



Province of the  
**EASTERN CAPE**  
EDUCATION

Umrondi leMpona Kapa; Isibhe leMundo  
Provincie van die Oos-Kaap: Departement van Onderwys  
poratensiya Ya Kapa Botjanabeli; Lafapha Is Thuto

## NATIONAL SENIOR CERTIFICATE

**BUFFALO CITY METRO DISTRICT**

**GRADE 10**

**MATHEMATICS TEST**

**21-08-2025**

**MARKS : 50**

**Time : 1 Hour**

This question paper consists of 6 pages with diagram sheet.

## INSTRUCTIONS AND INFORMATION:

Read the following instructions carefully before answering the questions.

1. This paper consists of **FOUR QUESTIONS**.
2. Answer **ALL** the questions.
3. Clearly show **ALL** calculations, diagrams, graphs, etc. that you have used in determining your answers.
4. Answers only will **NOT** necessarily be awarded full marks.
5. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
6. If necessary, round answers off to **TWO** decimal places, unless stated otherwise.
7. Diagrams are **NOT** necessarily drawn to scale.
8. Write neatly and legibly.

**QUESTION 1**

Given the equation:  $h(x) = \frac{-2}{x} + 2$

1.1 Determine the  $x$ -intercept of  $h$ . (2)

1.2 Calculate the  $y$ -intercept of  $h$ . (2)

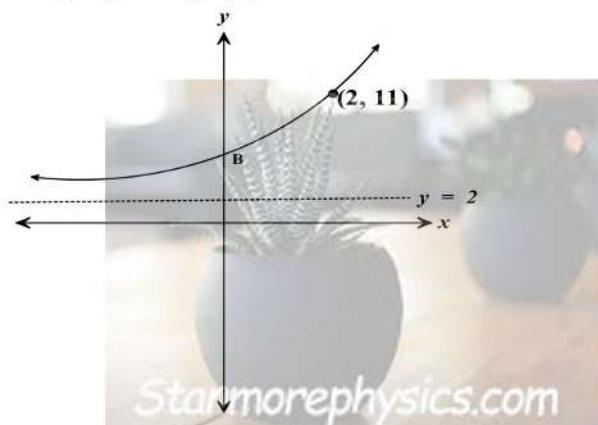
1.3 Write down the equation of asymptotes of  $h$ . (2)

1.4 Hence, sketch the graph of  $h$ . Clearly show all intercepts with the axes and asymptotes. (3)

[9]

**QUESTION 2**

The graph of  $f(x) = a^x + b$  is drawn below. B is the  $y$  intercept of  $f$ .



Use the above graph to answer the following questions:

2.1 Write down the equation of asymptote of  $f$ . (1)

2.2 Determine the values of  $a$  and  $b$ . (3)

2.3 Write down the range of  $f$ . (1)

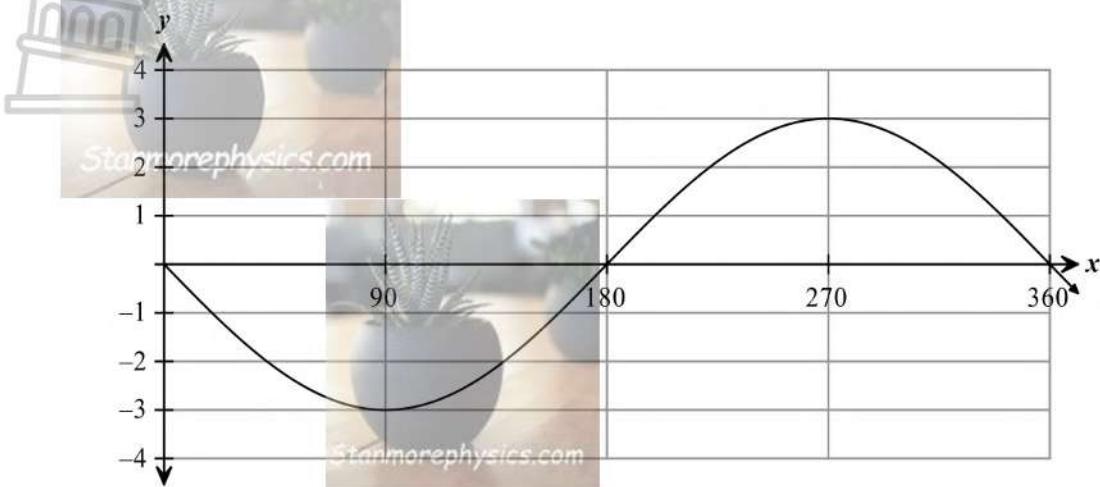
2.4 Determine the coordinates of B. show all your workings. (2)

2.5 Determine the equation of  $t$ , if  $t(x) = 3f(x) - 1$ . (3)

[10]

### QUESTION 3

In the diagram below, the graph of  $f(x) = -3\sin x$  is drawn for the interval of  $0^\circ \leq x \leq 360^\circ$



- 3.1 Write down the amplitude of  $f$ . (1)
- 3.2 Write down the minimum value of  $f(x) + 5$  (1)
- 3.3 On the same set of axes, draw the graph of  $p$ ,  $p(x) = \tan x$  for the interval  $0^\circ \leq x \leq 360^\circ$  (3)
- 3.4 Use the graph to determine the following:
  - 3.4.1 The value of  $f(90^\circ) - p(180^\circ)$  (3)
  - 3.4.2 Determine the equations of asymptotes of  $p$ . (2)
  - 3.4.3 For which values of  $x$  is  $p(x) \leq 0$  (4)
- 3.5 The graph of  $f$  is reflected about x-axis and then moved 2 units upwards to form the graph of  $k$ . Determine:
  - 3.5.1 The equation of  $k$ . (2)
  - 3.5.2 The range of  $k$  for the interval  $0^\circ \leq x \leq 360^\circ$  (2)

[18]

**QUESTION 4**

4.1 Given the equation of  $r(x) = 2\cos x - 1$

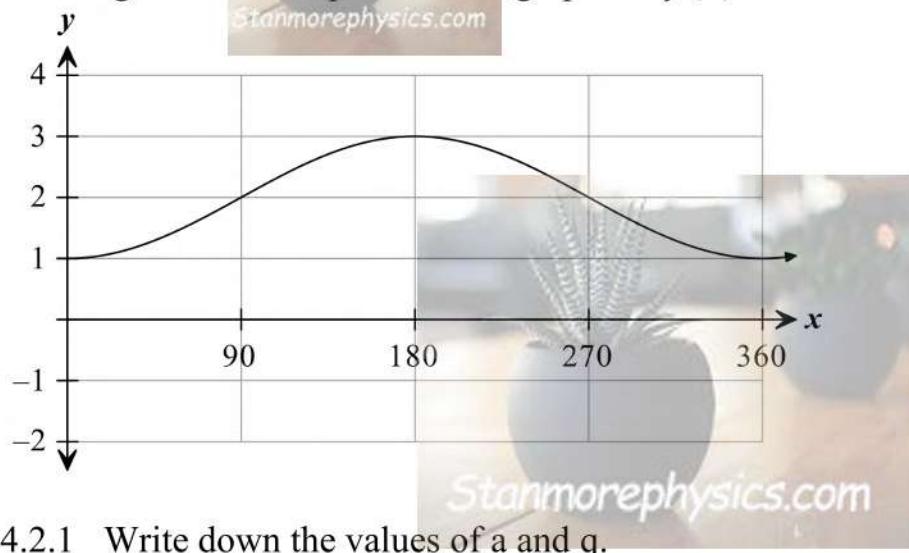
4.1.1 Sketch the graph of  $r$  on the provided grid, for  $x \in [0^\circ; 360^\circ]$  (3)

4.1.2 Write down the period of  $r$ . (1)

4.1.3 Determine the maximum value of  $r$ . (1)

4.1.4 Determine the range of  $r$ . (2)

4.2 The diagram below represents the graphs of  $f(x) = a\cos x + q$



4.2.1 Write down the values of  $a$  and  $q$ . (2)

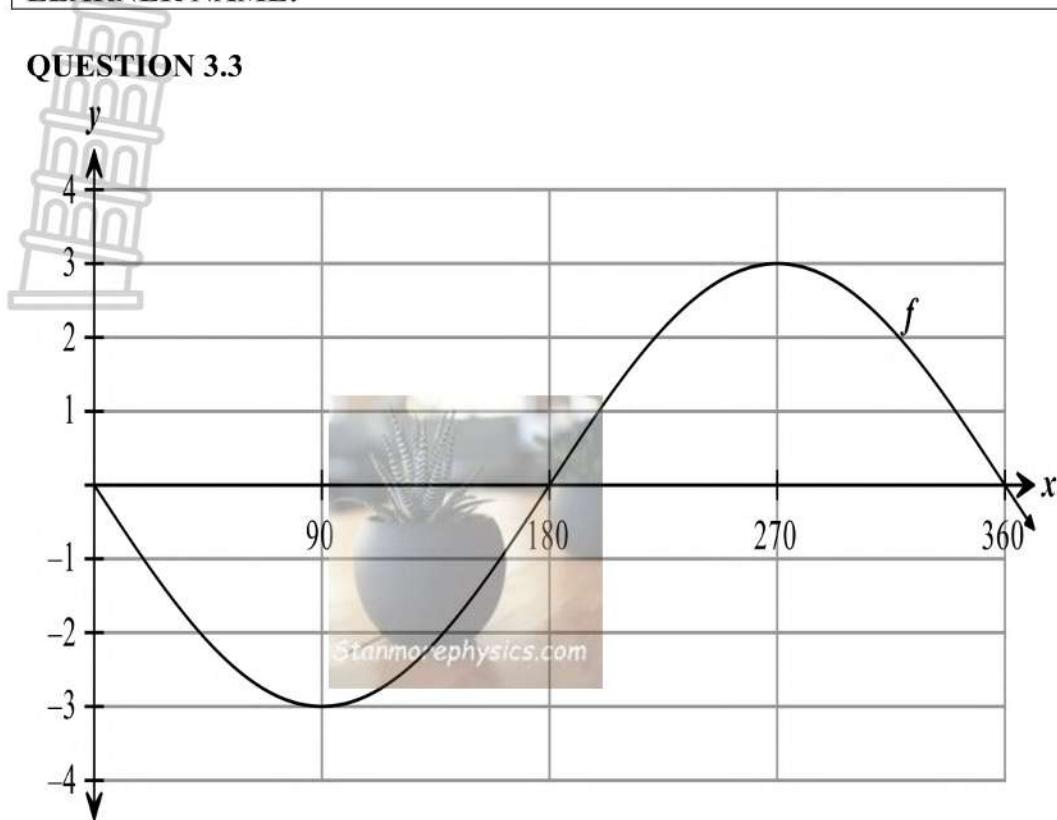
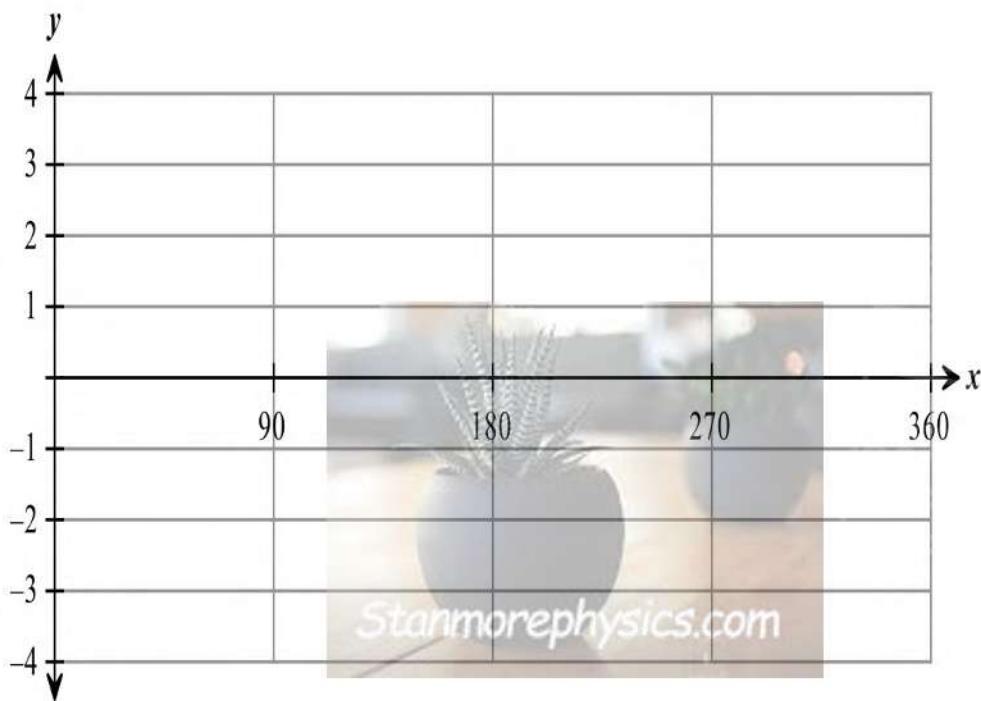
4.2.2 Using the graph for which values of  $x$  is  $f$  a decreasing function. (1)

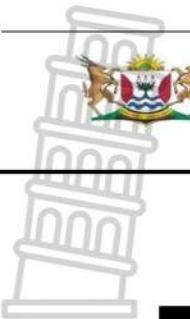
4.2.3 For which values of  $x$  is  $f(x) \geq 2$  (2)

4.2.4 Write down the minimum value of  $f$ , if  $f$  is shifted 3 units downwards. (1)

**[13]**

LEARNER NAME: \_\_\_\_\_

**QUESTION 3.3****QUESTION 4.1.1**



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## NATIONAL SENIOR CERTIFICATE

**BUFFALO CITY METRO DISTRICT**

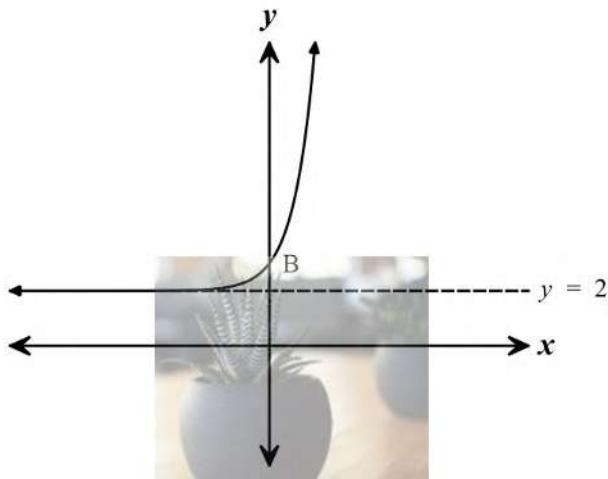
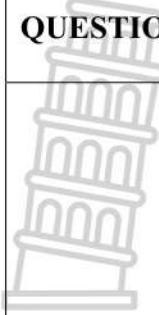
**GRADE 10**  
**MATHEMATICS TEST**  
**MARKING GUIDELINES**

**MARKS : 50**

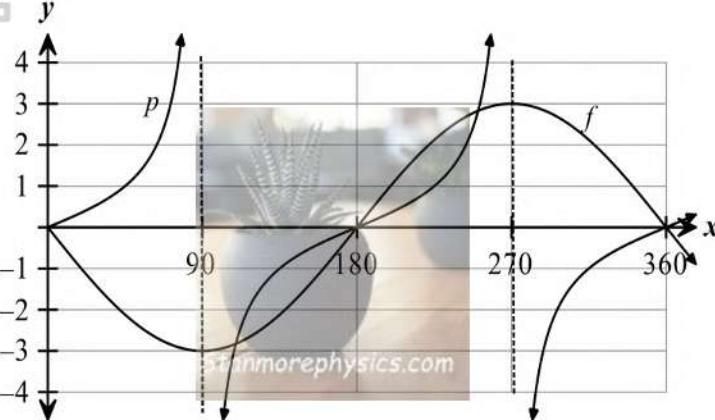
**Time : 1 Hour**

QUESTION 1			
1.1	$x\text{-intercept } (y = 0)$ $0 = \frac{-2}{x} + 2$ $-2 = \frac{-2}{x}$ $-2x = -2$ $x = 1$	$y = 0 \checkmark$ $x = 1 \checkmark$	(2)
1.2	$y \text{ intercept } (x = 0)$ $y = \frac{-2}{0} + 2 \text{ (undefined)}$ $\therefore \text{There is no } y \text{ intercept}$	$x = 0 \checkmark$ <i>Conclusion</i> $\checkmark$	(2)
1.3	$x = 0$ $y = 2$	$x = 0 \checkmark$ $y = 2 \checkmark$	(2)
1.4	<p>The graph shows a rational function with a vertical asymptote at <math>x = 0</math> and a horizontal asymptote at <math>y = 2</math>. The curve passes through the point <math>(1, 0)</math>. The graph is labeled with <math>x</math> and <math>y</math> axes. A dashed horizontal line represents the asymptote <math>y = 2</math>. The curve approaches the vertical asymptote from both sides and approaches the horizontal asymptote as <math>x</math> increases.</p>	Shape $\checkmark$ $x\text{-intercept } \checkmark$ Asymptote $\checkmark$	(3)
			[9]

## QUESTION 2

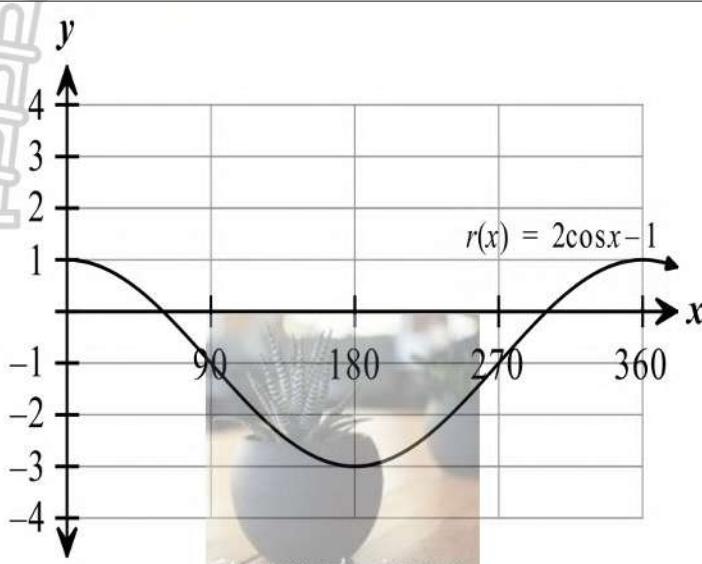


2.1	$y = 2$	$y = 2 \checkmark$	(1)
2.2	$b = 2$ $f(x) = a^x + 2$ at point $(2; 11)$ $11 = a^2 + 2$ $9 = a^2$ $\sqrt{9} = \sqrt{a^2}$ $a = \pm 3, a = 3$	$b = 2 \checkmark$ Substitution $\checkmark$ $a = 3 \checkmark$	(3)
2.3	$y \in \mathbb{R}, y > 2$ OR $y \in (2; \infty)$ <b>ACCEPT:</b> $y > 2$	Answer $\checkmark \checkmark$	(2)
2.4	Since B is the y intercept ( $x = 0$ ) $y = 3^0 + 2$ $y = 3$ $\therefore B(0; 3)$	$x = 0 \checkmark$ $y = 3 \checkmark$	(2)
2.5	$t(x) = 3f(x) - 1$ $t(x) = 3(3^x + 2) - 1$ $t(x) = 3 \cdot 3^x + 6 - 1$ $t(x) = 3^{x+1} + 5$	$3(3^x + 2) - 1 \checkmark$ Simplification $\checkmark$ $3^{x+1} + 5 \checkmark$	(3)
			[10]

QUESTION 3			
3.1	Amplitude = 3	3 ✓	(1)
3.2	Minimum value = $-3 + 5$ Minimum value = 2	2✓	(1)
3.3		Shape ✓ Asymptotes ✓ All intercepts ✓	(3)
3.4.1	$f(90^\circ) - p(180^\circ) \\ = -3 - 0 \\ = -3$ <div style="border: 1px solid black; padding: 5px; margin-left: 20px;"> <b>NOTE:</b> Learner is required to use graph not Algebraically!     </div>	-3 ✓ 0✓ -3✓	(3)
3.4.2	$x = 90^\circ$ $x = 270^\circ$	$x = 90^\circ$ ✓ $x = 270^\circ$ ✓	(2)
3.4.3	$90^\circ < x \leq 180^\circ$ OR $x \in (90^\circ; 180^\circ]$ $270^\circ < x \leq 360$ OR $x \in (270^\circ; 360^\circ]$ <div style="border: 1px solid black; padding: 5px; margin-left: 20px;"> <b>NOTE:</b> Correct notation <math>90^\circ</math> and <math>270^\circ</math> must be excluded on the solution of a learner     </div>	$90^\circ < x \leq 180^\circ$ ✓✓ $270^\circ < x \leq 360$ ✓✓	(4)
3.5.1	$f(x) = -3\sin x$ reflect $f$ on $x$ axis $-y = -3\sin x$ $y = 3\sin x$ moving 2 units upwards $k(x) = 3\sin x + 2$	$3\sin(x) + 2$ ✓✓	(2)
3.5.2	$-1 \leq y \leq 5$ OR $y \in [-1; 5]$ <b>INCORRECT NOTATION: 0 MARKS</b>	Answer ✓✓	(2)
			[18]

## QUESTION 4

4.1.1



Shape ✓  
Turning point ✓  
y-intercept ✓

(3)

4.1.2 Period =  $360^\circ$ 

Answer ✓

(1)

4.1.3 Maximum value = 1

Answer ✓

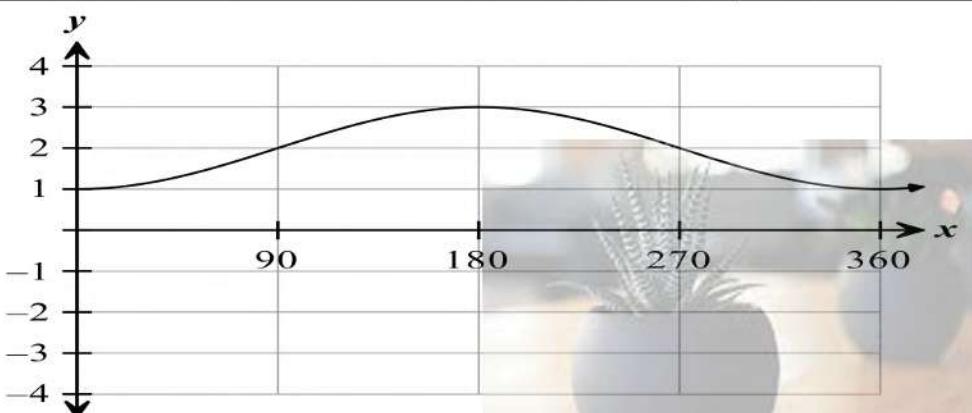
(1)

4.1.4  $-3 \leq y \leq 1$  OR  $y \in [-3; 1]$ 

Answer ✓✓

(2)

4.2

4.2.1  $a = -1$   
 $q = 2$ 

*Stanmorephysics.com*  
 $a = -1$  ✓  
 $q = 2$  ✓

(2)

4.2.2  $180^\circ \leq x \leq 360^\circ$   
ACCEPT:  $180^\circ < x < 360^\circ$ 

Answer ✓

(1)

4.2.3  $90^\circ \leq x \leq 270^\circ$ 

Answer ✓✓

(2)

4.2.4 Minimum value =  $1 - 3 = -2$ 

-2 ✓

(1)

[13]