## SENIOR PHASE

## GRADE 9

## NOVEMBER 2016

## MATHEMATICS

MARKS: 100

TIME: 2 hours


This question paper consists of 13 pages including an information sheet.

## INSTRUCTIONS AND INFORMATION

1. Read the following instructions carefully.
2. Answer ALL the questions.
3. Write neatly and legibly.
4. Number your answers exactly as questions are numbered.
5. Give reasons for each statement in QUESTION 5 and QUESTION 6.
6. Show ALL working.
7. You may use an approved scientific calculator (non-programmable and non-graphical).
8. Diagrams are NOT necessarily drawn to scale.
9. Use attached ANNEXTURE A to answer QUESTION 3.3.

## QUESTION 1

In this question, write only the correct letter next to the corresponding number, e.g. If the correct answer for question 1.1 is D , write 1.1 D only.
1.1 What is the correct pair of values of $x$ in $(x-3)(x+2)=0$ ?

A $\quad x=-3$ and $x=-2$
B $\quad x=3$ and $x=-2$
C $\quad x=-3$ and $x=2$
D $\quad x=3$ and $x=2$
1.2 What is the HCF of 210 and 350 ?

A $\quad 2 \times 5 \times 5 \times 7$
B $\quad 2 \times 3 \times 5 \times 7$
C $\quad 2 \times 5 \times 7$
D $\quad 5 \times 7$
1.3 Calculate: $6+6 \div 2-6 \times(-2)$

A 21
B 18
C 12
D 0
1.4 Determine the next term in the pattern $2 ; 5 ; 9 ; 14 ; \ldots$ ?

A 21
B 20
C 19
D $\quad 18$
1.5 Which of the following statements is true about a kite?

A The longer diagonal bisects the shorter diagonal at $90^{\circ}$.
B The shorter diagonal bisects the longer diagonal at $90^{\circ}$.
C Diagonals bisect each other.
D Diagonals are equal.
1.6 What will be the volume of a rectangular prism if all its dimensions are doubled?

A $2 \times$ the volume of the original prism.
B $4 \times$ the volume of the original prism.
C $6 \times$ the volume of the original prism.
D $8 \times$ the volume of the original prism.
1.7 Which of the following statements has the same effect as rotating an object about the line $y=x$ ?

A Rotating the object $270^{\circ}$ anti-clockwise.
B Rotating the object $90^{\circ}$ anti-clockwise.
C Rotating the object $180^{\circ}$ clockwise.
D Rotating the object $90^{\circ}$ clockwise.
1.8 What will be the total surface area of a cube with a volume of $64 \mathrm{~cm}^{3}$ ?

A $96 \mathrm{~cm}^{2}$
B $\quad 64 \mathrm{~cm}^{2}$
C $\quad 16 \mathrm{~cm}^{2}$
D $\quad 4 \mathrm{~cm}^{2}$

1.9 What is the length of $A D$ in the figure below?


A 16 cm
B 15 cm
C $\quad 13 \mathrm{~cm}$
D 5 cm
1.10 What is the mode of the scores presented in the frequency distribution table below?

| Score | Frequency |
| :---: | :---: |
| 111 | 2 |
| 112,1 | 7 |
| 114,3 | 6 |
| 115 | 2 |
| 211 | 1 |

A 118,5
B 113,6
C 112,1
D 100


## QUESTION 2

2.1 Write 0,000 000674 in scientific notation.
2.2 Simplify:
2.1.1 $\sqrt[3]{x^{3}}+x^{0}$
$2.1 .2 \sqrt{0,03 x^{8}+0,01 x^{8}}$
2.2.2 $\frac{\left(2 d^{2} e\right)^{2}}{\left(4 d^{-3} e^{-2}\right)^{-1}}$
2.2.4 $2(x+2)^{2}-2(x+1)(x+2)$
2.3 Factorise completely:
2.3.1 $x^{2}+5 x-24$
2.3.2 $2(a-b)-b+a$
2.4 Solve for $x$ :
2.4.1 $4 x-10=6$
2.4.2 $\frac{3 x-10}{2}=\frac{2 x-5}{3}$
2.4.3 $\quad x^{2}=4$
2.4.4 $3 x^{5}=96$


## QUESTION 3

3.1 Study the geometric pattern below and answer the questions that follow.


| Figure | 1 | 2 | 3 |
| :--- | :---: | :---: | :---: |
| Number of lines | 6 | 11 |  |

3.1.1 Complete the table.
3.1.2 Write down the general rule for the pattern in the form $T_{n}=$.
3.2 Study the straight line graphs below and answer the questions that follow.

3.2.1 Write down the equation of $A B$.
3.2.2 Write down the equation of $A D$.
3.3 On the attached grid, draw a graph defined by $y=-2 x+1$. Remove the ANNEXURE and attach it in your ANSWER BOOK.

## QUESTION 4

4.1 How long will it take an investment of R5 000 at $12 \%$ per annum simple interest to earn R1 800 interest?
4.2 The sum of two numbers is 143 and their difference is 7 , what are the numbers?
4.3 There are 10 boxes, five contain pencils, four contain pens and two contain pens and pencils. How many boxes contain no pens and pencils?
4.4 A car travelling at an average speed of $100 \mathrm{~km} / \mathrm{h}$ covers a certain distance in 3 hours. At what average speed must the car travel to cover the same distance in 2 hours?

## QUESTION 5

5.1 In the diagram below $A \hat{B} E=65^{\circ}$ and $D \hat{C} F=32^{\circ}$.

5.1.1 Calculate the size of $E \hat{B} C$. Give reasons for your answer.
5.1.2 Calculate the size of $\widehat{A B}$. Give reasons for your answer.

5.2 In the diagram below, $\widehat{C A B}=2 x-48^{\circ}, A \hat{B} C=x+14^{\circ}$ and $B \hat{C} E=116^{\circ}$.

5.2.1 Calculate the value of $x$. Give reasons for your answer.
5.2.2 Calculate the actual size of $\widehat{C A} B$.
5.2.3 What type of $\triangle$ is $\triangle A B C$ ? Give reasons for your answer.
5.3 In the figure below, O is the centre of the circle.

5.3.1 Calculate the size of $C \hat{A} B$. Give a reason for your answer.
5.3.2 Calculate the size of $A \widehat{D} O$. Give a reason for your answer.

## QUESTION 6

6.1 In the diagram below, prove that $\triangle K L M \equiv \triangle K N M$.

6.2 In the diagram below, AB || PQ .

6.2.1 Prove that $\triangle \mathrm{ABO}\|\| \mathrm{PQO}$.
6.2.2 Calculate the value of $x$.


## QUESTION 7

7.1 In the figure below $A B C D$ is a square and $A O D$ is the diameter of the circle.

Calculate the area of the shaded part if $r=7 \mathrm{~cm}$. N.B $\pi=\frac{22}{7}$

7.2 A rectangular carpet has a perimeter of 16 m and an area of $15 \mathrm{~m}^{2}$. What are the dimensions of the sides of the carpet?


## QUESTION 8

8.1 A spinner with 5 colours, red, yellow, green, black and white is spun and a coin is tossed, at the same time.
8.1.1 Draw a tree diagram to illustrate the number of possible outcomes for the experiment.
8.1.2 What is the probability of spinning any colour and tossing a head?
8.1.3 What is the probability of spinning a red colour?
8.2 The pie chart below shows different modes of transport used by learners of Boiteko Junior Secondary School when travelling to school. The total number of learners in the school is 600 . Study the graph and answer the questions that follow.

8.2.1 What fraction of learners walk to school? Give your answer as a fraction.
8.2.2 Express the number of learners who travel by bus as a percentage.
8.2.3 What is the ratio of learners who walk to school to those who use their own transport?

ANNEXURE A
NAME: $\qquad$
SURNAME: $\qquad$



Although great care is taken with the setting and quality assurance of question paper, unfortunately due to various factors, errors due creep in. In order to ensure that learners are not disadvantaged in any way, it is requested that the following must be brought to the attention of learners before they start to write.

## ERRATA FOR GRADE 9 MATHS PAPER BEFORE WRITING COMMENCES

QUESTION PAPER

| ITEM <br> NO. | INCORRECT STATEMENT | CORRECT STATEMENT/SUGGESTIONS |  |
| :--- | :--- | :--- | :---: |
| 1.7 | Which of the following statements has <br> the same effect as rotating an object <br> about the line $y=x ?$ | Which of the following statements has the same <br> effect as rotating an object 270 <br> origin? |  |
|  |  |  |  |
| 2.2 | Numbering is incorrect. | The correct numbering is: about the |  |
|  |  |  |  |
|  | 2.1 .1 | 2.2 .1 |  |
|  | 2.1 .2 | 2.2 .2 |  |
|  | 2.2 .2 | 2.2 .3 |  |




We want to apologise for any inconvenience caused and please note that the errata was issued to ensure that learners are assessed in the most accurate and fair manner.

Yours in education.

Uet
MS N. MBELEKI
CES: INSTRUMENT DEVELOPMENT SECTION

THIS MUST BE ISSUED ONLY TO MARKERS OF THE PAPER AFTER THE PAPER HAS BEEN WRITTEN.

MEMORANDUM


We want to apologise for any inconvenience caused and please note that the errata was issued to ensure that learners are assessed in the most accurate and fair manner.

Yours in education.


MS N. MBELEKI
CES: INSTRUMENT DEVELOPMENT SECTION

21 November 2016
DATE


## GRADE 9

## NOVEMBER 2016

## MATHEMATICS MEMORANDUM

MARKS: 100

This memorandum consists of 9 pages.

## NOTE:

- This is marking guideline. In instances where learners have used different mathematically sound strategies to solve the problems, they should be credited.
- Underline errors committed by learners and apply Consistent Accuracy (CA) marking.

| KEY |  |
| :--- | :--- |
| $M$ | Method mark |
| CA | Consistent Accuracy mark |
| A | Accuracy mark |
| S | Statement |
| R | Reason |
| S/R | Statement and Reason |


| QUESTION 1 [10 marks] |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Ques. |  |  | Mark Allocation | Total |
| 1.1 | B | $\checkmark$ | 1 mark for each correct answer | (1) |
| 1.2 | C | $\checkmark$ |  | (1) |
| 1.3 | A | $\checkmark$ |  | (1) |
| 1.4 | B | $\checkmark$ |  | (1) |
| 1.5 | A | $\checkmark$ |  | (1) |
| 1.6 | D | $\checkmark$ |  | (1) |
| 1.7 | C | $\checkmark$ |  | (1) |
| 1.8 | A | $\checkmark$ |  | (1) |
| 1.9 | C | $\checkmark$ |  | (1) |
| 1.10 | C | $\checkmark$ |  | (1) |
|  |  |  |  | [10] |


| QUESTION 2 [26 marks] |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| Ques. | Solution | Mark Allocation | Total |
| 2.1 | $6,74 \times 10^{-7} \checkmark \mathbf{A}$ | Answer: 1 mark | (1) |
| 2.2.1 | $\begin{aligned} & \sqrt[3]{x^{3}}+x^{0} \\ & \checkmark \mathbf{A} \checkmark \mathbf{A} \\ & x+1 \end{aligned}$ | $\begin{aligned} x & : 1 \text { mark } \\ +1 & : 1 \text { mark } \end{aligned}$ | (2) |
| 2.2.2 | $\begin{aligned} & \sqrt{0,03 x^{8}+0,01 x^{8}} \\ & \sqrt{0,04 x^{8}} \quad \checkmark \mathbf{A} \\ & 0,2 x^{4} \quad \checkmark \mathbf{A} \end{aligned}$ | $\sqrt{0,04 x^{8}}: 1$ mark Answer: 1 mark | (2) |
| 2.2.3 | $\begin{aligned} & \frac{\left(2 d^{2} e\right)^{2}}{\left(4 d^{-3} e^{-2}\right)^{-1}} \\ & \checkmark \checkmark \mathbf{M} \quad \checkmark \mathbf{M} \\ & 2^{2} d^{4} e^{2} \times 2^{2} d^{-3} e^{-2} \\ & 16 d \quad \checkmark \mathbf{A} \end{aligned}$ | $2^{2} d^{4} e^{2}: 1$ mark $2^{2} d^{-3} e^{-2}: 1$ mark Answer: 1 mark | (3) |
| 2.2.4 | $\begin{aligned} & 2(x+2)^{2}-2(x+1)(x+2) \\ & 2\left(x^{2^{\vee}+4} \mathbf{M} x+4\right)-2\left(x^{2}+3 x+2\right) \\ & 2 x^{2}+8 x+8-2 x^{2}-6 x-4 \\ & 2 x+4 \quad \checkmark \mathbf{C A} \end{aligned}$ | $\begin{array}{r} x^{2}+4 x+4: 1 \text { mark } \\ x^{2}+3 x+2: 1 \text { mark } \\ 2 x^{2}+8 x+8-2 x^{2}-6 x-4 \\ : 1 \text { mark } \\ \text { Answer: } 1 \text { mark } \end{array}$ | (4) |
| 2.3.1 | $\begin{gathered} x^{2}+5 x-24 \\ \checkmark \mathbf{A} \quad \checkmark \mathbf{A} \\ (x+8)(x-3) \end{gathered}$ | $\begin{aligned} & x+8: 1 \text { mark } \\ & x-3: 1 \text { mark } \end{aligned}$ | (2) |
| 2.3.2 | $\begin{aligned} & 2(a-b)-b+a \\ & 2(a-b)+1(a-b) \quad \checkmark \mathbf{M} \\ & (2+1)(a-b) \quad \checkmark \mathbf{M} \\ & 3(a-b) \quad \checkmark \mathbf{A} \end{aligned}$ | $\begin{array}{r} +1(a-b: 1 \text { mark } \\ (2+1)(a-b): 1 \text { mark } \\ \text { Answer : } 1 \text { mark } \end{array}$ | (3) |
| 2.4.1 | $\begin{aligned} & 4 x-10=6 \\ & 4 x=16 \quad \checkmark \mathbf{M} \\ & x=4 \quad \checkmark \mathbf{A} \end{aligned}$ | $4 x=16: 1$ mark <br> Answer: 1 mark $\square$ | (2) |
| 2.4.2 | $\begin{aligned} & \frac{3 x-10}{2}=\frac{2 x-5}{3} \\ & 6 \times\left(\frac{3 x-10}{2}\right)=6 \times\left(\frac{2 x-5}{3}\right) \quad \checkmark \mathrm{M} \\ & 9 x-30=4 x-10 \quad \checkmark \mathrm{~A} \\ & 5 x=20 \\ & x=4 \quad \vee \mathrm{CA} \end{aligned}$ | $9 x-30 \begin{array}{\|c\|c\|} \hline \times \text { LCD: } 6: 1 \text { mark } \\ =4 x-10: 1 \text { mark } \\ & \text { Answer: } 1 \text { mark } \end{array}$ | (3) |



| Question 4 [12 marks] |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| Ques. | Solution | Mark Allocation | Total |
| 4.1 | $\begin{aligned} & \text { p. n. i=SI } \quad \checkmark \mathbf{M} \\ & 5000 \times n \times 0,12=1800 \\ & n=3 \quad \checkmark \mathbf{A} \\ & \text { OR } \\ & A=P(1+n i) \quad \checkmark \mathbf{M} \\ & 6800=5000(1+0,12 n) \quad \checkmark \mathbf{M} \\ & 1.36=1+0,12 n \\ & 0,36=0,12 n \\ & n=3 \quad \checkmark \mathbf{A} \end{aligned}$ | Formula: 1 mark Substitution: 1 mark Answer: 1 mark | (3) |
| 4.2 | Let the numbers be $a$ and $b$ $\begin{aligned} & a+b=143 \\ & a-b=7 \\ & a=b+7 \\ & b+7+b=143 \\ & 2 b=136 \\ & b=68 \\ & a=68+7 \end{aligned}$ $a=75 \quad \quad \checkmark \mathbf{A} \quad \checkmark \mathbf{A}$ <br> The numbers are 75 and 68 <br> OR $\begin{aligned} & a+b=143 \\ & a-b=7 \\ & \therefore 2 a=150 \text { (adding the } 2 \text { equations) } \\ & \quad a=75 \\ & 75+b=143 \\ & \quad b=68 \end{aligned}$ | Any method: 1 mark <br> 75: 1 mark <br> 68: 1 mark |  |



| QUESTION 5 [16 marks] |  |  |  |
| :---: | :---: | :---: | :---: |
| S |  |  |  |
| Ques. | Solution | Mark Allocation | Total |
| $5.1 .1$ | $\begin{aligned} & \angle A C B=\angle D C F=32^{\circ}\left(\text { Vert. opp. } \angle^{\prime} s\right) \\ & \angle E B C=\angle A C B=32^{\circ}\left(\text { Alt. } \angle^{\prime} s, E B \\| D A\right) \end{aligned}$ | Statement and reason: 1 mark each | (2) |
| 5.1.2 | $\begin{aligned} & \angle C A B+\angle A B E=180^{\circ}\left(\text { Co int. } \angle^{\prime} s: E B \\| D A\right) \checkmark \mathbf{S} / \mathbf{R} \\ & \angle C A B=180^{\circ}-65^{\circ} \quad \checkmark \mathbf{M} \\ & \angle C A B=115^{\circ} \checkmark \mathbf{A} \end{aligned}$ <br> OR $\begin{aligned} & \angle C A B+\angle A C B+\angle A B C=180^{\circ}\left(\angle^{\prime} s \text { of a } \Delta\right) \checkmark \mathbf{S} / \mathbf{R} \\ & \angle C A B=180^{\circ}-\left(32^{\circ}+33^{\circ}\right)\left[\angle A B C=65^{\circ}-32^{\circ} \curlyvee \mathbf{M}\right. \\ & \angle C A B=180^{\circ}-65^{\circ} \\ & \angle C A B=115^{\circ} \quad \checkmark \mathbf{A} \end{aligned}$ | Statement and reason: 1 mark Substitution: 1 mark Answer: 1 mark | (3) |
| 5.2.1 | $\begin{aligned} & \angle A+\angle A B C=\angle B C E(\text { Ext } \angle \text { of a } \triangle) \quad \checkmark \mathbf{S} / \mathbf{R} \\ & \left(2 x-48^{\circ}\right)+\left(x+14^{\circ}\right)=116^{\circ} \quad \checkmark \mathbf{M} \\ & 3 x-34^{\circ}=116^{\circ} \\ & 3 x=150^{\circ} \\ & x=50^{\circ} \end{aligned}$ $\begin{aligned} & \text { OR } \quad \begin{array}{l} \quad \checkmark \mathbf{S} / \mathbf{R} \\ \angle A+\angle A B C++\angle A C B=180^{\circ} \quad(\angle ' s \text { of a } \triangle) \\ \left(2 x-48^{\circ}\right)+\left(x+14^{\circ}\right)+64^{\circ}=180^{\circ} \quad \checkmark \mathbf{M} \\ 3 x+30^{\circ}=180^{\circ} \\ 3 x=150^{\circ} \\ x=50^{\circ} \end{array} \quad \checkmark \mathbf{A} \end{aligned}$ | Statement and reason: 1 mark <br> Substitution: 1 mark <br> Answer: 1 mark |  |
|  |  |  | (3) |
| 5.2.2 | $\begin{aligned} & \angle A=2 x-48^{\circ} \\ & =2\left(50^{\circ}\right)-48^{\circ} \quad \checkmark \mathbf{M} \\ & =100^{\circ}-48^{\circ} \\ & =52^{\circ} \quad \checkmark \mathbf{A} \end{aligned}$ | Substitution: 1 mark <br> Answer: 1 mark | (2) |
| 5.2.3 | $\begin{gathered} \angle A B C=50^{\circ}+14^{\circ}=64^{\circ} \\ \angle A C B=180^{\circ}-116^{\circ}=64^{\circ} \\ \checkmark \mathbf{S} \end{gathered}$ <br> $\triangle A B C$ is an isosceles triangle $(\angle A B C=\angle A C B)$ | Correct statement: $\square$ 1 mark <br> Correct Reason: <br> 1 mark | (2) |
| 5.3.1 | $\stackrel{\checkmark \mathbf{S}}{\angle A B C}=40^{\circ}\left(\text { Complementary } \angle^{\prime} s\right)$ | Correct statement: <br> 1 mark Correct Reason: <br> 1 mark | (2) |
| 5.3.2 | $\angle A D O=32^{\circ}\left(\mathrm{AO}=\stackrel{\sqrt{ } \mathbf{R}}{O^{\prime}} /\right. \text { radii) }$ | Correct statement: <br> 1 mark Correct Reason: <br> 1 mark | (2) |
|  |  |  | [16] |

QUESTION 6 [11 marks]

| Ques. | Solution | Mark Allocation | Total |
| :---: | :---: | :---: | :---: |
| 6.1 | STATEMENT | REASON | (4) |
|  | $K L=K N$ | Given $\mathbf{\checkmark A}$ statement |  |
|  | $L M=N M$ | Given $\checkmark \mathbf{A}$ with |  |
|  | $K M=K M$ | Common $\checkmark$ A reason: 1 |  |
|  | $\therefore \Delta \mathrm{KLM} \equiv \Delta \mathrm{KNM}$. | $\operatorname{SSS} \mathbf{A}$ mark each |  |
| 6.2.1 | STATEMENT | REASON Correct | (4) |
|  | $\hat{A}=\hat{P}$ | Alt . $\angle$ 's, $\mathrm{AB} \\| \mathrm{PQ} \checkmark$ ' statement |  |
|  | $\hat{B}=\hat{Q}$ | Alt.$\angle$ 's, $A B \\| P Q \quad \checkmark A$ with |  |
|  | $A \widehat{O} B=P \hat{O} Q$ | Vert. opp. $\angle$ 's $\checkmark$ A ${ }^{\text {a }}$ l ${ }^{\text {reason: } 1}$ |  |
|  | $\therefore \triangle \mathrm{ABO} \\|\| \| \triangle \mathrm{PQO}$. | $A A A \quad \checkmark \mathbf{A}$ |  |
| 6.2 .2 | $\begin{aligned} & \frac{O Q}{O B}=\frac{O P}{A O}(\text { Corr. sides are proportional) } \mathbf{S} / \mathbf{R} \\ & \frac{x}{5 \mathrm{~cm}}=\frac{12 \mathrm{~cm}}{6 \mathrm{~cm}} \quad \checkmark \mathbf{A} \\ & x=O Q=10 \mathrm{~cm} \\ & \quad \checkmark \mathbf{C A} \end{aligned}$ | Statement and reason: 1 mark $\frac{x}{5 \mathrm{~cm}}=\frac{12 \mathrm{~cm}}{6 \mathrm{~cm}}: 1 \text { mark }$ <br> Answer: 1 mark | (3) |
|  |  |  | [11] |
|  |  |  |  |
| QUESTION 7 [8 marks] |  |  |  |
| Ques. | Solution |  | Total |
| 7.1 | $d=7 \times 2=14 \mathrm{~cm} \quad \checkmark \mathbf{M}$ $\begin{aligned} & \text { Area of the shaded part }=s^{2}-\frac{\pi r^{2}}{2} \\ & \qquad \begin{aligned} & =14 \times 14-\frac{\frac{22}{7} \times 49}{2} \\ & =196 \mathrm{~cm}^{2}-77 \mathrm{~cm}^{2} \quad \checkmark \mathbf{A} \\ & =119 \mathrm{~cm}^{2} \checkmark \mathbf{C A} \end{aligned} \end{aligned}$ | $14 \mathrm{~cm}: 1$ mark $s^{2}-\frac{\pi r^{2}}{2}: 1$ mark $196 \mathrm{~cm}^{2}-77 \mathrm{~cm}^{2}: 1$ mark <br> Answer: 1 mark |  <br>  <br>  <br>  <br> (4) |
| 7.2 | $\begin{aligned} & 2 l+2 b=16 \\ & l+b=8 \\ & b=8-l \\ & l \times b=15 \quad \checkmark \mathbf{M} \\ & l(8-l)=15 \\ & 8 l-l^{2}=15 \\ & l^{2}-8 l-15=0 \\ & (l-5)(l-3)=0 \\ & l=5 \text { or } l=3 \quad \text { 又A } \\ & b=3 \text { or } b=5 \quad \checkmark \mathbf{A} \end{aligned}$ | $\begin{aligned} & 2 l+2 b=16: 1 \text { mark } \\ & l \times b= \\ & 15: 1 \text { mark } \\ & 5: 1 \text { mark } \\ & 3: 1 \text { mark } \end{aligned}$ | (4) |
|  |  |  | [8] |



