A}$	x - 3: 1 mark		
	(x+8)(x-3)		(2)	
2.3.2	2(a-b) - b + a	+1(a - b; 1 mark)	(2)	
_	$\frac{2(a-b)+1(a-b)}{2(a-b)} \checkmark \mathbf{M}$	(2+1)(a-b): 1 mark		
	$(2+1)(a-b) \checkmark M$	Answer : 1 mark		
	3(a-b)			
2/1	4x - 10 - 6	4x - 16.1 mark	(3)	
2.7.1	4x - 16 - 4	4x = 10.1 mark		
	$r_{\lambda} = 10$ V M		$\langle \mathbf{O} \rangle$	
212	3r - 10 $2r - 5$	× I CD: 6: 1 mark	(2)	
2.7.2	$\frac{3x^{2}}{2} = \frac{2x^{2}}{3}$			
		9x - 30 = 4x - 10: 1 mark		
	$6 \times \left(\frac{3x-10}{2}\right) = 6 \times \left(\frac{2x-5}{3}\right) \checkmark M$	Answer: 1 mark		
	$9x - 30 = 4x - 10 \qquad \checkmark \mathbf{A}$			
	5x = 20			
	$x = 4$ \checkmark CA		(3)	

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2.4.3	$x^2 = 4$	(x+2)(x-2) = 0: 1 mark	
F	$(x+2)(x-2) = 0 \checkmark \mathbf{M}$	Answer: 1 mark	
	$x = -2$ or $x = 2$ $\checkmark A$		(2)
2.4.4	$3x^5 = 96$	2 ⁵ : 1 mark	
	$x^5 = 32$	Answer: 1 mark	
	$x^5 = 2^5 \checkmark M$		
	$x = 2$ \checkmark A		(2)
	7		[26]
QUEST	TON 3 [8 marks]		
Ques	Solution	Mark Allocation	Total
311		Answer: 1 mark	(1)
3.1.2		5 <i>n</i> : 1 mark	(1)
	✓ A ✓ A	2	
	5n + 1	+1: 1 mark	(2)
3.2.1	$y = x \checkmark \mathbf{A}$	Answer: 1 mark	(1)
3.2.2	$x = -2$ $\checkmark \mathbf{A}$	Answer: 1 mark	(1)
	Y		
	5		
	y = -2x + 1		
	3		
	-5 -4 -3 -2 -1 0	$1 \qquad 2 \qquad 3 \qquad 4 \qquad 5 \qquad X$	
	-1		
	-2		
	-3		
	-4		
	-5		
	↓ ↓ ↓ ↓ ↓ ¥		
	y intercept : $y = +1$ $\checkmark A$		
	x intercept : $x = \frac{1}{2}$ \checkmark A		(-)
	label 🗸 A		(3)
			[8]

Questio	Question 4 [12 marks]						
Ques.	Solution	Mark Allocation	Total				
4.1	$p.n.i = SI \checkmark M$	Formula: 1 mark					
	$5000 \times n \times 0,12 = 1800$ $\checkmark M$	Substitution: 1 mark					
	$n=3$ $\checkmark \mathbf{A}$	Answer: 1 mark					
	OR						
	$A = P(1+ni) \checkmark \mathbf{M}$						
	$6\ 800 = 5\ 000(1+0,12n) \checkmark \mathbf{M}$						
	1.36 = 1 + 0,12n						
	0,36 = 0,12n						
	$n=3$ $\checkmark \mathbf{A}$		(3)				
4.2	Let the numbers be a and b $\checkmark M$ a + b = 143	Any method: 1 mark					
	a-b=7	75: 1 mark					
	a = b + 7						
	b + 7 + b = 143	68: 1 mark					
	2b = 136						
	b = 68						
	a = 68 + 7						
	$a = 75$ $\checkmark A$ $\checkmark A$ The numbers are 75 and 68						
	OR						
	a + b = 143						
	a-b=7						
	$\therefore 2a = 150$ (adding the 2 equations)						
	a = 75	Innat					
	75 + b = 143						
	b = 68		(3)				

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4.3			S = 10	Answer: 2 marks	
	PENS		S		
	10 - 7 = 3 b	oxes 🗸 🖌 A			(2)
4.4	$d = s \times t$	M		Formula/method: 1 mark	
	a = 100 km/d = 300 km/d	$n \times 3n$	¥ A		
	a = 500 km			300 km: 1 mark	
	$S = \frac{1}{t}$			$\frac{300 \text{ km}}{2 \text{ hrs}}$: 1 mark	
Av. Speed = $\frac{300km}{2hrs}$ \checkmark M				Answer: 1 mark	
	$= 150 \ km/h$ \checkmark CA				
	OR				
	Speed	100 <i>km</i>	x km		
	Time	3 hrs	2 hrs		
	2x = 300				
	<i>x</i> = 150 <i>km</i>	n/h			(4)
					[12]



QUESTION 5 [16 marks]						
F		-	1			
Ques.	Solution	Mark Allocation	Total			
5.1.1	$\angle ACB = \angle DCF = 32^{\circ}$ (Vert. opp. $\angle s$)	Statement and	(-)			
	$\angle EBC = \angle ACB = 32^{\circ}$ (Alt. $\angle s$, EB DA)	reason: 1 mark each	(2)			
5.1.2	$\angle CAB + \angle ABE = 180^{\circ}$ (Co int. $\angle s : EB DA$) \checkmark S/R	Statement and				
	$\angle CAB = 180^\circ - 65^\circ \checkmark \mathbf{M}$	reason: 1 mark				
	$\angle CAB = 115^{\circ} \checkmark \mathbf{A}$	Substitution: 1 mark				
	OP	Answer: 1 mark				
	\mathbf{OR}					
	$2CAB + 2ACB + 2ABC = 180^{\circ} (2.5 \text{ of } a \Delta) \vee \mathbf{5/R}$					
	$2CAB = 180^{\circ} - (32^{\circ} + 33^{\circ}) [ZABC = 65^{\circ} - 32^{\circ} \text{Y} \text{M}$					
	$2CAB = 180^{\circ} - 65^{\circ}$					
	$2CAB = 115^{\circ} \checkmark \mathbf{A}$		(3)			
5.2.1	$\angle A + \angle ABC = \angle BCE$ (Ext \angle of a \triangle) \checkmark S/R	Statement and				
		reason: 1 mark				
	$(2x - 48^{\circ}) + (x + 14^{\circ}) = 116^{\circ}$ $\checkmark M$					
	$3x - 34^\circ = 116^\circ$	Substitution: 1 mark				
	$3x = 150^{\circ}$ $\checkmark \mathbf{A}$					
	$x = 50^{\circ}$	Answer: 1 mark				
	OR ✓S/R					
	$\angle A + \angle ABC + + \angle ACB = 180^{\circ} \ (\angle's \text{ of a } \Delta)$					
	$(2x - 48^{\circ}) + (x + 14^{\circ}) + 64^{\circ} = 180^{\circ}$ $\checkmark M$					
	$3x + 30^{\circ} = 180^{\circ}$					
	$3x = 150^{\circ}$					
	$x = 50^{\circ}$ $\checkmark A$					
			(3)			
5.2.2	$\angle A = 2x - 48^{\circ}$	Substitution: 1 mark				
	$= 2(50^{\circ}) - 48^{\circ}$ $\checkmark M$					
	$-100^{\circ} - 48^{\circ}$	Answer: 1 mark				
	- 529					
500	$= 52^{\circ} \checkmark \mathbf{A}$		(2)			
5.2.3	$\angle ABC = 50^\circ + 14^\circ = 64^\circ$	Correct statement:				
	$\angle ACB = 180^{\circ} - 116^{\circ} = 64^{\circ}$	1 mark				
	√S √R					
	$\triangle ABC$ is an isosceles triangle ($\angle ABC = \angle ACB$)	Correct Reason:				
	• • • •	1 mark	(2)			
5.3.1	√S √R	Correct statement:				
	$\angle ABC = 40^{\circ}$ (Complementary $\angle's$)	1 mark				
		Correct Reason:				
		1 mark				
			(2)			
5.3.2	√S √R	Correct statement:				
	$\angle AD\bar{O} = 32^{\circ} (AO = OD / radii)$	1 mark				
		Correct Reason:				
		1 mark	(2)			
			[16]			

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QUESTION 6 [11 marks]						
Ques	Solution	Mark Allocation		Total		
6.1	STATEMENT	REASON	Correct	Total		
	KL = KN	Given √A	statement			
	LM = NM	Given √ ∆	with			
	KM = KM	Common 🗸 A	reason: 1			
	$\therefore \Delta KLM \equiv \Delta KNM.$	SSS√A	mark each	(4)		
				(4)		
6.2.1	STATEMENT	REASON	Correct			
	$\hat{A} = \hat{P}$	Alt.∠'s, AB∥PQ √A	statement			
	$\hat{B} = \hat{O}$	Alt.∠'s, AB∥PQ √A	with			
	$A\hat{O}B = P\hat{O}O$	Vert. opp. ∠'s ✓ A	reason: 1			
		$AAA \checkmark \Delta$	mark each	(4)		
6.2.2	OQ = OP (Corr. sides are proportional),	Statement and rea	son: 1 mark	(4)		
	$\frac{1}{OB} = \frac{1}{AO}$ \checkmark S/R					
	x 12 cm	$\frac{x}{5 cm} = \frac{1}{4}$	$\frac{2 cm}{cm}$: 1 mark			
	$\frac{\pi}{5 cm} = \frac{12 cm}{6 cm} \qquad \checkmark \mathbf{A}$	5011	, cm			
		Ans	swer: 1 mark			
	$x = 0Q = 10 \ cm$ \checkmark CA			(3)		
				[11]		
QUEST	ION 7 [8 marks]					
Ques.	Solution	Mark Allocat	ion	Total		
7.1		14 <i>cm</i> : 1 mark				
	$d = 7 \times 2 = 14cm \checkmark \mathbf{M}$	$s^2 - \frac{\pi r^2}{2}$: 1 mark				
	πr^2	$196 \ cm^2 - 77 \ cm^2$: 1 mark				
	Area of the shaded part = $s^2 - \frac{\pi r^2}{2}$ Answer: 1 mark		swer: 1 mark			
	$= 14 \times 14 - \frac{\frac{22}{7} \times 49}{7}$	$\frac{\frac{22}{7} \times 49}{2}$				
	$-196 \text{ cm}^2 - 77 \text{ cm}^2 \checkmark \Delta$					
	$= 119 cm^2 \checkmark C \Delta$			(4)		
7.2	$2l + 2b = 16$ $\checkmark M$	2l + 2b = 16:1 mark				
	l+b=8					
	b = 8 - l	$l \times b =$	15:1 mark			
	$l \times b = 15 \checkmark M$		5.1 Mark			
	l(8-l) = 15 $8l - l^2 - 15$		3 : 1 mark			
	$l^2 - 8l - 15 = 0$					
	(l-5)(l-3) = 0					
	$l = 5 \text{ or } l = 3 \checkmark \mathbf{A}$					
	$b = 3 \text{ or } b = 5 \checkmark \mathbf{A}$			(4)		
				[8]		

