



# basic education

Department:  
Basic Education  
**REPUBLIC OF SOUTH AFRICA**

## SENIOR CERTIFICATE EXAMINATIONS/ NATIONAL SENIOR CERTIFICATE EXAMINATIONS

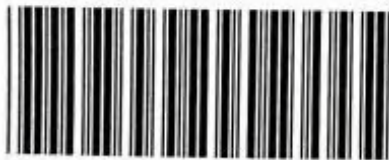
**MATHEMATICS P2**

**MAY/JUNE 2024**

Stanmorephysics.com

**MARKS: 150**

**TIME: 3 hours**



EMATHP2

**This question paper consists of 12 pages, 1 information sheet  
and an answer book of 23 pages.**

## INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

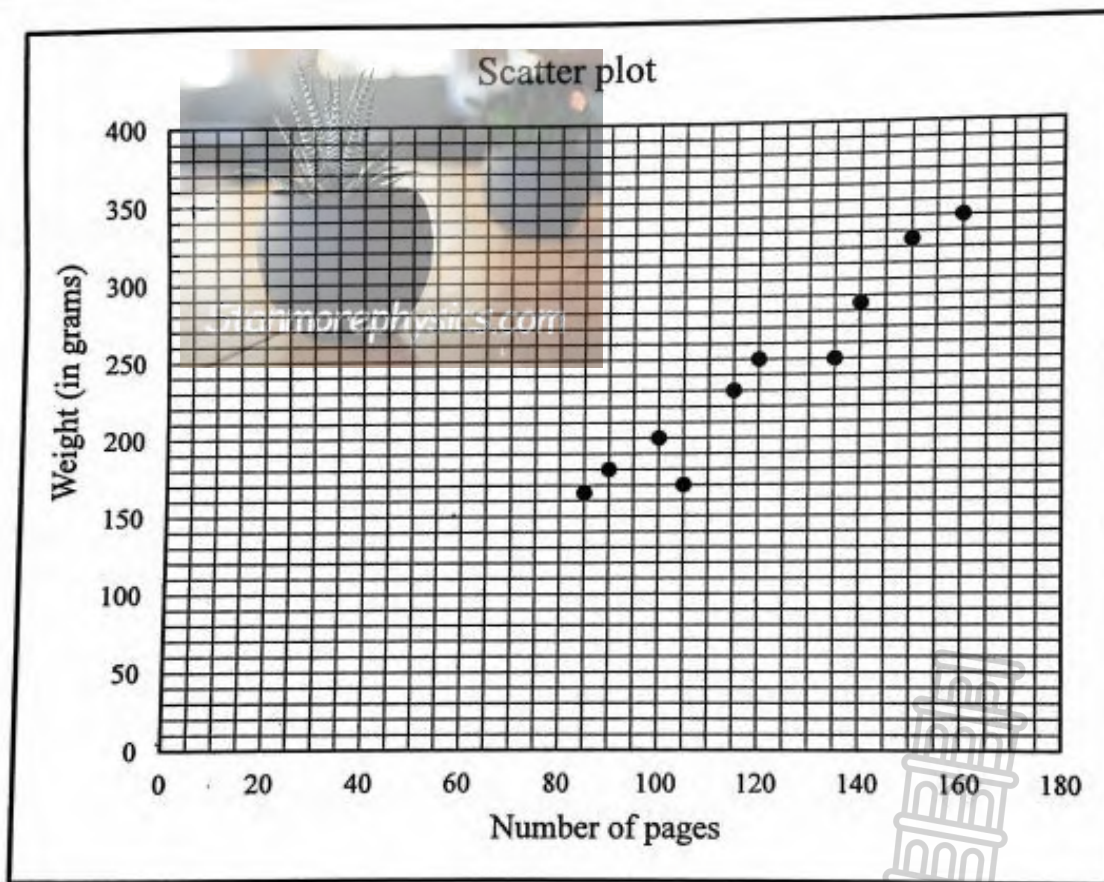
1. This question paper consists of 10 questions.
2. Answer ALL the questions in the SPECIAL ANSWER BOOK provided.
3. Clearly show ALL calculations, diagrams, graphs, etc. which you have used in determining your answers.
4. Answers only will NOT necessarily be awarded full marks.
5. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
6. If necessary, round off answers correct to TWO decimal places, unless stated otherwise.
7. Diagrams are NOT necessarily drawn to scale.
8. An information sheet with formulae is included at the end of the question paper.
9. Write neatly and legibly.



**QUESTION 1**

The number of pages in ten A4 books and their corresponding weights (in grams) are given in the table below. The data is also represented in the scatter plot.

<b>Number of pages (x)</b>	85	150	100	120	90	140	135	105	115	160
<b>Weight (in grams) (y)</b>	165	325	200	250	180	285	250	170	230	340



- 1.1 Determine the equation of the least squares regression line. (3)
- 1.2 Draw the least squares regression line on the scatter plot in the ANSWER BOOK. (2)
- 1.3 Predict the weight of an A4 book that has 110 pages. (2)
- 1.4 Calculate the percentage weight increase between a book with 110 pages and a book with 130 pages. (3)

**QUESTION 2**

Fifty athletes need to access suitable training facilities. The table below shows the distances, in km, that they need to travel to obtain access to suitable training facilities.

DISTANCE ( $x$ km)	NUMBER OF ATHLETES
$0 \leq x < 5$	3
$5 \leq x < 10$	7
$10 \leq x < 15$	20
$15 \leq x < 20$	12
$20 \leq x < 25$	5
$25 \leq x < 30$	3

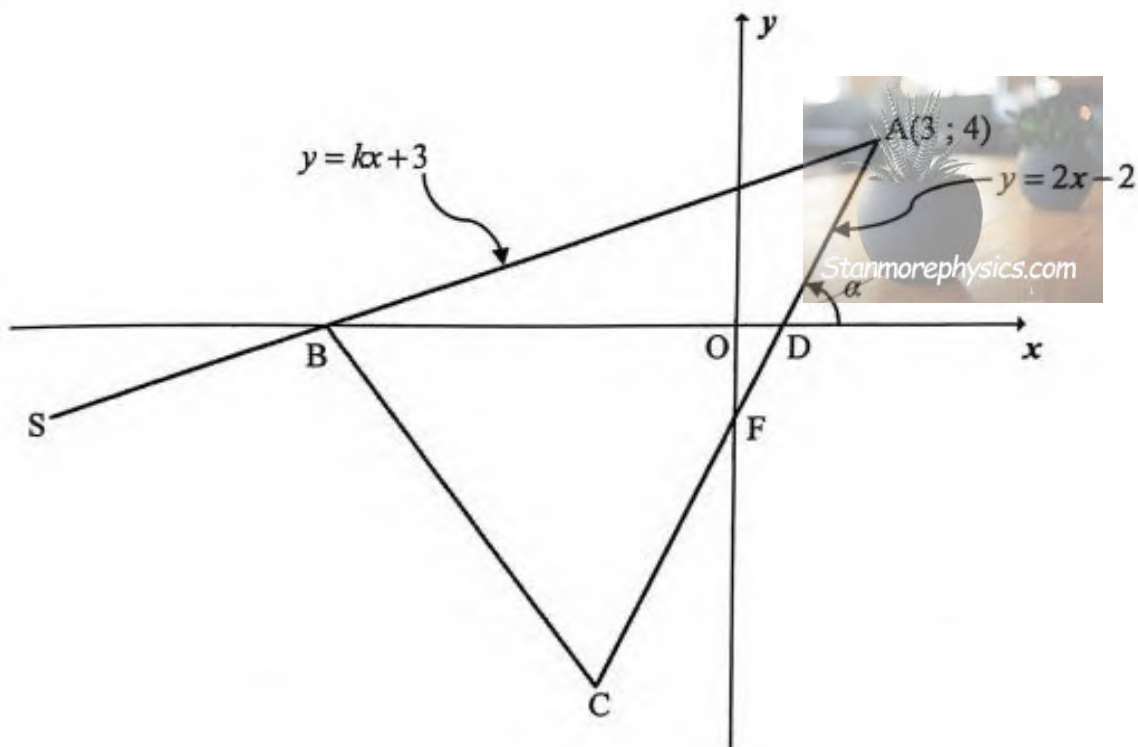
- 2.1 Complete the cumulative frequency column provided in the table in the ANSWER BOOK. (2)
- 2.2 On the grid provided in the ANSWER BOOK, draw a cumulative frequency graph (ogive) to represent the above data. (3)
- 2.3 Calculate the interquartile range (IQR) of the above data. (2)
- 2.4 The families of 4 of the athletes above who stay between 15 and 20 km from a suitable training facility, decide to move 10 kilometres closer to the facility. In which interval will the number of athletes increase? (1)
- 2.5 Calculate the estimated mean distance that the fifty athletes need to travel after the 4 families have moved 10 kilometres closer to the facility. Clearly show ALL working. (3)

[11]-



**QUESTION 3**

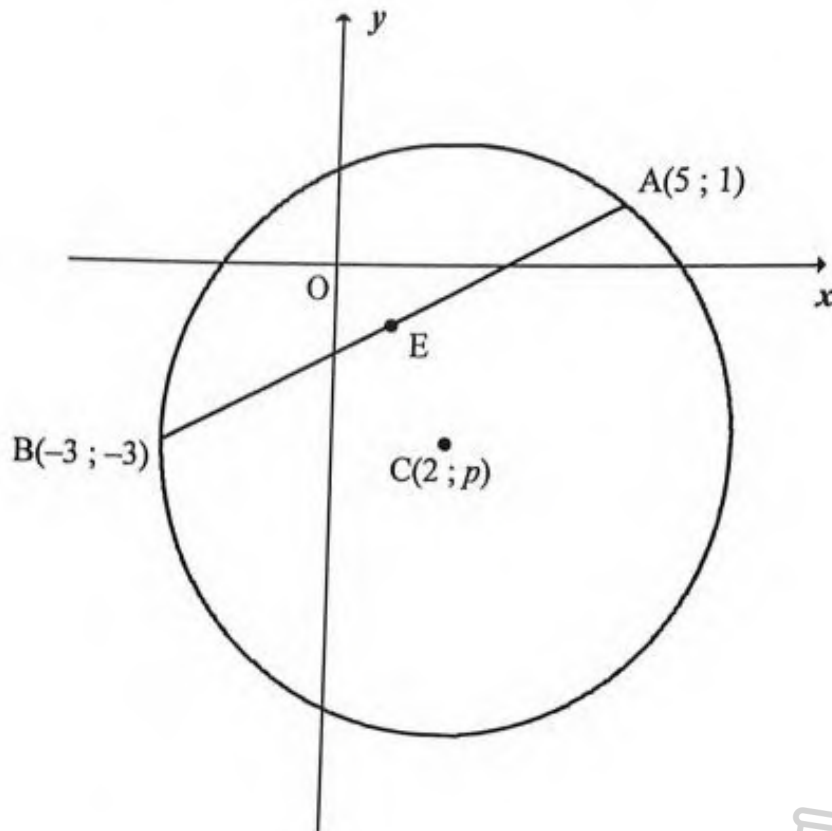
In the diagram,  $A(3; 4)$ ,  $B$  and  $C$  are vertices of  $\triangle ABC$ .  $AB$  is produced to  $S$ .  $D$  and  $F$  are the  $x$ - and  $y$ -intercepts of  $AC$  respectively.  $F$  is the midpoint of  $AC$  and the angle of inclination of  $AC$  is  $\alpha$ . The equation of  $AB$  is  $y = kx + 3$  and the equation of  $AC$  is  $y = 2x - 2$ .



- 3.1 Show that  $k = \frac{1}{3}$ . (1)
- 3.2 Calculate the coordinates of  $B$ , the  $x$ -intercept of line  $AS$ . (2)
- 3.3 Calculate the coordinates of  $C$ . (4)
- 3.4 Determine the equation of the line parallel to  $BC$  and passing through  $S(-15; -2)$ . Write your answer in the form  $y = mx + c$ . (5)
- 3.5 Calculate the size of  $\hat{BAC}$ . (5)
- 3.6 If it is further given that the length of  $AC$  is  $6\sqrt{5}$  units, calculate the value of  $\frac{\text{Area of } \triangle ABD}{\text{Area of } \triangle ASC}$ . (5)

## QUESTION 4

In the diagram, the circle centred at  $C(2; p)$  is drawn.  $A(5; 1)$  and  $B(-3; -3)$  are points on the circle.  $E$  is the midpoint of  $AB$ .



- 4.1 Calculate the coordinates of  $E$ , the midpoint of  $AB$ . (2)
- 4.2 Calculate the length of  $AB$ . Leave your answer in surd form. (1)
- 4.3 Determine the equation of the perpendicular bisector of  $AB$  in the form  $y = mx + c$ . (4)
- 4.4 Show that  $p = -3$ . (1)
- 4.5 Show, by calculation, that the equation of the circle is  $x^2 + y^2 - 4x + 6y - 12 = 0$  (4)
- 4.6 Calculate the values of  $t$  for which the straight line  $y = tx + 8$  will not intersect the circle. (6)

(6)  
[18]

## QUESTION 5

5.1 If  $\sin 40^\circ = p$ , write EACH of the following in terms of  $p$ .

5.1.1  $\sin 220^\circ$  (2)

5.1.2  $\cos^2 50^\circ$  (2)

5.1.3  $\cos(-80^\circ)$  (3)

5.2 Given:  $\tan x(1 - \cos^2 x) + \cos^2 x = \frac{(\sin x + \cos x)(1 - \sin x \cos x)}{\cos x}$

5.2.1 Prove the above identity. (5)

5.2.2 For which values of  $x$ , in the interval  $x \in [-180^\circ; 180^\circ]$ , will the identity be undefined? (3)

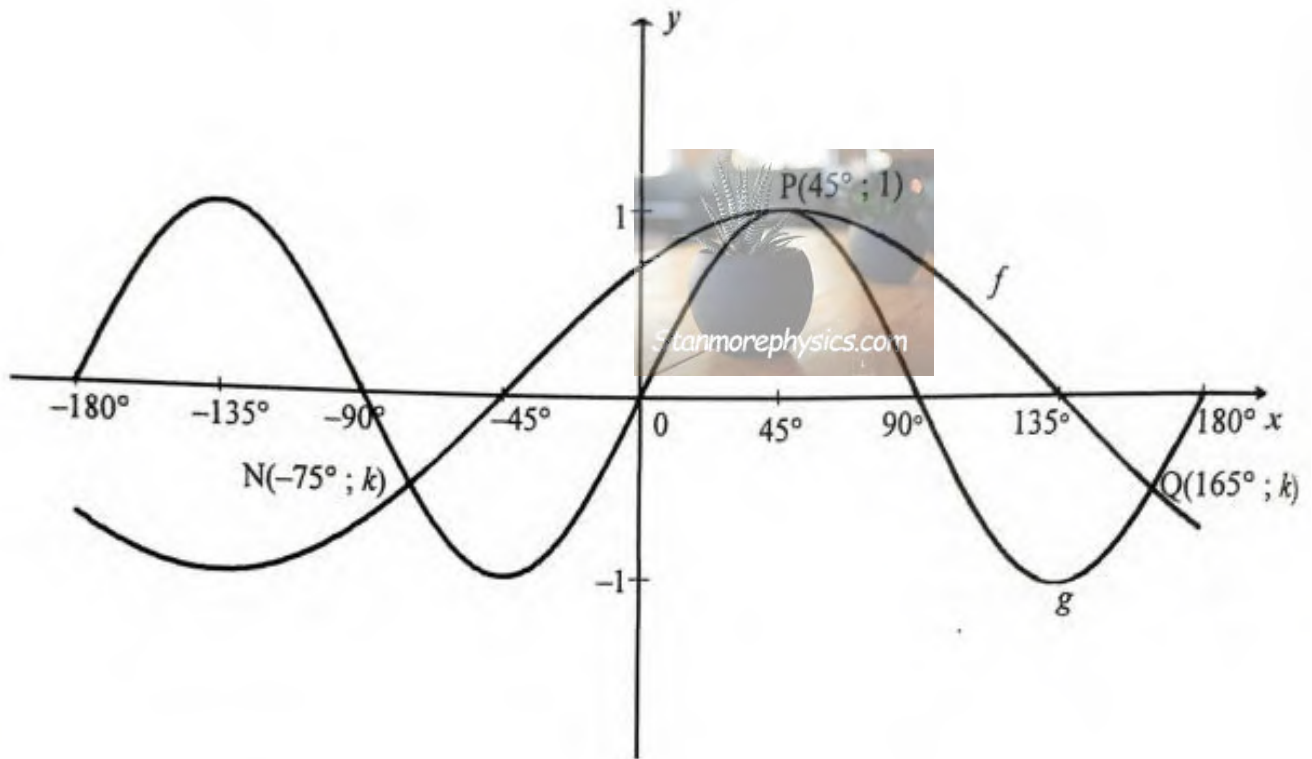
5.3 Given the expression:  $\frac{\sin 150^\circ + \cos^2 x - 1}{2}$

5.3.1 **Without using a calculator**, simplify the expression given above to a single trigonometric term in terms of  $\cos 2x$ . (6)

5.3.2 Hence, determine the general solution of  $\frac{\sin 150^\circ + \cos^2 x - 1}{2} = \frac{1}{25}$  (5)  
[26]

**QUESTION 6**

In the diagram, the graphs of  $f(x) = \cos(x + a)$  and  $g(x) = \sin 2x$  are drawn for the interval  $x \in [-180^\circ; 180^\circ]$ . The graphs intersect at  $N(-75^\circ; k)$ ,  $P(45^\circ; 1)$  and  $Q(165^\circ; k)$ .  $P$  is also a turning point of both graphs.

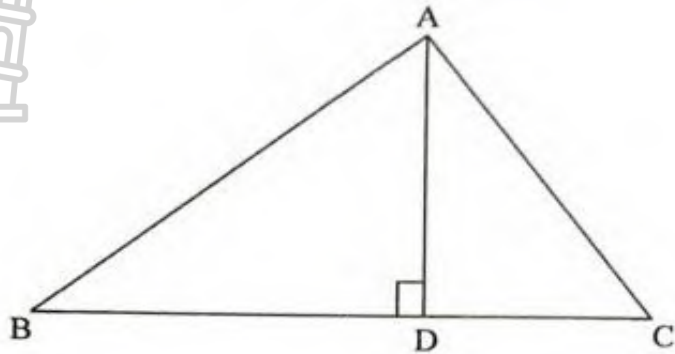


- 6.1 Write down the period of  $f$ . (1)
- 6.2 Write down the amplitude of  $g$ . (1)
- 6.3 Write down the value of  $a$ . (1)
- 6.4 Calculate the value of  $k$ , the  $y$ -coordinate of  $N$  and  $Q$ , **without the use of a calculator**. (2)
- 6.5 Calculate the value of  $x$  if  $g(x + 60^\circ) = f(x + 60^\circ)$  and  $x \in [-45^\circ; 0^\circ]$ . (1)
- 6.6 **Without using a calculator**, determine the number of solutions the equation  $\sqrt{2} \sin 2x = \sin x + \cos x$  has in the interval  $x \in [-90^\circ; 90^\circ]$ . Clearly show ALL working. (4)



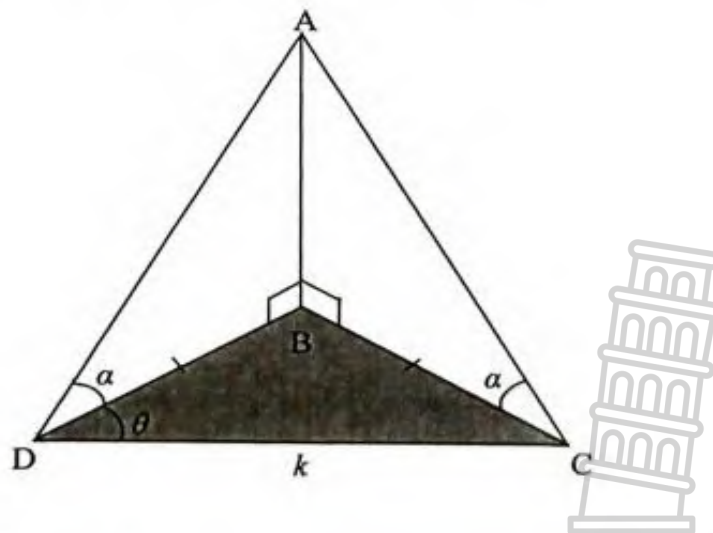
## QUESTION 7

- 7.1 In the diagram,  $\triangle ABC$  is drawn.  $AD$  is drawn such that  $AD \perp BC$ .



- 7.1.1 Use the diagram above to determine  $AD$  in terms of  $\sin \hat{B}$  (2)
- 7.1.2 Hence, prove that the area of  $\triangle ABC = \frac{1}{2}(BC)(AB)\sin \hat{B}$  (1)

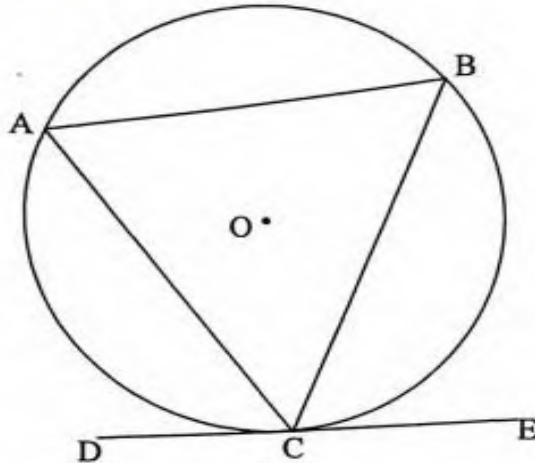
- 7.2 In the diagram, points  $B$ ,  $C$  and  $D$  lie in the same horizontal plane.  $\hat{A}DB = \hat{A}CB = \alpha$ ,  $\hat{C}DB = \theta$  and  $DC = k$  units.  $BD = BC$ .



- 7.2.1 Prove that  $AD = AC$  (2)
- 7.2.2 Prove that  $BD = \frac{k}{2 \cos \theta}$  (3)
- 7.2.3 Determine the area of  $\triangle BCD$  in terms of  $k$  and a single trigonometric ratio of  $\theta$ . (3)

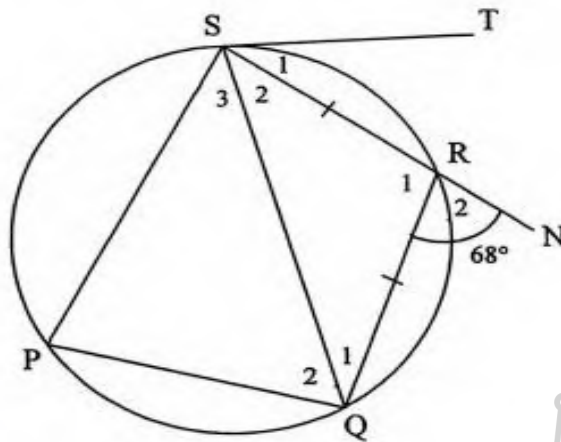
**QUESTION 8**

8.1 In the diagram, chords AB, BC and AC are drawn in the circle with centre O. DCE is a tangent to the circle at C.



Prove the theorem which states that the angle between the tangent to a circle and the chord drawn from the point of contact is equal to the angle in the alternate segment, i.e.  $\hat{BCE} = \hat{A}$ . (5)

8.2 In the diagram, PQRS is a cyclic quadrilateral with  $RQ = RS$ . ST is a tangent to the circle at S. SR is produced to N.  $\hat{R}_2 = 68^\circ$ .

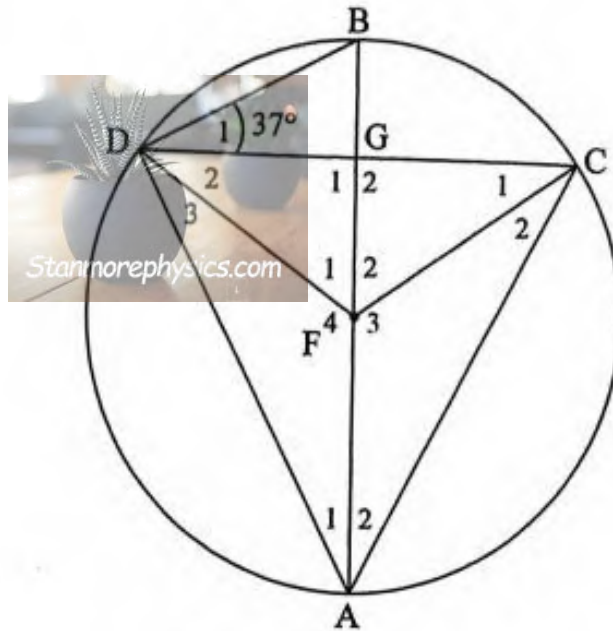


Determine, with reasons, the size of:

- 8.2.1  $\hat{P}$  (2)
  - 8.2.2  $\hat{Q}_1$  (2)
  - 8.2.3  $\hat{S}_1$  (2)
- [11]

**QUESTION 9**

In the diagram,  $AB$  is a diameter of the circle, with centre  $F$ .  $AB$  and  $CD$  intersect at  $G$ .  $FD$  and  $FC$  are drawn.  $BA$  bisects  $\hat{C}AD$  and  $\hat{D}_1 = 37^\circ$ .

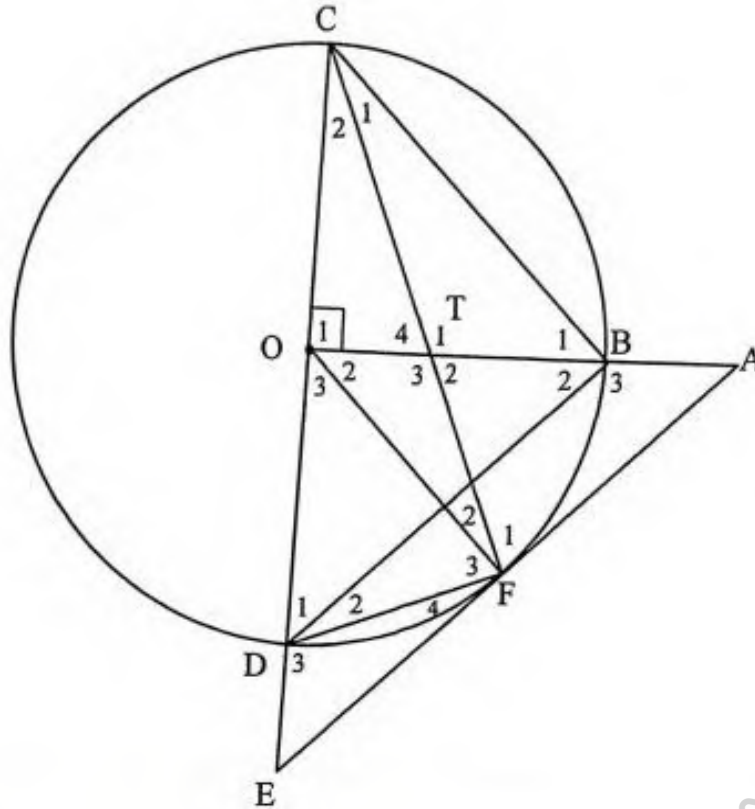


- 9.1 Determine, giving reasons, any three other angles equal to  $\hat{D}_1$ . (4)
  - 9.2 Show that  $DG = GC$ . (4)
  - 9.3 If it is further given that the radius of the circle is 20 units, calculate the length of  $BG$ . (4)
- [12]**



**QUESTION 10**

In the diagram, COD is the diameter of the circle with centre O. EA is a tangent to the circle at F. AO ⊥ CE. Diameter COD produced intersects the tangent to the circle at E. OB produced intersects the tangent to the circle at A. CF intersects OB in T. CB, BD, OF and FD are drawn.



Prove, with reasons, that:

- 10.1 TODF is a cyclic quadrilateral (4)
- 10.2  $\hat{D}_3 = \hat{T}_1$  (3)
- 10.3  $\Delta TFO \parallel \Delta DFE$  (5)
- 10.4 If  $\hat{B}_2 = \hat{E}$ , prove that  $DB \parallel EA$ . (2)
- 10.5 Prove that  $DO = \frac{TO \cdot FE}{AB}$  (5)

[19]

**TOTAL: 150**

**INFORMATION SHEET**

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni)$$

$$A = P(1 - ni)$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$T_n = a + (n - 1)d$$

$$S_n = \frac{n}{2}[2a + (n - 1)d]$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}; r \neq 1$$

$$S_\infty = \frac{a}{1 - r}; -1 < r < 1$$

$$F = \frac{x[(1 + i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1 + i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$\text{In } \Delta ABC: \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cdot \cos A$$

$$\text{area } \Delta ABC = \frac{1}{2} ab \cdot \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases}$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\sin 2\alpha = 2 \sin \alpha \cdot \cos \alpha$$

$$\bar{x} = \frac{\sum x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$





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**SENIOR CERTIFICATE EXAMINATIONS/  
SENIORSERTIFIKAAT-EKSAMEN  
NATIONAL SENIOR CERTIFICATE EXAMINATIONS/  
NASIONALE SENIORSERTIFIKAAT-EKSAMEN**

**MATHEMATICS P2/WISKUNDE V2  
MARKING GUIDELINES/NASIENRIGLYNE  
MAY/JUNE/MEI/JUNIE 2024**

**MARKS: 150  
PUNTE: 150**

*M. Dasman*  
Approved (UMALUSI)  
2024-05-14

These marking guidelines consist of 26 pages.  
*Hierdie nasienriglyne bestaan uit 26 bladsye.*

APPROVED  
*Opambili (DBE IM)*  
14/5/2024



*[Signature]*  
Approved  
*[Signature]*  
2024/05/14  
2024-05-14

DEPARTMENT OF BASIC  
EDUCATION  
PRIVATE BAG 4886, PRETORIA 0001

2024-05-18

APPROVED MARKING GUIDELINES  
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**NOTE:**

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and did not redo the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the Marking Guidelines. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

**LET WEL:**

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.
- As 'n kandidaat 'n antwoord op 'n vraag doodtrek en nie oordoen nie, sien die doodgetrekte poging na.
- Volgehoue akkuraatheid word in ALLE aspekte van die Nasiennriglyne toegepas. Hou op nasien by die tweede berekeningsfout.
- Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.

GEOMETRY	
S	A mark for a correct statement (A statement mark is independent of a reason)  'n Punt vir 'n korrekte bewering ('n Punt vir 'n bewering is onafhanklik van die rede)
R	A mark for the correct reason (A reason mark may only be awarded if the statement is correct)  'n Punt vir 'n korrekte rede ('n Punt word slegs vir die rede toegeken as die bewering korrek is)
S/R	Award a mark if statement AND reason are both correct  Ken 'n punt toe as die bewering EN rede beide korrek is

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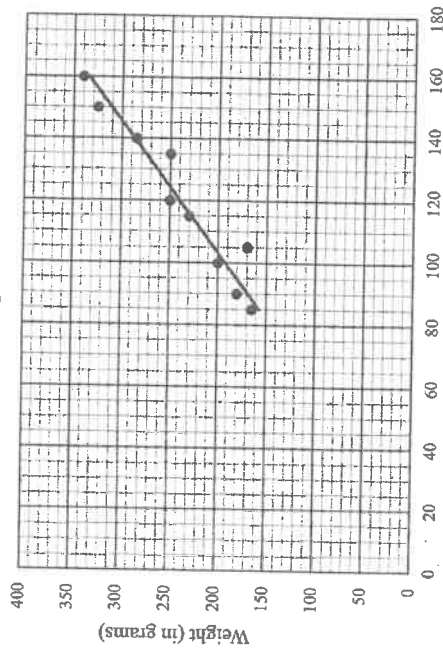
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**QUESTION/VRAAG 1**

1.1  $a = -43,72$   
 $b = 2,36$   
 $y = -43,72 + 2,36x$

1.2  $a = -43,72$   
 $b = 2,36$   
 equation

Scatter plot



1.3  $y = -43,72 + 2,36(110)$   
 $y = 215,88$

OR

$y = 215,90$  (calculator)

1.4  $y = -43,72 + 2,36(130)$   
 $y = 263,08$

Percentage increase in weight =  $\frac{263,08 - 215,88}{215,88} \times 100$   
 $= 21,86\%$

OR

$y = 263,08$

Percentage =  $\frac{263,08}{215,88} \times 100$   
 $= 121,86\%$

Percentage increase in weight =  $121,86 - 100 = 21,86$

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QUESTION/VRAG 2

2.1

Distance (x km)	Frequency	Cumulative frequency
$0 \leq x < 5$	3	3
$5 \leq x < 10$	7	10
$10 \leq x < 15$	20	30
$15 \leq x < 20$	12	42
$20 \leq x < 25$	5	47
$25 \leq x < 30$	3	50

✓ 10  
✓ all values correct

2.2

Ogive/Ogief

Distance/Afstand (in km)

2.3

$Q_3 = 17,8$   
 $Q_1 = 11$   
IQR = 6,8

✓  $Q_3$  (accept between 17-19) and  $Q_1$  (accept between 10-12,5) answer (accept 5-9)

2

2.4

$5 \leq x < 10$  ✓  $5 \leq x < 10$

2.5

Estimated mean =  $\frac{2,5(3) + 7,5(1) + 12,5(20) + 17,5(8) + 22,5(5) + 27,5(3)}{50}$  ✓ new frequencies

$= \frac{675}{50}$  ✓  $\sum fx$

$= 13,5$  km ✓ answer

(1)

(3)

(1)

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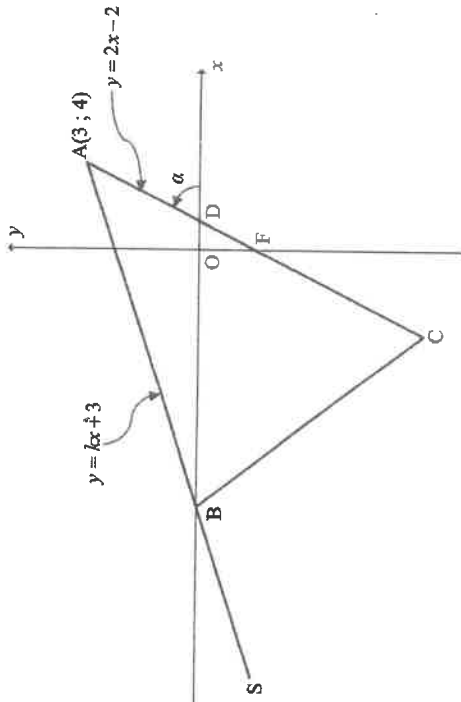
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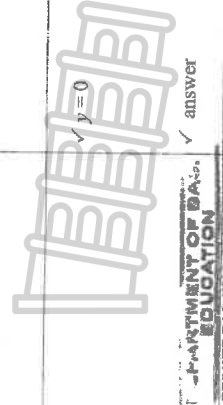
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2





<p>3.1</p> $y = kx + 3$ $4 = k(3) + 3$ $3k = 1$ $\therefore k = \frac{1}{3}$ <p><b>OR</b></p> <p>y-intercept of AB: (0 ; 3)</p> $m_{AB} = \frac{4-3}{3-0}$ $= \frac{1}{3}$ $\therefore k = \frac{1}{3}$	<p>(1)</p> <p>✓ substitution (3 ; 4)</p>	<p>(1)</p> <p>✓ substitution (0 ; 3)</p>	<p>(1)</p> <p>✓ <math>y=0</math></p> <p>✓ answer</p>
<p>3.2</p> $0 = \frac{1}{3}x + 3$ $-3 = \frac{1}{3}x$ $x = -9$ <p>B(-9 ; 0)</p>	<p>(2)</p>		



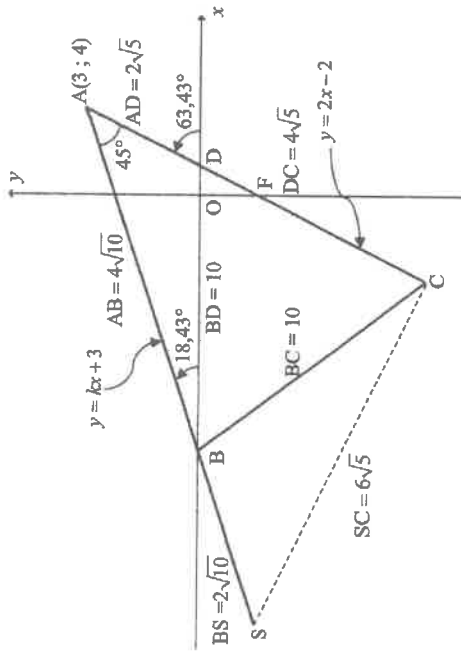
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<p>3.3</p> <p><math>F(0; -2)</math></p> $F\left(\frac{x+3}{2}; \frac{y+4}{2}\right)$ $\frac{x+3}{2} = 0$ $x = -3$ $C(-3; -8)$ <p><b>OR by translation</b></p> <p><math>F(0; -2)</math></p> <p><math>A \rightarrow F(x; y) \rightarrow (x-3; y-6)</math></p> <p><math>F \rightarrow C(0; -2) \rightarrow (0-3; -2-6) = (-3; -8)</math></p>	<p>(4)</p> <p>✓ <math>F(0; -2)</math></p> <p>✓ <math>\frac{x+3}{2} = 0; \frac{y+4}{2} = -2</math></p> <p>✓ x-value ✓ y-value</p> <p>✓ <math>F(0; -2)</math></p> <p>✓ <math>(x-3; y-6)</math></p> <p>✓ x-value ✓ y-value</p>
<p>3.4</p> $m_{BC} = \frac{0-(-8)}{-9-(-3)}$ <p><b>OR</b></p> $m_{BC} = \frac{-8-0}{-3-(-9)}$ $m_{BC} = -\frac{4}{3}$ $y = -\frac{4}{3}x + c$ $(-2) = -\frac{4}{3}(-15) + c$ $c = -22$ $y = -\frac{4}{3}x - 22$ <p><b>OR</b></p> $m_{BC} = \frac{0-(-8)}{-9-(-3)}$ <p><b>OR</b></p> $m_{BC} = \frac{-8-0}{-3-(-9)}$ $m_{BC} = -\frac{4}{3}$ <p><math>y - y_1 = -\frac{4}{3}(x - x_1)</math></p> <p><math>y - (-2) = -\frac{4}{3}(x - (-15))</math></p> $y + 2 = -\frac{4}{3}x - 20$ $y = -\frac{4}{3}x - 22$	<p>(4)</p> <p>✓ substitution of B and C into the gradient formula</p> <p>✓ <math>m_{BC}</math></p> <p>✓ <math>m_{line} = m_{BC}</math></p> <p>✓ substitution of <math>S(-15; -2)</math></p> <p>✓ equation</p>
<p>3.5</p> <p>substitution into the gradient formula</p> <p><math>m_{BC}</math></p> <p><math>m_{line} = m_{BC}</math></p> <p>substitution of <math>S(-15; -2)</math></p> <p>equation</p>	<p>(5)</p> <p>✓ substitution into the gradient formula</p> <p>✓ <math>m_{BC}</math></p> <p>✓ <math>m_{line} = m_{BC}</math></p> <p>✓ substitution of <math>S(-15; -2)</math></p> <p>✓ equation</p>

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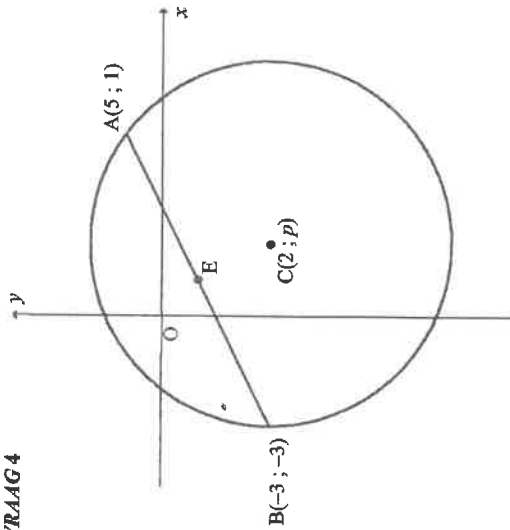
3.5	$\tan \alpha = m_{AC} = 2$ $\alpha = 63,43^\circ$ $\tan \hat{A}BD = m_{AS} = \frac{1}{3}$ $\hat{A}BD = 18,43^\circ$ $\hat{B}AC = \alpha - \hat{A}BD$ $\hat{B}AC = 63,43^\circ - 18,43^\circ$ $\hat{B}AC = 45^\circ$ <b>OR</b> $AB = \sqrt{(-9-3)^2 + (0-4)^2}$ $AB = 4\sqrt{10}$ $BD = 10$ $AD = \sqrt{(3-1)^2 + (4-0)^2}$ $AD = 2\sqrt{5}$ $BD^2 = AB^2 + AD^2 - 2AB \cdot AD \cos \hat{B}AC$ $(10)^2 = (4\sqrt{10})^2 + (2\sqrt{5})^2 - 2(4\sqrt{10})(2\sqrt{5}) \cos \hat{B}AC$ $\cos \hat{B}AC = \frac{\sqrt{2}}{2}$ $\hat{B}AC = 45^\circ$	✓ $\tan \alpha = m_{AC} = 2$ ✓ $\alpha = 63,43^\circ$ ✓ $\tan \hat{A}BD = m_{AS} = \frac{1}{3}$ ✓ $\hat{A}BD = 18,43^\circ$ ✓ answer ✓ length of AB ✓ calculation of remaining 2 lengths ✓ substitution into cosine-rule ✓ rewriting in terms of $\cos \hat{B}AC$ ✓ answer	(5)
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*MS*

3.6	$A(3; 4)$ and $S(-15; -2)$ $AS = \sqrt{(x_A - x_S)^2 + (y_A - y_S)^2}$ $AS = \sqrt{(3 - (-15))^2 + (4 - (-2))^2}$ $AS = \sqrt{360} = 6\sqrt{10} = 18,97$ Area of $\triangle ABD = \frac{1}{2}(BD)(\perp h)$ Area of $\triangle ASC = \frac{1}{2}(AS)(AC) \sin \hat{B}AC$ Area of $\triangle ABD = \frac{1}{2}(10)(4)$ Area of $\triangle ASC = \frac{1}{2}(6\sqrt{10})(6\sqrt{5}) \sin 45^\circ$ Area of $\triangle ABD = 2$ Area of $\triangle ASC = 9$	✓ Area $\triangle ABD$ ✓ Area $\triangle ASC$ ✓ answer ✓ length of AS	(5)
	<b>OR</b> $AS = \sqrt{(3 - (-15))^2 + (4 - (-2))^2}$ $AS = \sqrt{360} = 6\sqrt{10} = 18,97$ $AB = \sqrt{(-9-3)^2 + (0-4)^2} = 4\sqrt{10}$ $AD = \sqrt{(3-1)^2 + (4-0)^2} = 2\sqrt{5}$ Area of $\triangle ABD = \frac{1}{2}(AB)(AD) \sin \hat{A}$ Area of $\triangle ASC = \frac{1}{2}(AS)(AC) \sin \hat{A}$ $\frac{1}{2}(4\sqrt{10})(2\sqrt{5}) \sin \hat{A}$ $= \frac{1}{2}(6\sqrt{10})(6\sqrt{5}) \sin \hat{A}$ $= \frac{2}{9}$	✓ Area $\triangle ABD$ ✓ Area $\triangle ASC$ ✓ answer	(5)

*MS*

QUESTION/VRAAG 4



4.1	$E\left(\frac{5+(-3)}{2}, \frac{1+(-3)}{2}\right)$ $\therefore E(1; -1)$	$x = 1 \checkmark \quad y = -1$	(2)	
4.2	$AB = \sqrt{(x_A - x_B)^2 + (y_A - y_B)^2}$ $AB = \sqrt{(5 - (-3))^2 + (1 - (-3))^2}$ $AB = \sqrt{80} = 4\sqrt{5} = 8,94$	$m_{AB} = \frac{1}{5 - (-3)}$ $m_{AB} = \frac{1}{8}$ $\therefore m_{CB} = -2$ $E(1; -1)$ <p style="text-align: center;">[ CE <math>\perp</math> AB ]</p>	$y - y_1 = -2(x - x_1)$ $y - (-1) = -2(x - 1)$ $y = -2x + 1$	(4)
4.3	$m_{AB} = \frac{1}{5 - (-3)}$ $m_{AB} = \frac{1}{8}$ $\therefore m_{CB} = -2$ $E(1; -1)$ <p style="text-align: center;">[ CE <math>\perp</math> AB ]</p>	$m_{AB} = \frac{1}{8}$ $\therefore m_{CB} = -2$	$y - y_1 = -2(x - x_1)$ $y - (-1) = -2(x - 1)$ $y = -2x + 1$	(4)

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4.4	$y = -2x + 1$ $p = -2(2) + 1$ $p = -3$ <p>OR</p> $m_{CB} = -2$ $\frac{p - (-1)}{2 - 1} = -2$ $p + 1 = -2$ $p = -3$	$BC = r = 5 \text{ units}$ $\therefore (x - 2)^2 + (y + 3)^2 = 25$ $x^2 - 4x + 4 + y^2 + 6y + 9 = 25$ $x^2 + y^2 - 4x + 6y - 12 = 0$	$\checkmark$ substitution of C(2; p) into $\perp$ bisector of AB $\checkmark$ substitution of C and E into the gradient formula $\checkmark$ BC = r = 5 units $\checkmark (x - 2)^2 + (y + 3)^2 = 25$ $\checkmark x^2 - 4x + 4 + y^2 + 6y + 9 = 25$	(1)
4.5	$(x - 2)^2 + (y + 3)^2 = 25$ $y = tx + 8$ $(x - 2)^2 + (tx + 8 + 3)^2 = 25$ $x^2 - 4x + 4 + t^2x^2 + 22tx + 121 - 25 = 0$ $x^2(t^2 + 1) + x(22t - 4) + 100 = 0$ $\Delta < 0$ $(22t - 4)^2 - 4(t^2 + 1)(100) < 0$ $484t^2 - 176t + 16 - 400t^2 - 400 < 0$ $84t^2 - 176t - 384 < 0$ $21t^2 - 44t - 96 < 0$ $(7t - 24)(3t + 4) < 0$	$OR \quad x^2 + y^2 - 4x + 6y - 12 = 0$ $OR \quad x^2 + (x + 8)^2 - 4x + 6(x + 8) - 12 = 0$ $OR \quad x^2 + t^2x^2 + 16tx + 64 - 4x + 6x + 48 - 12 = 0$	$\checkmark$ substitution of $y = tx + 8$ into standard form $\checkmark \Delta < 0$ $\checkmark$ standard form of $\Delta$ $\checkmark$ critical values $\checkmark$ answer	(6)

4.6	$CV: \frac{24}{7}; -\frac{4}{3}$		$\therefore t \in \left(-\frac{4}{3}; \frac{24}{7}\right)$ <p>OR</p> $-\frac{4}{3} < t < \frac{24}{7}$	(6)
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*MS*

QUESTION/VRAGS

<p>5.1.1 <math>\sin 220^\circ</math> = <math>-\sin 40^\circ</math> = <math>-p</math></p>	<p>✓ <math>-\sin 40^\circ</math> ✓ answer</p>
<p>5.1.2 <math>\cos^2 50^\circ</math> = <math>\sin^2 40^\circ</math> = <math>p^2</math></p>	<p>✓ <math>\sin^2 40^\circ</math> ✓ answer</p>
<p>5.1.3 <math>\cos(-80^\circ)</math> = <math>\cos 80^\circ</math> = <math>1 - 2\sin^2 40^\circ</math> = <math>1 - 2p^2</math> <b>OR</b> <math>\cos(-80^\circ)</math> = <math>\cos 80^\circ</math> = <math>\cos(30^\circ + 50^\circ)</math> = <math>\cos 30^\circ \cos 50^\circ - \sin 30^\circ \sin 50^\circ</math> = <math>\frac{\sqrt{3}p}{2} - \sqrt{1-p^2}</math></p>	<p>✓ <math>\cos 80^\circ</math> ✓ double angle ✓ answer  ✓ <math>\cos 80^\circ</math> ✓ expansion ✓ answer</p>
<p>5.2.1 LHS = <math>\tan x(1 - \cos^2 x) + \cos^2 x</math> = <math>\frac{\sin x}{\cos x}(\sin^2 x) + \cos^2 x</math> = <math>\frac{\sin^3 x + \cos^3 x}{\cos x}</math> = <math>\frac{(\sin x + \cos x)(\sin^2 x - \sin x \cos x + \cos^2 x)}{\cos x}</math> = <math>\frac{(\sin x + \cos x)(1 - \sin x \cos x)}{\cos x}</math> = RHS</p>	<p>✓ <math>\frac{\sin x}{\cos x}</math> ✓ <math>\sin^2 x</math> ✓ simplification ✓ factorisation of cubes ✓ <math>\sin^2 x + \cos^2 x = 1</math></p>

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<p>RHS = <math>\frac{(\sin x + \cos x)(1 - \sin x \cos x)}{\cos x}</math> = <math>\frac{\sin x - \sin^2 x \cos x + \cos x - \sin x \cos^2 x}{\cos x}</math> = <math>\frac{\tan x - \sin^2 x + 1 - \sin x \cos x}{\cos x}</math> = <math>\frac{\tan x + \cos^2 x - \sin x \cos x}{\cos x}</math> = <math>\frac{\tan x \left(1 - \frac{\sin x \cos x}{\tan x}\right) + \cos^2 x}{\cos x}</math> = <math>\frac{\tan x \left(1 - \frac{\sin x \cos x}{\frac{\sin x}{\cos x}}\right) + \cos^2 x}{\cos x}</math> = <math>\frac{\tan x \left(1 - \cos^2 x\right) + \cos^2 x}{\cos x}</math> = LHS</p>	<p>5.2.2 <math>\cos x = 0</math> or where <math>\tan x</math> is undefined <math>x = 90^\circ + k \cdot 360^\circ</math> or <math>x = 270^\circ + k \cdot 360^\circ</math> <math>x = 90^\circ</math> or <math>x = -90^\circ</math></p>	<p>5.3.1 <math>\frac{\sin 150^\circ + \cos^2 x - 1}{2}</math> = <math>\frac{\sin 30^\circ + \cos^2 x - 1}{2}</math> = <math>\frac{1}{2} - \frac{(1 - \cos^2 x)}{2}</math> = <math>\left(\frac{1}{2} - \sin^2 x\right) \times \frac{1}{2}</math> = <math>\frac{1 - 2\sin^2 x}{4}</math> = <math>\frac{\cos 2x}{4}</math></p>	<p>5.3.2 <math>\frac{\sin 150^\circ + \cos^2 x - 1}{2} = \frac{1}{25}</math> <math>\frac{\cos 2x}{4} = \frac{1}{25}</math> <math>\cos 2x = \frac{4}{25}</math> ref <math>\angle = 80,79^\circ</math>  <math>2x = 80,79^\circ + k \cdot 360^\circ</math> or <math>2x = 279,20^\circ + k \cdot 360^\circ</math> <math>x = 40,40^\circ + k \cdot 180^\circ</math> or <math>x = 139,60^\circ + k \cdot 180^\circ</math>; <math>k \in \mathbb{Z}</math></p>	<p>✓ multiplication ✓ <math>\div</math> by <math>\cos x</math> ✓ <math>-\sin^2 x + 1 = \cos^2 x</math> ✓ factorisation ✓ <math>\tan x = \frac{\sin x}{\cos x}</math>  ✓ <math>\cos x = 0</math> or <math>\tan x</math> undefined ✓ <math>x = 90^\circ</math> ✓ <math>x = -90^\circ</math>  ✓ <math>\sin 30^\circ</math> ✓ <math>\sin 30^\circ = \frac{1}{2}</math> ✓ factor ✓ <math>1 - \cos^2 x = \sin^2 x</math> ✓ simplification ✓ answer in terms of <math>\cos 2x</math>  ✓ answer 5.3.1 = <math>\frac{1}{25}</math>  ✓ <math>2x = 80,79^\circ</math> ✓ <math>2x = 279,20^\circ</math> ✓ <math>x = 40,40^\circ</math> and <math>x = 139,60^\circ</math> ✓ <math>+ k \cdot 180^\circ</math>; <math>k \in \mathbb{Z}</math></p>
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QUESTION/VRAAG 6

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6.1	Period = $360^\circ$	✓ $360^\circ$	(3)
6.2	Amplitude = 1	✓ 1	(3)
6.3	$a = -45^\circ$	✓ $a = -45^\circ$	(1)
6.4	$\sin 2x = k$ $k = \sin(2 \times 165^\circ)$ OR $k = \sin(2 \times (-75^\circ))$ $k = \sin 330^\circ$ OR $k = \sin(-150^\circ)$ $k = -\sin 30^\circ$ $k = -\frac{1}{2}$	✓ $-\sin 30^\circ$ ✓ $-\frac{1}{2}$	(2)
	OR $k = \cos(65^\circ - 45^\circ)$ OR $k = \cos(-75^\circ - 45^\circ)$ $k = \cos 120^\circ$ OR $k = \cos(-120^\circ)$ $k = -\cos 60^\circ$ $k = -\frac{1}{2}$	✓ $-\cos 60^\circ$ ✓ $-\frac{1}{2}$	(2)
6.5	Points of intersection are translated $60^\circ$ to the left $x = -15^\circ$	✓ $x = -15^\circ$	(1)
6.6	$\sqrt{2} \sin 2x = \sin x + \cos x$ $\sin 2x = \frac{1}{\sqrt{2}} \sin x + \frac{1}{\sqrt{2}} \cos x$ $\sin 2x = \sin 45^\circ \sin x + \cos 45^\circ \cos x$ $\sin 2x = \cos(45^\circ - x)$ OR $\sin 2x = \cos(x - 45^\circ)$  $\therefore 2$ roots in the interval $x \in [-90^\circ; 90^\circ]$	✓ division by $\sqrt{2}$ ✓ special angles ✓ $\cos(45^\circ - x)$ or $\cos(x - 45^\circ)$ ✓ answer	(4)
			10

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OR $\frac{\sin 150^\circ + \cos^2 x - 1}{2} = \frac{1}{25}$ $\sin 150^\circ + \cos^2 x - 1 = \frac{2}{25}$ $\sin 30^\circ + \cos^2 x - 1 = \frac{2}{25}$ $\cos^2 x = \frac{29}{50}$ $\cos x = \pm \sqrt{\frac{29}{50}}$ $x = 40, 40^\circ + k \cdot 360^\circ$ OR $x = 319, 60^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ OR $x = 139, 60^\circ + k \cdot 360^\circ$ OR $x = 220, 40^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$	✓ $\cos^2 x = \frac{29}{50}$  ✓ $x = 40, 40^\circ$ ✓ $x = 139, 60^\circ$ ✓ $x = 220, 40^\circ$ and $x = 319, 60^\circ$ ✓ $+ k \cdot 360^\circ; k \in \mathbb{Z}$	(5)
		26

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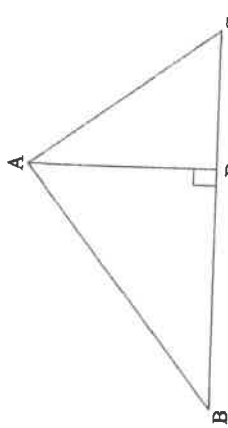
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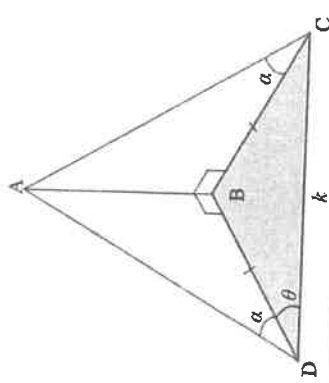
QUESTION/VRAAG 7

7.1



7.1.1	$\sin \hat{B} = \frac{AD}{AB}$ $AD = AB \sin \hat{B}$	$\checkmark \sin \hat{B} = \frac{AD}{AB}$ $\checkmark$ answer
7.1.2	$\text{Area of } \triangle ABC = \frac{1}{2}(BC)(AD)$ $\therefore \text{Area of } \triangle ABC = \frac{1}{2}(BC)(AB) \sin \hat{B}$	$\checkmark \frac{1}{2}(BC)(AD)$ (2)

7.2



7.2.1	In $\triangle ADB$ $\sin \alpha = \frac{AB}{AD}$ $AD = \frac{AB}{\sin \alpha}$ In $\triangle ABC$ $\sin \alpha = \frac{AB}{AC}$ $AC = \frac{AB}{\sin \alpha}$ $AD = AC$ OR	$\checkmark \sin \alpha = \frac{AB}{AD}$ $\checkmark \sin \alpha = \frac{AB}{AC}$
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In $\triangle ADB$ and $\triangle ADB$ $AB = AB$ $\hat{A}DB = \hat{A}DB = 90^\circ$ $BD = BC$ $\triangle ADB \cong \triangle ADB$ $\therefore AD = AC$ OR In $\triangle ADB$ and $\triangle ADB$ $\hat{A}DB = \hat{A}DB = \alpha$ $\hat{A}BD = \hat{A}DB = 90^\circ$ $AB = AB$ OR $BD = BC$ $\therefore \triangle ADB \cong \triangle ADB$ $\therefore AD = AC$ OR $AD^2 = AB^2 + DB^2$ $AC^2 = AB^2 + BC^2$ But $DB = BC$ $\therefore AD^2 = AC^2$ $\therefore AD = AC$	[common side] [given] [given] [S,ZS] [Pythagoras] [Pythagoras] [given]	$\checkmark \triangle ADB \cong \triangle ADB$ ✓ R (2) $\checkmark$ both Pythagoras statements $\checkmark DB = BC$ (2)
7.2.2	$\frac{BD}{\sin \theta} = \frac{k}{\sin(180^\circ - 2\theta)}$ $BD = \frac{k \sin \theta}{\sin 2\theta}$ $BD = \frac{k \sin \theta}{2 \sin \theta \cos \theta}$ $BD = \frac{k}{2 \cos \theta}$ OR $BC^2 = k^2 + BD^2 - 2k(BD) \cos \theta$ $BD^2 = k^2 + BD^2 - 2k(BD) \cos \theta$ $k^2 - 2k(BD) \cos \theta = 0$ $2k(BD) \cos \theta = k^2$ $\therefore BD = \frac{k}{2 \cos \theta}$	$\checkmark$ substitution of $(180^\circ - 2\theta)$ into sine rule $\checkmark$ reduction $\checkmark$ double angle (3) $\checkmark$ substitution into cosine rule $\checkmark$ substitution BC with BD into cosine-rule $\checkmark$ simplification in terms of BD (3)

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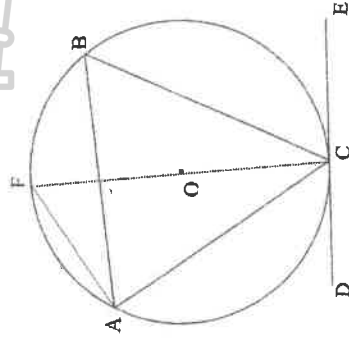
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7.2.3	<p>Area of <math>\triangle BCD = \frac{1}{2}(DC)(BD)(\sin CDB)</math>  <math>= \frac{1}{2}k \left( \frac{k}{2 \cos \theta} \right) \sin \theta</math>  <math>= \frac{1}{4}k^2 \tan \theta</math></p> <p><b>OR</b></p> <p>Area of <math>\triangle BCD = \frac{1}{2}(BD)(BC)(\sin(180^\circ - 2\theta))</math>  <math>= \frac{1}{2} \left( \frac{k}{2 \cos \theta} \right) \left( \frac{k}{2 \cos \theta} \right) (\sin 2\theta)</math>  <math>= \frac{2k^2 \sin \theta \cos \theta}{8 \cos \theta \cos \theta}</math>  <math>= \frac{1}{4}k^2 \tan \theta</math></p>	<p>✓ substitution into area rule  <math>\frac{\sin \theta}{\cos \theta} = \tan \theta</math>  <math>\frac{1}{4}k^2 \tan \theta</math></p> <p>✓ substitution into area rule  <math>\frac{\sin \theta}{\cos \theta} = \tan \theta</math>  <math>\frac{1}{4}k^2 \tan \theta</math></p>	(3) (11)
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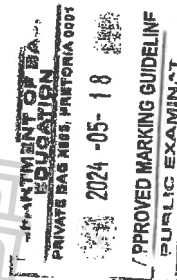
**QUESTION/VRAAG 8**

8.1

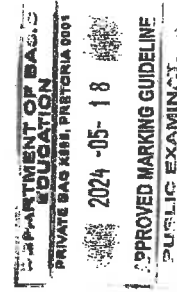


Construction: Draw diameter CF and draw AF Konstruksie: Trek middellyn CF en verbind AF	<p>✓ Constr</p> <p>✓ S ✓ R</p> <p>✓ S/R</p> <p>✓ S/R</p>	(5)
FĈE = 90°	[tan ⊥ radius/raaklyn ⊥ radius]	
FĀC = 90°	[∠ in semi circle/∠ in half sirkel]	
FĀB = FĈB	[∠s same segment/∠e dieselfde segm]	
∴ BĀC = BĈE		
∴ BCB = Ā		

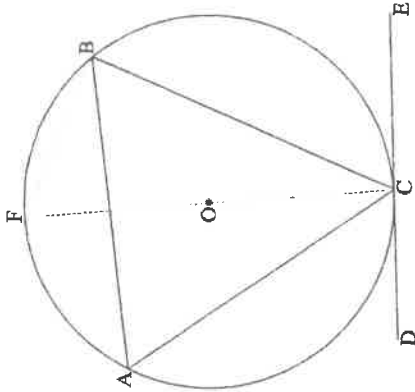
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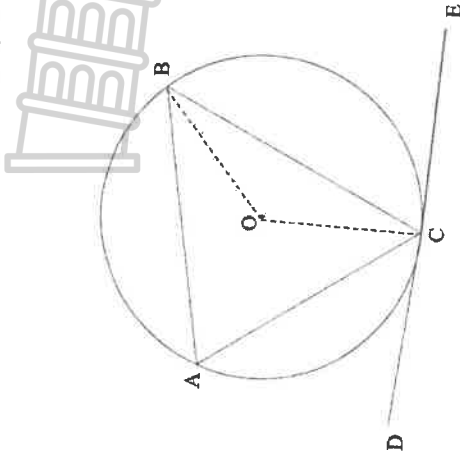


<p>Construction: Draw diameter CF and draw FB                  Konstrukisie: Trek middellyn CF en verbind FB</p> <p><math>\widehat{FBC} = 90^\circ</math>  <math>\widehat{BFC} + \widehat{FCB} = 90^\circ</math></p> <p><math>\widehat{OCB} = 90^\circ</math>  <math>\therefore \widehat{BCE} = \widehat{A}</math>                  but <math>\widehat{A} = \widehat{A}</math>  <math>\therefore \widehat{BCE} = \widehat{A}</math></p>	<p>[<math>\sphericalangle</math> in semi circle/<math>\sphericalangle</math> in halwe sirkel]                  [sum of <math>\sphericalangle</math>s in <math>\Delta</math>/binne <math>\sphericalangle</math>e v <math>\Delta</math>]</p> <p>[tan <math>\perp</math> radius/ raaklyn <math>\perp</math> radius]</p> <p>[<math>\sphericalangle</math>s in same seg/<math>\sphericalangle</math> in dies. segment]</p>	<p>✓ construction</p> <p>✓ S / R</p> <p>✓ S ✓ R</p> <p>✓ S / R</p>	(5)
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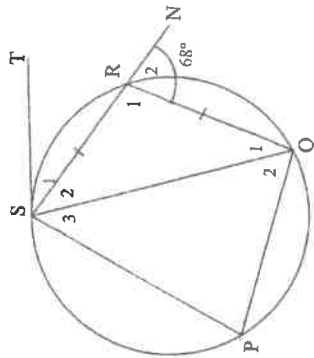


<p>Construction: Draw radii BO and OC                  Konstrukisie: Trek radiusse BO en OC</p> <p><math>\widehat{OCB} = 90^\circ</math> or <math>\widehat{BCE} = 90^\circ - \widehat{OCB}</math> [tan <math>\perp</math> radius / raaklyn <math>\perp</math> radius]</p> <p><math>\widehat{OCB} = \widehat{OBC}</math>  <math>\therefore \widehat{COB} = 180^\circ - 2\widehat{OCB}</math>  <math>\widehat{CAB} = 90^\circ - \widehat{OCB}</math>  <math>\therefore \widehat{BCE} = \widehat{CAB}</math></p>	<p>[<math>\sphericalangle</math>s opp equal sides/  <math>\sphericalangle</math>e teenoor gelyke sye]                  [<math>\sphericalangle</math>s of <math>\Delta</math>/<math>\sphericalangle</math>e van <math>\Delta</math>]                  [<math>\sphericalangle</math> at centre = <math>2 \times \sphericalangle</math> circumf/                  midpts <math>\sphericalangle</math> = <math>2 \times</math> omtreks <math>\sphericalangle</math>]</p>	<p>✓ construction</p> <p>✓ S ✓ R</p> <p>✓ S</p> <p>✓ S/R</p>	(5)
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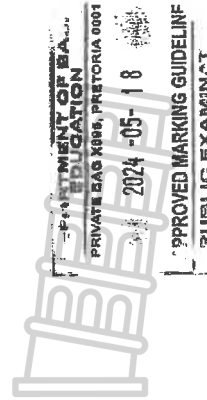
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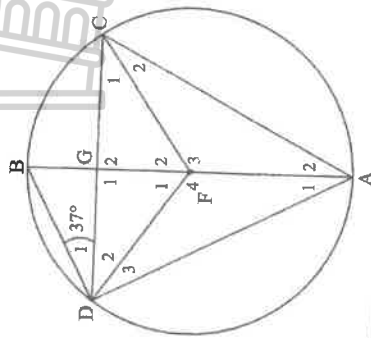




8.2.1	$\hat{P} = \hat{R}_2 = 68^\circ$	[ext $\angle$ of cyclic quad /buite $\angle$ van kvh]	✓ S ✓ R	(2)
8.2.2	$\hat{Q}_1 = \hat{S}_2$ $\hat{Q}_1 + \hat{S}_2 = 68^\circ$ $\therefore \hat{Q}_1 = 34^\circ$	[ $\angle$ s opp equal sides / $\angle$ e teenoor gelyke sye] [ext $\angle$ of $\Delta$ / buite $\angle$ van $\Delta$ ]	✓ S	
8.2.3	$\hat{S}_1 = \hat{Q}_1 = 34^\circ$	[tan-chord theorem / $\angle$ tussen rkl en koord]	✓ S ✓ R	(2)
[11]				



QUESTION/VRAG 9

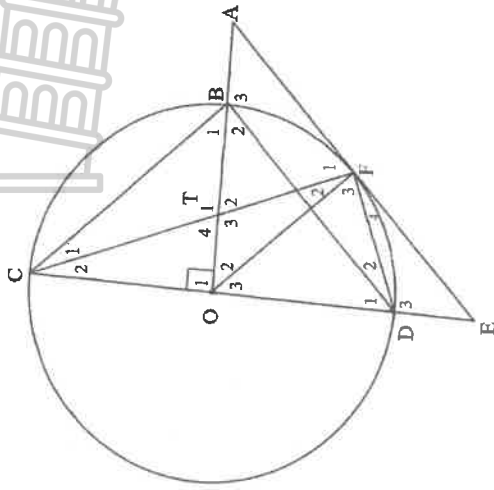


9.1	$\hat{A}_2 = \hat{D}_1 = 37^\circ$ $\hat{A}_1 = \hat{A}_3 = 37^\circ$ $\hat{D}_3 = \hat{A}_1 = 37^\circ$ $\hat{C}_2 = \hat{A}_2 = 37^\circ$	[ $\angle$ s in the same seg / $\angle$ e in dies segment] [BA bisects $\hat{C}\hat{A}\hat{D}$ / BA halveer $\hat{C}\hat{A}\hat{D}$ ] [ $\angle$ s opp equal sides / $\angle$ e teenoor gelyke sye] [ $\angle$ s opp equal sides / $\angle$ e teenoor gelyke sye]	✓ S ✓ R ✓ any other two statements	(4)
9.2	$\hat{A}\hat{D}\hat{G} = 53^\circ$ $\hat{A}_1 = 37^\circ$ $\therefore \hat{G}_1 = 90^\circ$ $\therefore CG = DG$	[ $\angle$ in semi circle / $\angle$ in halwe sirkel] [proved in 9.1 / reeds bewys in 9.1] [sum of $\angle$ s in $\Delta$ / binne $\angle$ e van $\Delta$ ] [line from centre $\perp$ to chord / lyn uit midpt. $\perp$ op koord]	✓ S ✓ R ✓ S ✓ R	(4)
OR				
	$\hat{F}_2 = 2\hat{D}_1 = 74^\circ$ $\hat{D}_3 = 37^\circ$ $\therefore \hat{D}_2 = 16^\circ$ $\hat{C}_1 = \hat{D}_2 = 16^\circ$ $\therefore \hat{G}_2 = 90^\circ$ $\therefore CG = DG$	[ $\angle$ at centre = $2 \times \angle$ at circumference / midpt. $\angle$ s = $2 \times$ omtreks $\angle$ ] [proved in 9.1 / reeds bewys in 9.1] [ $\angle$ in semi circle / $\angle$ in halwe sirkel] [ $\angle$ s opp equal sides / $\angle$ e teenoor gelyke sye] [sum of $\angle$ s in $\Delta$ / binne $\angle$ e van $\Delta$ ] [line from centre $\perp$ to chord / lyn uit midpt. $\perp$ op koord]	✓ S ✓ R ✓ S ✓ R	(4)

<p>9.3 <math>\hat{F}_1 = 2\hat{D}_1 = 74^\circ</math> OR <math>\hat{F}_2 = 2\hat{A}_2 = 74^\circ</math> [<math>\angle</math> at centre = <math>2 \times \angle</math> at circum./ midpt. <math>\angle</math> = <math>2 \times</math> omtreks <math>\angle</math>]</p> <p><math>\frac{FG}{20} = \cos 74^\circ</math>  <math>FG = 5,51</math>  <math>\therefore BG = 14,49</math> units</p> <p><b>OR</b></p> <p><math>\hat{F}_2 = 2\hat{D}_1 = 74^\circ</math></p> <p><math>\frac{FG}{20} = \sin 16^\circ</math>  <math>FG = 5,51</math>  <math>\therefore BG = 14,49</math> units</p> <p><b>OR</b></p> <p><math>\frac{DG}{20} = \cos 16^\circ</math>  <math>DG = 19,23</math></p> <p><math>BG = \tan 37^\circ</math>  <math>19,23</math>  <math>BG = 14,49</math> units</p> <p><b>OR</b></p> <p><math>\frac{DG}{20} = \cos 16^\circ</math>  <math>DG = 19,23</math></p> <p><math>FG^2 = FD^2 - DG^2</math>  <math>FG^2 = 20^2 - (19,23)^2</math>  <math>FG = 5,51</math></p> <p><math>BG = 20 - 5,51</math>  <math>= 14,49</math> units</p>	<p>✓ S</p> <p>✓ trig ratio</p> <p>✓ FG</p> <p>✓ answer</p> <p>(4)</p> <p>✓ S</p> <p>✓ trig ratio</p> <p>✓ FG</p> <p>✓ answer</p> <p>(4)</p> <p>✓ trig ratio</p> <p>✓ length of DG</p> <p>✓ trig ratio</p> <p>✓ answer</p> <p>(4)</p> <p>✓ trig ratio</p> <p>✓ length of DG</p> <p>✓ correct use of Pythagoras</p> <p>✓ answer</p> <p>(4)</p>	<p>121</p>
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QUESTION/VRAG 10



<p>10.1 <math>\hat{O}_1 = 90^\circ</math>  <math>\hat{F}_2 + \hat{F}_3 = 90^\circ</math>  <math>\hat{O}_1 = \hat{F}_2 + \hat{F}_3 = 90^\circ</math>  <math>\therefore</math> TODF is a cyclic quad</p>	<p>[given/gegee]  <math>\angle</math> in semi circle/<math>\angle</math> in hakwe sirkel]                    [ext <math>\angle</math> = int opp <math>\angle</math>/                  buite <math>\angle</math> = teenoorst. binne <math>\angle</math>]  <b>OR</b>                  [converse ext <math>\angle</math> of cyclic quad/                  omgekeerde buite <math>\angle</math> v kvh]                  [vert opp <math>\angle</math> = / regoorstaande <math>\angle</math>e]                  [ext <math>\angle</math> of cyclic quad/ buite <math>\angle</math> v kvh]</p>	<p>✓ S ✓ R                  ✓ S                  ✓ R</p>
<p>10.2 <math>\hat{T}_1 = \hat{F}_3</math>                  But <math>\hat{D}_3 = \hat{F}_3</math>  <math>\therefore \hat{T}_1 = \hat{D}_3</math></p>	<p>[ext <math>\angle</math> = int opp <math>\angle</math>/                  buite <math>\angle</math> = teenoorst. binne <math>\angle</math>]                  [converse ext <math>\angle</math> of cyclic quad/                  omgekeerde buite <math>\angle</math> v kvh]                  [vert opp <math>\angle</math> = / regoorstaande <math>\angle</math>e]                  [ext <math>\angle</math> of cyclic quad/ buite <math>\angle</math> v kvh]</p>	<p>✓ S / R                  ✓ S ✓ R</p>
<p>10.3 In <math>\triangle DFE</math> and <math>\triangle TFO</math>                  1) <math>\hat{D}_3 = \hat{T}_3</math>                  2) <math>\hat{F}_4 = \hat{C}_2</math>                  but <math>\hat{C}_2 = \hat{F}_2</math>  <math>\therefore \hat{F}_4 = \hat{F}_2</math>                  3) <math>\hat{E} = \hat{O}_2</math>  <math>\triangle TFO \parallel \triangle DFE</math></p>	<p>[ext <math>\angle</math> of cyclic quad/ buite <math>\angle</math> v kvh]                  [tan-chord theorem/  <math>\angle</math> tussen rkl en koord]                  [<math>\angle</math>s opp equal sides/  <math>\angle</math>e teenoor gelyke sye]                  [3<sup>rd</sup> <math>\angle</math> of <math>\triangle</math> / <math>\angle</math>e van <math>\triangle</math>]                  [∠∠∠]</p>	<p>✓ S                  ✓ S / R                  ✓ S                  ✓ S                  ✓ S OR R</p>

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	<p><b>OR</b>                  In <math>\triangle DFE</math> and <math>\triangle TFO</math>                  1) <math>\hat{D}_3 = \hat{T}_3</math> [ext <math>\angle</math> of cyclic quad/buite <math>\angle</math> van <math>\Delta</math>]                  2) <math>\hat{F}_4 = \hat{C}_2</math> [tan-chord theorem/<math>\angle</math> tussen rkl en koord]  <math>\hat{F}_2 + \hat{F}_3 = 90^\circ</math> [<math>\angle</math> in semi circle/<math>\angle</math> in halwe sirkel]  <math>\hat{D}_1 + \hat{D}_2 = 90^\circ - \hat{C}_2</math> [sum of <math>\angle</math>s in <math>\Delta</math>/ binne <math>\angle</math>e van <math>\Delta</math>]  <math>\hat{E} = 90^\circ - 2\hat{F}_4</math> [ext <math>\angle</math> of <math>\Delta</math>/ buite <math>\angle</math> van <math>\Delta</math>]  <math>\hat{O}_3 = 2\hat{C}_2</math> [<math>\angle</math> at centre = <math>2 \times \angle</math> at circumference/ midpt. <math>\angle</math>s = <math>2 \times</math> omtreks <math>\angle</math>]  <math>\hat{O}_2 = 90^\circ - 2\hat{F}_4</math> [<math>\angle</math>s on a str line/<math>\angle</math>e op 'n reguitlyn]  <math>\hat{O}_2 = \hat{E}</math> <math>\circ</math>                  3) <math>\therefore \hat{F}_4 = \hat{E}_2</math> [3<sup>rd</sup> <math>\angle</math> of <math>\Delta</math>/<math>\angle</math>e van <math>\Delta</math>]  <math>\triangle TFO \parallel \triangle DFE</math> [<math>\angle\angle\angle</math>]</p>	<p>✓ S                  ✓ S / R                  ✓ S                  ✓ S                  ✓ S OR R                  (5)</p>
<p>10.4</p>	<p><math>\hat{B}_2 = \hat{D}_1</math> [<math>\angle</math>s opp equal sides/<math>\angle</math>e teenoor gelyke sye]  <math>\hat{B}_2 = \hat{E}</math> [given/gegee]  <math>\therefore \hat{D}_1 = \hat{E}</math>  <math>\therefore DB \parallel EA</math> [corresp <math>\angle</math>s =/ooreenkomstige <math>\angle</math>e gelyk]</p>	<p>✓ S / R                  ✓ R                  (2)</p>
<p>10.5</p>	<p>In <math>\triangle OEA</math>  <math>DB \parallel EA</math> [proven/reeds bewys]  <math>\frac{OD}{DE} = \frac{OB}{BA}</math> [line <math>\parallel</math> one side of <math>\Delta</math>/lyn <math>\parallel</math> een sy van <math>\Delta</math>]  <b>OR</b>  [prop theorem; <math>DB \parallel EA</math>/ eweredigheid stelling; <math>DB \parallel EA</math>]  <math>\therefore DE = \frac{DO \cdot AB}{OB}</math>  <math>\frac{FO}{FE} = \frac{TO}{DE}</math> [<math>\triangle TFO \parallel \triangle DFE</math>]  <math>DE = \frac{TO \cdot FE}{FO}</math>  <math>\therefore \frac{DO \cdot AB}{OB} = \frac{TO \cdot FE}{FO}</math>  <math>\therefore \frac{DO \cdot AB}{DO} = \frac{TO \cdot FE}{DO}</math> [<math>DO = OB = FO</math>]  <math>\therefore DO = \frac{TO \cdot FE}{AB}</math></p>	<p>✓ R                  ✓ S                  ✓ S / R                  ✓ S                  ✓ S                  (5)</p>
<p style="text-align: right;">19</p>		

TOTAL/TOTAAL: 150