



**PROVINCIAL EXAMINATION  
NOVEMBER 2022  
GRADE 10**

**MATHEMATICS  
(PAPER 2)**

**TIME:** 1 hour

**MARKS:** 100

**9 pages + 1 information sheet and a special answer book of 14 pages**



**INSTRUCTIONS AND INFORMATION**

Read the following instructions carefully before answering the questions.

1. This question paper consists of 10 questions.
2. Answer ALL the questions in the ANSWER BOOK provided.
3. Clearly show ALL calculations, diagrams, graphs, etc. that you have used to determine the answers
4. Answers only will NOT necessarily be awarded full marks.
5. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
6. If necessary, round-off answers to TWO decimal places, unless otherwise stated.
7. Diagrams are NOT necessarily drawn to scale.
8. Write neatly and legibly.



**QUESTION 1**

The heights of 18 grade 8 learners were recorded in cm as shown below. Use the data below to answer the questions that follow.

147	131	142	133	152	125
128	162	129	165	151	130
143	162	110	129	139	153

- 1.1 Represent the data on a stem and leaf diagram. (4)
  - 1.2 Determine the:
    - 1.2.1 Median (2)
    - 1.2.2 Mode (1)
    - 1.2.3 Lower quartile and the upper quartile (2)
    - 1.2.4 Mean (2)
- [11]

**QUESTION 2**

The figures in the table below are the ages, to the nearest year, of a random sample of 30 people negotiating a mortgage in a bank. Use the data below to answer the questions that follow.

29	26	31	42	38	45	35	37	38	38
36	39	49	40	32	32	34	27	56	29
33	31	33	52	44	32	30	38	42	33

- 2.1 Complete the frequency table on the diagram provided in your ANSWER BOOK. (4)

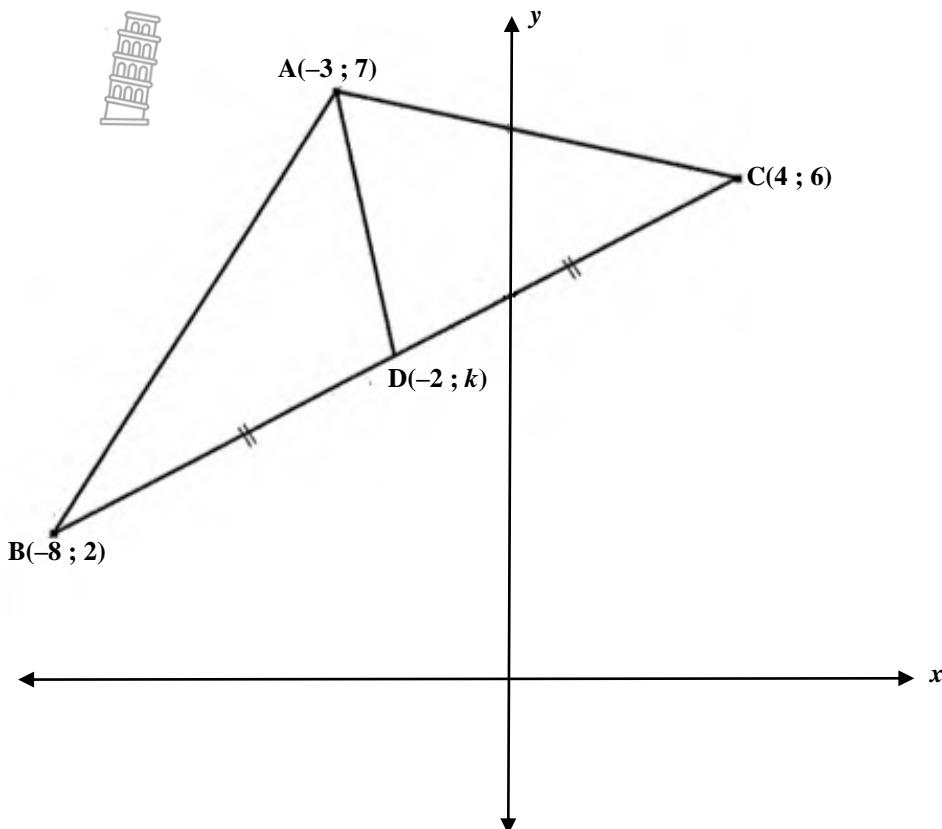
**FREQUENCY TABLE**

AGE INTERVALS	TALLY	FREQUENCY
$25 \leq x < 33$		
$33 \leq x < 41$		
$41 \leq x < 49$		
$49 \leq x < 57$		

- 2.2 Use the information from the frequency table to draw a histogram on the grid provided in the SPECIAL ANSWER SHEET. (2)
  - 2.3 Draw a frequency polygon on the grid provided in the SPECIAL ANSWER SHEET. (3)
- [9]

**QUESTION 3**

In the diagram below A (-3;7), B (-8;2) and C (4;6) are the vertices of triangle ABC. AD is drawn such that D (-2;k) is the midpoint of BC.



- 3.1 Determine the gradient of BC. (2)
- 3.2 Calculate the length of BC. (2)
- 3.3 Determine the value of  $k$ . (2)
- 3.4 Is  $AD \perp BC$ ? Show all your calculations. (3)  
**[9]**

**QUESTION 4**

- 4.1 If  $x = 66,4^\circ$  and  $y = 114,7^\circ$ , evaluate the following correct to TWO decimal places.

- 4.1.1  $\cos(x + y)$  (2)
- 4.1.2  $2\sin x$  (2)
- 4.1.3  $\operatorname{cosec} x$  (2)

4.2 Determine the value of  $\theta$  correct to ONE decimal place.

4.2.1  $\sin \theta + 0,38 = 1$  (2)

4.2.2  $2\cot 2\theta = 3$  (3)

4.2.3  $2\cos(3\theta - 60^\circ) = 1,71$  (4)  
[15]

### QUESTION 5

5.1 Given that  $\sin \theta = \frac{4}{5}$  and  $\tan \theta < 0$ . Determine with the aid of a diagram and WITHOUT the use of a calculator:

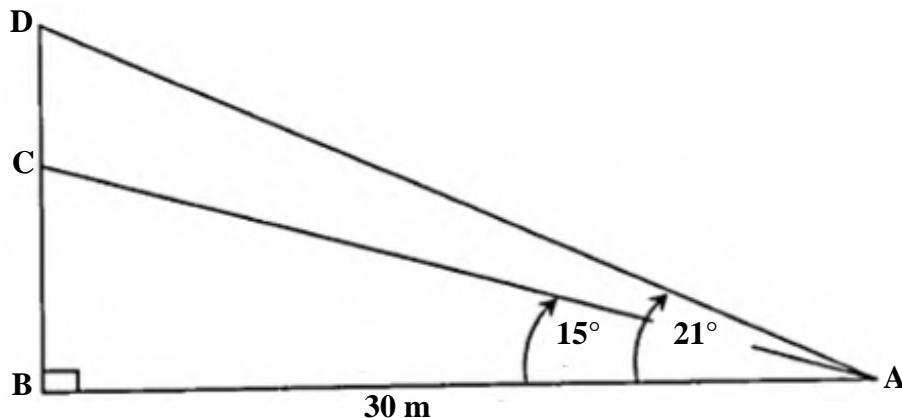
5.1.1  $\tan \theta$  (4)

5.1.2  $2\cos^2 \theta - 1$  (2)

5.2 Simplify the following expression WITHOUT using a calculator.

$$\cos 0^\circ + \sin^2 60^\circ + \sqrt{2} \cdot \sec 45^\circ \quad (4)$$

5.3 In the diagram below, a person is standing at point A which is 30 m away from point B. Point A and point B are on the same horizontal plane. The angle of elevation of a first storey window at point C from point A is  $15^\circ$ . The angle of elevation of the second storey window at point D from point A is  $21^\circ$ .



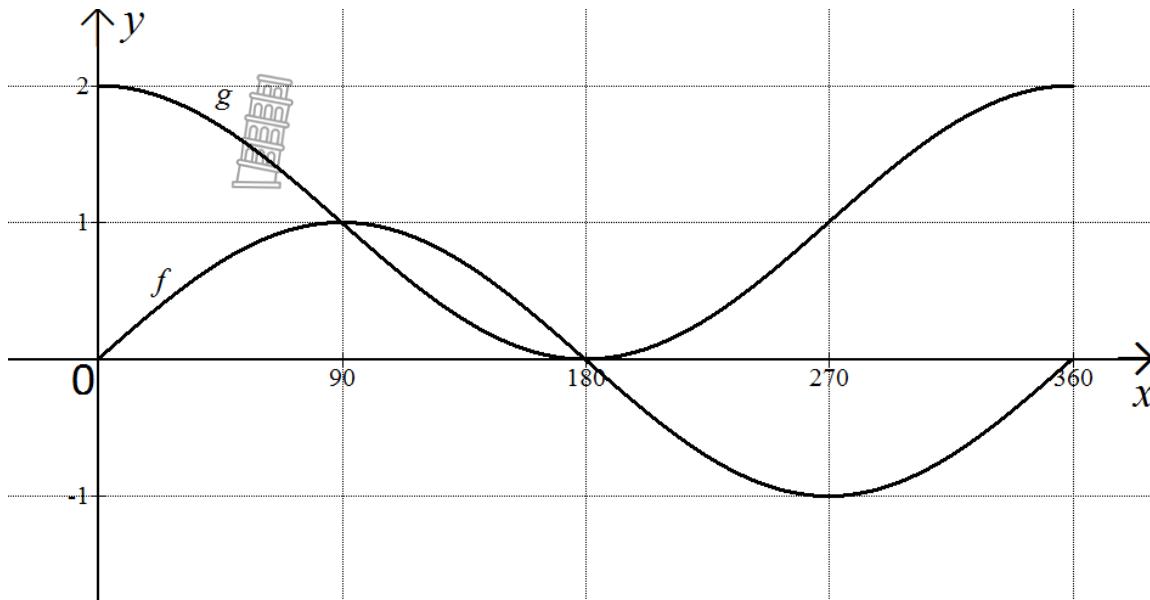
Determine the distance between the two windows.



(6)  
[16]

**QUESTION 6**

The graphs of  $f(x) = a \sin x$  and  $g(x) \cos x + 1$  for  $x \in [0^\circ; 360^\circ]$ .

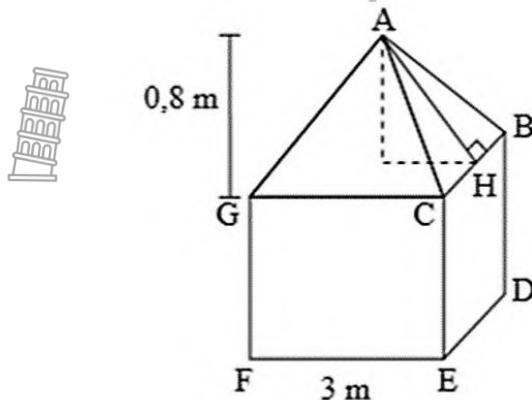


- 6.1 Write down the value of  $a$ . (1)
- 6.2 Determine the range of  $g$ . (2)
- 6.3 Determine the amplitude of  $g$ . (1)
- 6.4 For which value(s) of  $x$  will  $f(x) \geq g(x)$ . (2)
- 6.5 For which value(s) of  $x$  will  $g(x) - f(x) = 2$ . (3)
- 6.6 The graph of  $f$  is reflected across the  $x$ -axis. Write down the equation of the new graph  $h$ . (1)  
[10]



**QUESTION 7**

- 7.1 The roof of a canvas tent is in the shape of a right pyramid having a perpendicular height of 0,8 meters on a square base. The length of one side of the base is 3 metres.



- 7.1.1 Calculate the length of AH. (2)
- 7.1.2 Calculate the surface area of the roof. (2)
- 7.1.3 If the height of the walls of the tent is 2,1 metres, calculate the total amount of canvas required to make the tent if the floor is excluded. (2)

- 7.2 A metal ball has a radius of 8 millimetres.

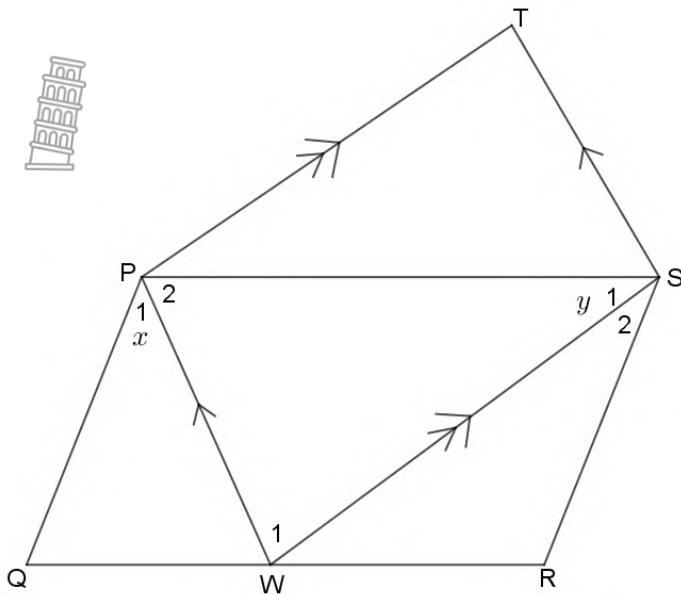
$$\text{Volume of sphere} = \frac{4}{3}\pi r^3$$

- 7.2.1 Calculate the volume of metal used to make this ball. Give your answer correct to TWO decimal places. (2)
- 7.2.2 If the radius of the ball is doubled, write down the ratio of the new volume : the original volume. (2)
- 7.2.3 You would like this ball to be silver plated to a thickness of 1 millimetre. What is the volume of silver required? Give your answer correct to TWO decimal places. (2)
- [12]



**QUESTION 8**

In parallelogram PQRS, PW bisects  $\hat{QPS}$  and SW bisects  $\hat{PSR}$ . PW // ST and PT // WS.

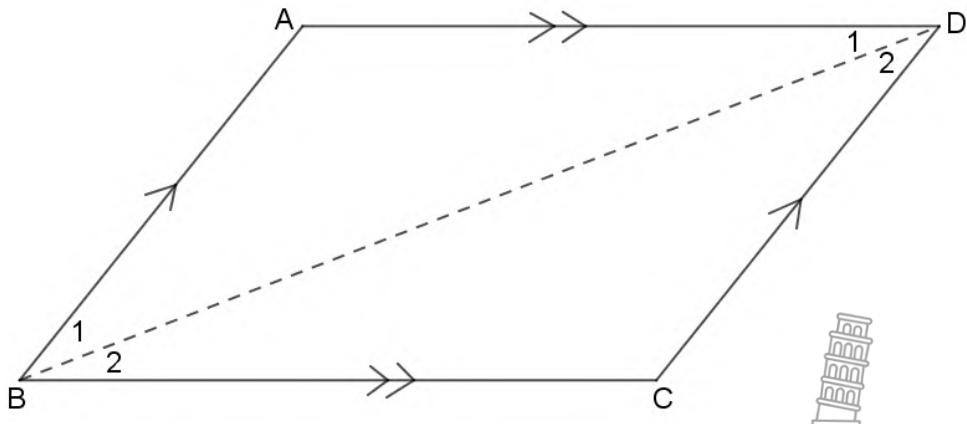


8.1 Prove that  $x + y = 90^\circ$ . (4)

8.2 Prove that PWST is a rectangle. (4)  
[8]

**QUESTION 9**

ABCD is a parallelogram with  $AD // BC$  and  $BA // CD$ .

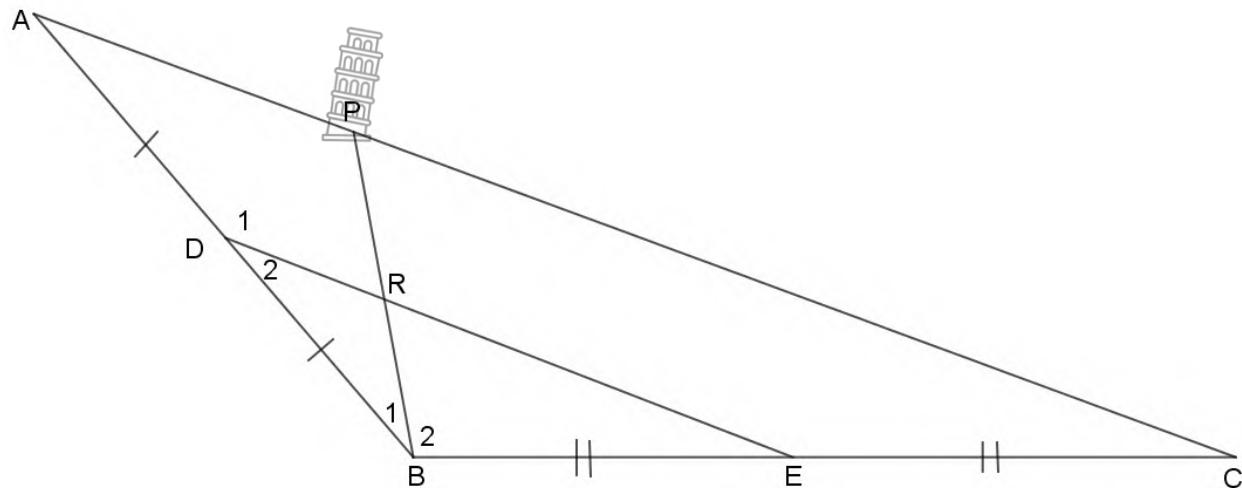


Using the diagram above, prove the theorem that states that the opposite sides of a parallelogram are equal.

[5]

**QUESTION 10**

In the diagram below, D and E are midpoints of sides AB and BC of  $\Delta ABC$ . Point P is on BC such that  $PA = PB$ . PB cuts DE at R.



Prove that  $\Delta RDB$  is isosceles.

[5]

**TOTAL:** 100**END**

## INFORMATION SHEET

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1+ni)$$

$$A = P(1-ni)$$

$$A = P(1-i)^n$$

$$A = P(1+i)^n$$

$$T_n = a + (n-1)d$$



$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r-1}; r \neq 1$$

$$S_\infty = \frac{a}{1-r}; -1 < r < 1$$

$$F = \frac{x[(1+i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x-a)^2 + (y-b)^2 = r^2$$

$$\text{In } \Delta ABC: \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{area } \Delta ABC = \frac{1}{2} ab \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases}$$

$$\sin 2\alpha = 2\sin \alpha \cos \alpha$$

$$\bar{x} = \frac{\sum x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$



$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$



**NOVEMBER EXAMINATION ANSWER BOOK**  
**NOVEMBER EKSAMEN-ANTWOORDBOEK**

2022

CANDIDATE'S NAME <i>LEERDER SE NAAM</i>							
DATE <i>DATUM</i>							
TEACHER <i>ONDERWYSER</i>							
SUBJECT NAME <i>VAKNAAM</i>	<b>MATHEMATICS/WISKUNDE</b>						
BOOK NUMBER <i>BOEKNOMMER</i>		OF <i>VAN</i>		BOOKS <i>BOEKE</i>			
PAPER NUMBER/ <i>VRAESTELNOMMER</i>	2						

This answer book consists of 14 pages./Hierdie antwoordboek bestaan uit 14 bladsye.

MARKER/NASIENER				MODERATOR'S INITIALS IN RELEVANT BLOCK <i>MODERATOR SE PARAAF IN BETROKKE BLOKKIE</i>					
Question <i>Vraag</i>	Marks <i>Punte</i>		Marker's Code & Initials/Nasiener se <i>Kode en parafeer</i>	Marks <i>Punte</i>					
1									
2									
3									
4									
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8									
9									
10									

				<b>TOTAL</b> <i>TOTAAL</i>					

READ THE INSTRUCTIONS ON THE NEXT PAGE.  
*LEES DIE INSTRUKSIES OP DIE VOLGENDE BLADSY.*



**FOLLOW THESE INSTRUCTIONS  
CAREFULLY.**

1. Answer ALL questions in the spaces provided.
2. No pages may be torn from this answer book.  

3. Candidates may not retain an answer book or remove it from the examination room. Answer books must be returned to the invigilator at the end of the examination session.
4. Answers must be written in blue ink as distinctly as possible. Do not write in the margins.
5. Rule-off through any work/rough work that must not be marked.
6. In the event that you use the additional space provided:
  - 6.1 Write down the number of the question.
  - 6.2 Leave a line and rule-off after your answer.

**VOLG HIERDIE INSTRUKSIES  
NOUKEURIG.**

1. *Beantwoord ALLE vrae in die ruimtes wat voorsien is.*
2. *Geen bladsye mag uit hierdie antwoordboek geskeur word nie.*
3. *Geen antwoordboek mag deur kandidate behou of uit die eksamenlokaal verwyder word nie. Antwoordboeke moet aan die toesighouer terugbesorg word aan die einde van die eksamensessie.*
4. *Skryf antwoorde so duidelik moontlik met swart/blou ink. Moenie in die kantlyn skryf nie.*
5. *Trek 'n netjiese lyn deur enige werk/rofwerk wat nie nagesien moet word nie.*
6. *Ingeval jy die bykomende ruimte wat voorsien word, gebruik:*
  - 6.1 *Skryf die nommer van die vraag neer.*
  - 6.2 *Laat 'n lyn oop en trek 'n lyn na jou antwoord.*

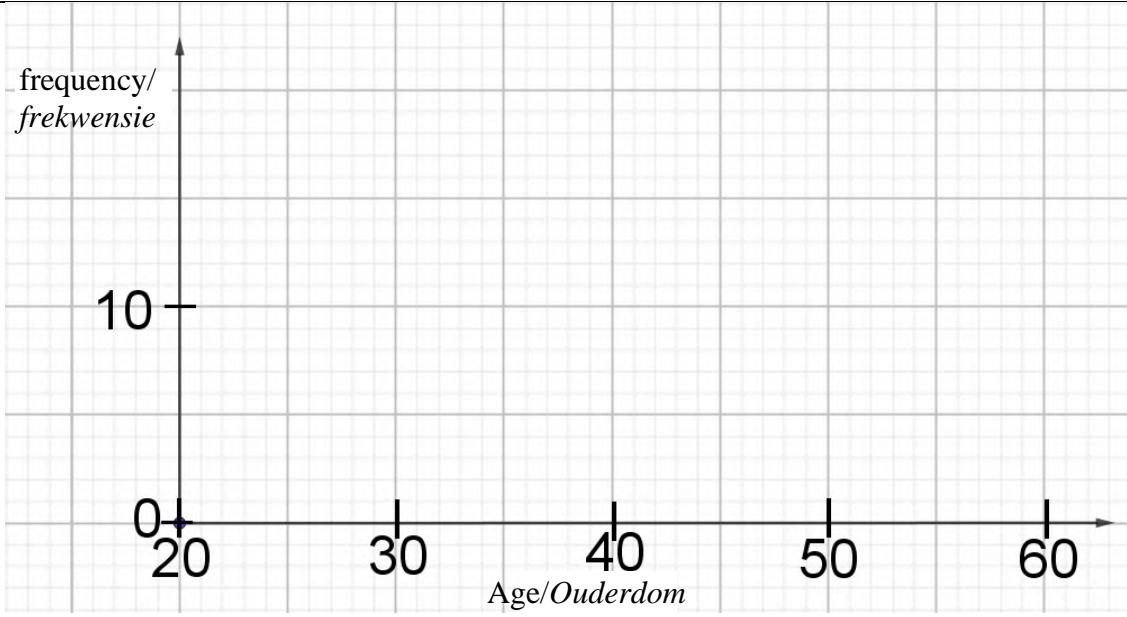
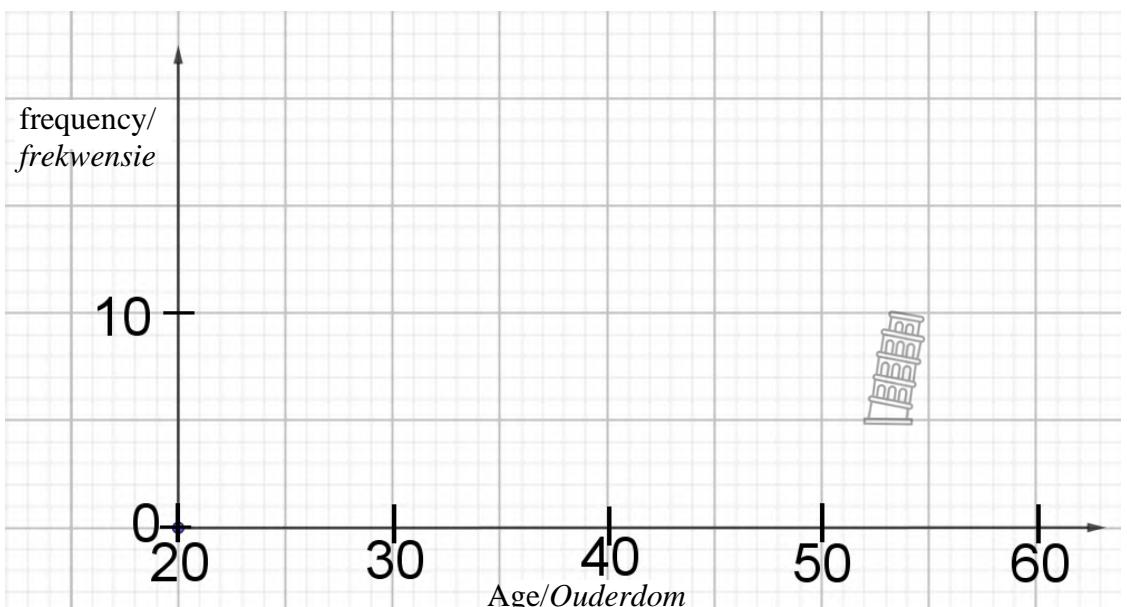


## QUESTION/VRAAG 1

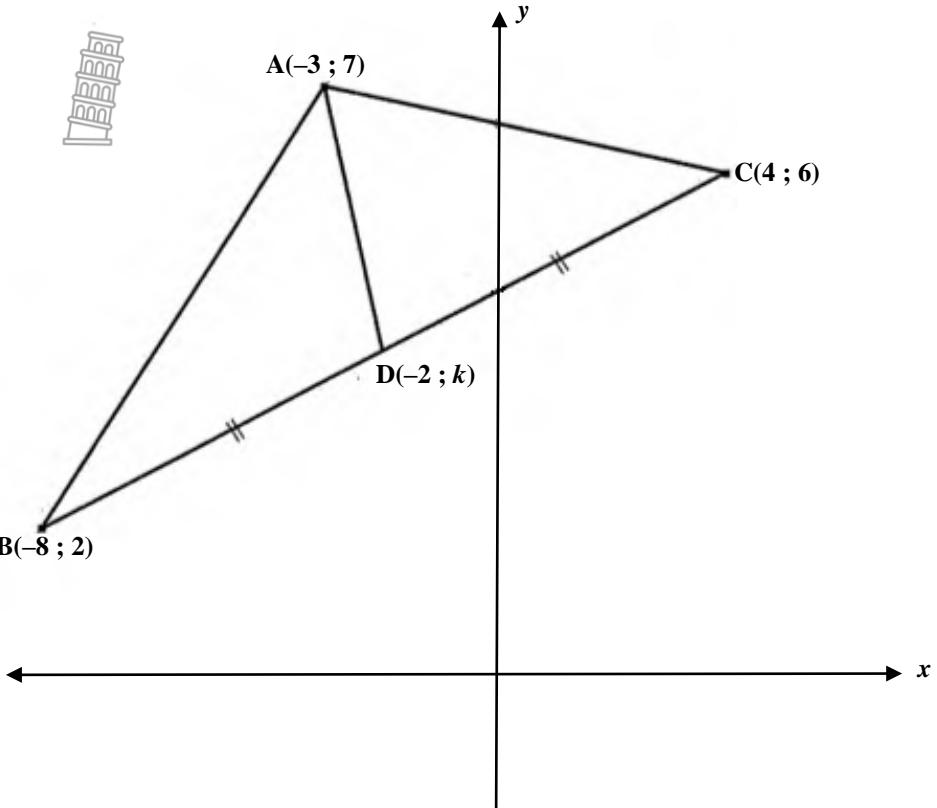
	<b>Solution/Oplossing</b>	<b>Marks/Punte</b>						
1.1	 <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>11</td></tr> <tr><td>12</td></tr> <tr><td>13</td></tr> <tr><td>14</td></tr> <tr><td>15</td></tr> <tr><td>16</td></tr> </table>	11	12	13	14	15	16	
11								
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		(4)						
1.2	1.2.1 <hr/> 1.2.2 <hr/> 1.2.3 <hr/> 1.2.4 <hr/> <hr/> <hr/> <hr/>	(2)  (1)  (2)  (2)						
		[11]						

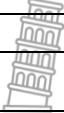


## QUESTION/VRAAG 2

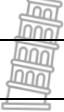
	Solution/Oplossing	Marks/Punte															
2.1	<table border="1"> <thead> <tr> <th>AGE INTERVALS/ OUDERDOMSINTERVALE</th> <th>TALLY/ TELLING</th> <th>FREQUENCY/ FREKWENSIE</th> </tr> </thead> <tbody> <tr> <td> <math>25 \leq x &lt; 33</math></td><td></td><td></td></tr> <tr> <td> <math>33 \leq x &lt; 41</math></td><td></td><td></td></tr> <tr> <td> <math>41 \leq x &lt; 49</math></td><td></td><td></td></tr> <tr> <td> <math>49 \leq x &lt; 57</math></td><td></td><td></td></tr> </tbody> </table>	AGE INTERVALS/ OUDERDOMSINTERVALE	TALLY/ TELLING	FREQUENCY/ FREKWENSIE	 $25 \leq x < 33$			 $33 \leq x < 41$			 $41 \leq x < 49$			 $49 \leq x < 57$			(4)
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2.3		(3)															
		[9]															

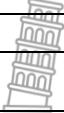
## QUESTION/VRAAG 3

	Solution/Oplossing	Marks/Punte
		
3.1		(2)
3.2		(2)

3.3		
		(2)
3.4		
		(3)
		[9]

**QUESTION/VRAAG 4**

4.1	<b>Solution/<i>Oplossing</i></b>	<b>Marks/ <i>Punte</i></b>
4.1.1		
		(2)
4.1.2		
		(2)
4.1.3		
		(2)

4.2	4.2.1		(2)
4.2.2			(3)
4.2.3			(4)
			[15]

**QUESTION/VRAAG 5**

5.1	Solution/ <i>Oplossing</i>	Marks/ <i>Punte</i>
5.1.1		(4)
5.1.2		(2)



## QUESTION/VRAAG 6

	Solution/ <i>Oplossing</i>	Marks/ <i>Punte</i>
6.1		(1)
6.2		(2)
6.3		(1)
6.4		(2)
6.5		(3)
6.6		(1)
		[10]

**QUESTION/VRAAG 7**

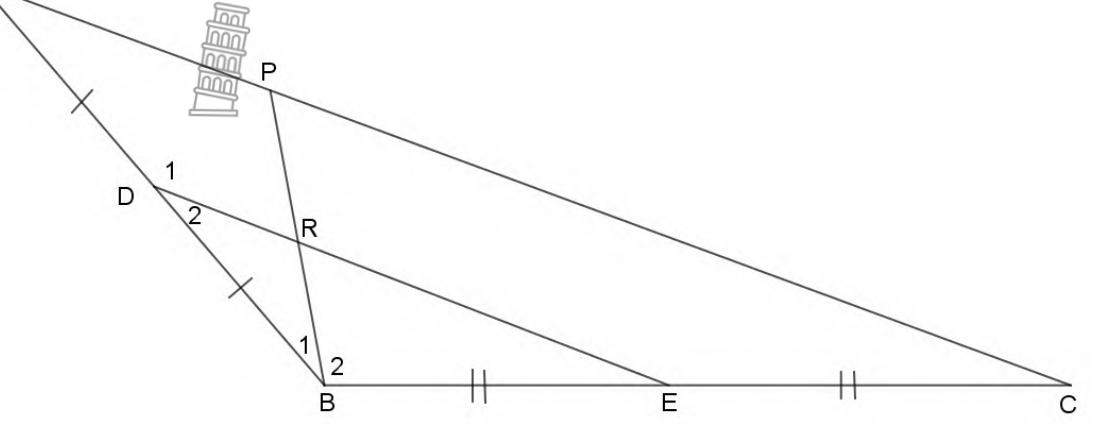
	<b>Solution/<i>Oplossing</i></b>	<b>Marks/ <i>Punte</i></b>
7.1	7.1.1 	(2)
7.1.2		(2)
7.1.3		(2)
7.2	7.2.1	(2)
7.2.2		(2)
7.2.3		(2)
		<b>[12]</b>

**QUESTION/VRAAG 8**

	<b>Solution/Oplossing</b>	<b>Marks/Punte</b>
8.1		(4)
8.2		(4)
		[8]

## **QUESTION/VRAAG 9**

## QUESTION/VRAAG 10

Solution/Oplossing	Marks/Punte
	[5]

	<b>Additional space/<i>Bykomende ruimte</i></b>	<b>Marks/ <i>Punte</i></b>
	 	
		<b>TOTAL/TOTAAL:</b> <b>100</b>



 **PROVINCIAL EXAMINATION/  
PROVINSIALE EKSAMEN**  
**NOVEMBER 2022**  
**GRADE 10/GRAAD 10**  
**MARKING GUIDELINES/  
NASIENRIGLYNE**

**MATHEMATICS (PAPER 2)/WISKUNDE (VRAESTEL 2)**

10 pages/bladsye



## QUESTION/VRAAG 1

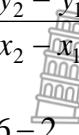
QUESTION/ VRAAG	Suggested solution/ Voorgestelde oplossing		Explanation/ Verduideliking	Marks/ Punte																											
1.1	 <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>11</td><td>0</td></tr> <tr><td>12</td><td>5</td><td>8</td><td>9</td><td>9</td></tr> <tr><td>13</td><td>0</td><td>1</td><td>3</td><td>9</td></tr> <tr><td>14</td><td>2</td><td>3</td><td>7</td><td></td></tr> <tr><td>15</td><td>1</td><td>2</td><td>3</td><td></td></tr> <tr><td>16</td><td>2</td><td>2</td><td>5</td><td></td></tr> </table> <div style="border: 1px solid red; padding: 5px; margin-top: 10px;"> <p>should be in order eg. 0139 <i>moet in volgorde wees bv.0139</i></p> <p>Should be in order eg. 237 <i>moet in volgorde wees bv.0139</i></p> </div>		11	0	12	5	8	9	9	13	0	1	3	9	14	2	3	7		15	1	2	3		16	2	2	5		<ul style="list-style-type: none"> <li>✓ Ist and 2<sup>nd</sup> leaf <i>1<sup>ste</sup> en 2<sup>de</sup> tak</i></li> <li>✓ 3<sup>rd</sup> and 4<sup>th</sup> leaf <i>3<sup>de</sup> en 4<sup>de</sup> tak</i></li> <li>✓ 5<sup>th</sup> and 6<sup>th</sup> leaf <i>5<sup>de</sup> en 6<sup>de</sup> tak</i></li> <li>✓ key/sleutel</li> </ul>	(4)
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13	0	1	3	9																											
14	2	3	7																												
15	1	2	3																												
16	2	2	5																												
1.2	<p>1.2.1</p> $Q_2 = \frac{139 + 142}{2} = 140,5$		<ul style="list-style-type: none"> <li>✓ method/metode</li> <li>✓ answer/antwoord</li> </ul>	(2)																											
1.2.2	129 and/en 162		<ul style="list-style-type: none"> <li>✓ both values <i>beide waardes</i></li> </ul>	(1)																											
1.2.3	Lower Quartile/onderste kwartiel = 129 Upper Quartile/boonste kwartiel = 152		<ul style="list-style-type: none"> <li>✓ answer/antwoord</li> <li>✓ answer/antwoord</li> </ul>	(2)																											
1.2.4	$\bar{x} = \frac{\sum x}{n} = \frac{2531}{18} = 140,61$ <div style="border: 1px solid black; padding: 10px; margin-top: 10px; text-align: center;"> <p>Answer ONLY: FULL marks <i>SLEGS antwoord : VOLPUNTE</i></p> </div>		<ul style="list-style-type: none"> <li>✓ 2 531</li> <li>✓ 140,61</li> </ul>	(2)																											
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## QUESTION/VRAAG 2

QUESTION/ VRAAG	Suggested solution/ Voorgestelde oplossing			Explanation/ Verduideliking	Marks/ Punte															
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AGE INTERVALS <i>OUDERDOMS- INTERVALLE</i>	TALLY/ <i>TELLING</i>	FREQUENCY/ <i>FREKWENSIE</i>																		
$25 \leq x < 33$	-	10																		
$33 \leq x < 41$	-      -	13																		
$41 \leq x < 49$		4																		
$49 \leq x < 57$		3																		
2.2				<ul style="list-style-type: none"> <li>✓ 1<sup>st</sup> and 2<sup>nd</sup> column/ 1<sup>ste</sup> en 2<sup>de</sup> kolomme</li> <li>✓ 3<sup>rd</sup> and 4<sup>th</sup> column/ 3<sup>rde</sup> en 4<sup>de</sup> kolomme</li> </ul>	(2)															
2.3				<ul style="list-style-type: none"> <li>✓ shape/vorm</li> <li>✓ (29;10) (28;13) (45;4) (53; 3)</li> <li>✓ grounding both sides/begronding beide kante At/By (21;0) and/en (61;0)</li> </ul>	(3)															
					[9]															

## QUESTION/VRAAG 3

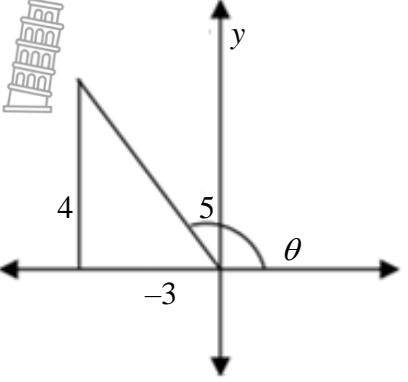
QUESTION/ VRAAG	Suggested solution/ Voorgestelde oplossing	Explanation/ Verduideliking	Marks/ Punte
3.1	$m_{BC} = \frac{y_2 - y_1}{x_2 - x_1}$  $= \frac{6 - 2}{4 + 8}$ $= \frac{1}{4}$	✓ substitution/vervanging ✓ answer/answer	(2)
3.2	$BC = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ $BC = \sqrt{(4 + 8)^2 + (6 - 2)^2}$ $BC = 12,65 \text{ OR } 4\sqrt{10}$	✓ substitution/vervanging ✓ answer/answer	(2)
3.3	$k = \frac{6 + 2}{2}$ $= 4$	✓ correct substitution/ korrekte vervanging ✓ answer/antwoord	(2)
3.4	For $AD \perp BC$ $m_{BC} \times m_{AD} = -1$ $m_{AD} = \frac{7 - 4}{3 + 2}$ $m_{AD} = -3$ $\therefore \frac{1}{4} \times -3 \neq -1$ $\therefore AD \text{ not } \perp BC$ $AD \text{ nie } \perp \text{ op } BC$	✓ deduction/afleiding ✓ substitution/vervanging ✓ answer/antwoord	(3)
			[9]

## QUESTION/VRAAG 4

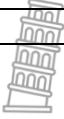
QUESTION/ VRAAG	Suggested solution/ Voorgestelde oplossing	Explanation/ Verduideliking	Punte/ Marks	
4.1    4.1.1	$\cos(x + y)$ $= \cos(66,4^\circ + 114,7^\circ)$ $= \cos(181,1^\circ)$ $= -1,00$ 	✓ substitution/vervanging  ✓ answer/antwoord	(2)	
4.1.2	$2\sin x$ $= 2\sin(66,4^\circ)$ $= 1,83$	✓ substitution/vervanging  ✓ answer/antwoord	(2)	
4.1.3	$\operatorname{cosec} x$ $\frac{1}{\sin(66,4^\circ)}$ $= 1,09$	✓ correct substitution/ korrekte vervanging  ✓ answer/antwoord	(2)	
4.2    4.2.1	$\sin \theta + 0,38 = 1$ $\sin \theta = 0,62$ $\theta = 38,3^\circ$	Penalise 1 mark for incorrect rounding off/ Penaliseer 1 punt vir verkeerde afronding	✓ 0,62  ✓ answer/antwoord	(2)
4.2.2	$2 \cot 2\theta = 3$ $2 \cot 2\theta = \frac{3}{2}$ $2\theta = \tan^{-1}(\frac{2}{3})$ $2\theta = 33,69 \dots^\circ$ $\theta = 16,8^\circ$	✓ $\frac{3}{2}$  ✓ $\tan^{-1}(\frac{2}{3})$ OR/OF $2\theta = 33,69 \dots^\circ$ ✓ answer/antwoord	(3)	
4.2.3	$2 \cos(3\theta - 60^\circ) = 1,71$ $\cos(3\theta - 60^\circ) = 0,855$ $3\theta - 60^\circ = 31,24 \dots^\circ$ $3\theta = 91,24 \dots^\circ$ $\theta = 30,4^\circ$	✓ 0,855  ✓ $3\theta - 60^\circ = 31,24^\circ$ ✓ $3\theta = 91,24^\circ$ ✓ answer/antwoord	(4)	
			[15]	



## QUESTION/VRAAG 5

QUESTION/VRAAG	Suggested solution/ Voorgestelde oplossing	Explanation/ Verduideliking	Punte/Marks
5.1    5.1.1	 $y^2 = (5)^2 - (4)^2 \quad \text{Pythagoras; } 90^\circ \angle$ $y^2 = 25 - 16$ $y = -3$ $\tan \theta = -\frac{4}{3}$	✓ diagram ✓ S ✓ $y = -3$ ✓ answer/antwoord	(4)
5.1.2	$2\cos^2 \theta - 1$ $= 2(-\frac{3}{5})^2 - 1$ $= -\frac{7}{25}$	✓ $2(-\frac{3}{5})^2 - 1$ ✓ answer/antwoord	(2)
5.2	$\cos 0^\circ + \sin^2 60^\circ + \sqrt{2} \cdot \sec 45^\circ$ $= 1 + \left(\frac{\sqrt{3}}{2}\right)^2 + \sqrt{2} \cdot \frac{2}{\sqrt{2}}.$ $3\frac{3}{4} \text{ OR/OF } \frac{15}{4}$	✓ 1 ✓ $\left(\frac{\sqrt{3}}{2}\right)^2$ ✓ $\sqrt{2} \cdot \frac{2}{\sqrt{2}}$ ✓ answer/antwoord	(4)
5.3	Distance/Afstand DB: $\tan 21^\circ = \frac{DB}{30}$ $DB = 11,515 \dots m$ Distance/Afstand BC: $\tan 15^\circ = \frac{BC}{30}$ $BC = 8,038 \dots m$ $\therefore DC = 11,515 m - 8,038 m$ $\therefore DC = 3,48$	✓ $\tan 21^\circ = \frac{DB}{30}$ ✓ $DB = 11,515 m$ ✓ $\tan 15^\circ = \frac{BC}{30}$ ✓ $BC = 8,038 m$ ✓ $DC = 11,515 m - 8,038 m$ ✓ answer/antwoord	(6)
			[16]

## QUESTION/VRAAG 6

QUESTION/ VRAAG	Suggested solution/ <i>Voorgestelde oplossing</i>	Explanation/ <i>Verduideliking</i>	Punte/ Marks
6.1	$a = 1$	✓ 1	(1)
6.2	$y \in [0;2]$ <b>OR/OF</b> $0 \leq y \leq 2; y \in \mathbb{R}$ <div style="text-align: center;">  <p><b>NOTE/NOTA</b></p> <p>In this type of answers – look at values and give the mark. Then look at inequalities. If values are wrong, then ZERO marks</p> <p><i>In hierdie tipe antwoorde – kyk na waardes en gee die punt. Kyk dan na ongelykhede. As waardes verkeerd is, dan NUL</i></p> </div>	✓ critical values/kritieke waardes ✓ notation/notasie	
6.3	1	✓ 1	(1)
6.4	$90^\circ \leq x \leq 180^\circ$ <b>OR/OF</b> $x \in [90^\circ;180^\circ]$ <div style="text-align: center;"> <p>See note above <i>Sien nota hierbo</i></p> </div>	✓ values/waardes ✓ inequality signs/ <i>ongelykheidstekens</i>	(2)
6.5	$x = 0^\circ$ or/of $x = 270^\circ$ or/of $x = 360^\circ$	✓ $x = 0^\circ$ ✓ $x = 270^\circ$ ✓ $x = 360^\circ$	(3)
6.6	$h(x) = -\sin x$	✓ answer/antwoord	(1)
			[10]



## QUESTION/VRAAG 7

QUESTION/ VRAAG		Suggested solution/ <i>Voorgestelde oplossing</i>	Explanation/ <i>Verduideliking</i>	Punte/ Marks
7.1	7.1.1	$AH^2 = 0,8^2 + 1,5^2$ $AH^2 = 2,89$ $AH = 1,7 \text{ m}$ 	✓ $AH^2 = 0,8^2 + 1,5^2$ ✓ answer/antwoord	(2)
	7.1.2	Surface area of roof/Buite-oppv van dak $= 4 \times \frac{1}{2} (3 \times 1,7)$ $= 10,2 \text{ m}^2$	✓ $4 \times \frac{1}{2} (3 \times 1,7)$ ✓ answer/antwoord	(2)
	7.1.3	Surface area of walls/Buite-oppv van mure $= 4 \times 3 \times 2,1$ $= 25,2 \text{ m}^2$ Total surface area/Totale oppv $= 10,2 \text{ m}^2 + 25,2 \text{ m}^2 = 35,4 \text{ m}^2$	✓ $= 25,2 \text{ m}^2$ ✓ answer/antwoord	(2)



QUESTION/ VRAAG	Suggested solution/ Voorgestelde oplossing	Explanation/ Verduideliking	Punte/ Marks
7.2 7.2.1	$\text{Volume} = \frac{4}{3} \pi r^3$ $= \frac{4}{3} \pi \times 8^3$  $= 2\ 144,62 \text{ m}^3$	$\checkmark = \frac{4}{3} \pi \times 8^3$ $\checkmark \text{ answer/antwoord}$	(2)
7.2.2	New volume/Nuwe volume : Orig volume/Oorspronklike volume $= 2^3 : 1$ $= 8:1$	$\checkmark 2^3$ $\checkmark \text{ answer/antwoord}$	(2)
7.2.3	Volume including silver/Volume met silwer ingesluit $= \frac{4}{3} \pi \times 9^3 = 3\ 053,66 \text{ mm}^3$ Volume of silver/Volume van silwer $= 3\ 053,66 - 2\ 144,62 = 908, \text{ mm}^3$	$\checkmark \frac{4}{3} \pi \times 9^3$ $\checkmark \text{ answer/antwoord}$	(2)
			[12]

## QUESTION/VRAAG 8

8.1	$\hat{P}_1 = \hat{P}_2 = x$ $\hat{S}_1 = \hat{S}_2 = y$ $x + x + y + y = 180^\circ$ $2x + 2y = 180^\circ$ $\therefore x + y = 90^\circ$	[given/gegee] [given/gegee] [co-interior $< s$ PQ // SR/ ko-binne $<^e$ ; PQ // SR]	$\checkmark S$ $\checkmark S$ $\checkmark S \checkmark R$	(4)
8.2	$\hat{W}_1 + x + y = 180^\circ$ $\hat{W}_1 = 90^\circ$  PWST is a parallelogram/ PWST is 'n parallelogram  $\therefore$ PWST is a rectangle PWST is 'n reghoek	[sum int $<$ of $\Delta$ / som binne $<^e$ van $\Delta$ ]  [both pairs of opp sides parallel/albei pare teenoorstaande sye ewewydig]	$\checkmark S/R$ $\checkmark S$  $\checkmark S$ $\checkmark R$	
				[8]

## **QUESTION/VRAAG 9**

$BD = BD$	[common/gemeenskaplik]	✓ S	
$\hat{D}_1 = \hat{B}_2$	[alternate $< s$ AD // BC/ verw. binne $<^e$ ; AD // BC]	✓ S/R	
$\hat{B}_2 = \hat{D}_1$	[alternate $< s$ AB // DC verw. binne $<^e$ ; AB // DC]	✓ S	
$\therefore \Delta ABC \equiv \Delta CBD$	[AAS/HHS]	✓ S	
$\therefore AD = BC, AB = DC$	$\Delta'^s/\Delta'^e \equiv$	✓ R	(5)

## **QUESTION/VRAAG 10**

